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Temperature Waves In Layered Correlated Materials And Temperonic Crystals

Marco Gandolfi

Giacomo Mazza,
Massimo Capone,
Francesco Banfi,
Claudio Giannetti

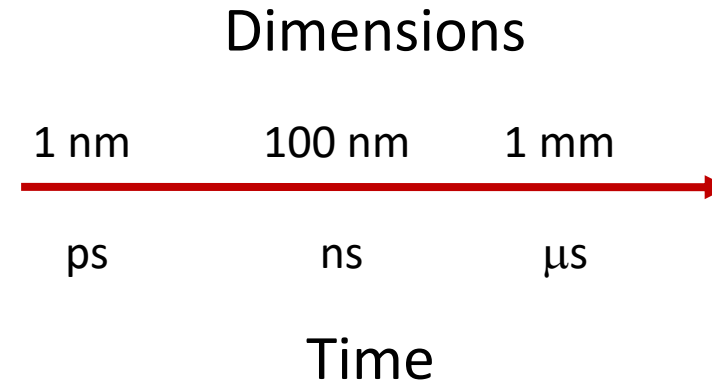
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Beyond Fourier Paris 2022

9th September 2022



Nano-scale heat transport



Beyond Fourier's Law ... a dispersion relation perspective

Temperature waves: graphite and correlated materials

Temperonic Crystal



$$\mathbf{q}(\mathbf{x}, t) = -k_T \nabla T(\mathbf{x}, t)$$



no causality

Dual-Phase-Lag-Model

$$\mathbf{q}(\mathbf{x}, t + \tau_q) = -k_T \nabla T(\mathbf{x}, t + \tau_T)$$



+ conservation of energy

$$\left(\frac{\tau_q}{\alpha}\right) \frac{\partial^2 T}{\partial t^2} - \frac{\partial^2 T}{\partial x^2} + \frac{1}{\alpha} \frac{\partial T}{\partial t} - \tau_T \frac{\partial^3 T}{\partial x^2 \partial t} = 0$$

Beyond Fourier's Law



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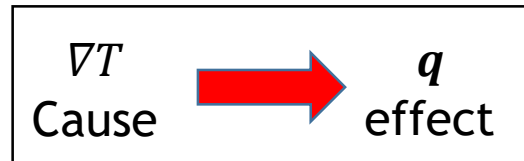
$$\left(\frac{\tau_q}{\alpha} \frac{\partial^2 T}{\partial t^2} - \frac{\partial^2 T}{\partial x^2} \right) + \frac{1}{\alpha} \frac{\partial T}{\partial t} - \tau_T \frac{\partial^3 T}{\partial x^2 \partial t} = 0$$

Waves

Diffusion
damping

Damping

$$\tau_q > \tau_T$$



Beyond Fourier's Law



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no causality

Dual-Phase-Lag-Model

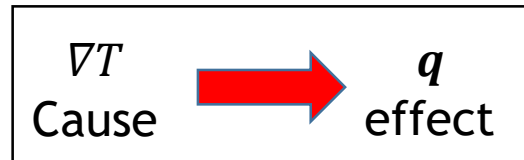
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Temperature «wave»

$$\mathbf{q}(\mathbf{x}, t) = -k_T \nabla T(\mathbf{x}, t)$$



no causality

Dual-Phase-Lag-Model

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Accessing temperature waves: A dispersion relation perspective

Marco Gandolfi ^{a, b}, Giulio Benetti ^{c, b}, Christ Glorieux ^a, Claudio Giannetti ^b, Francesco Banfi ^d

Frequency ω

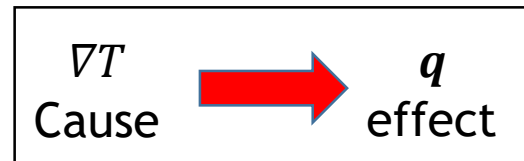
Wave vector k

Dispersion relation:

$$(1 + i\omega\tau_T)k^2 = \left(\frac{\tau_q}{\alpha}\right) \left(1 - \frac{i}{\omega\tau_q}\right) \omega^2$$

Q-factor

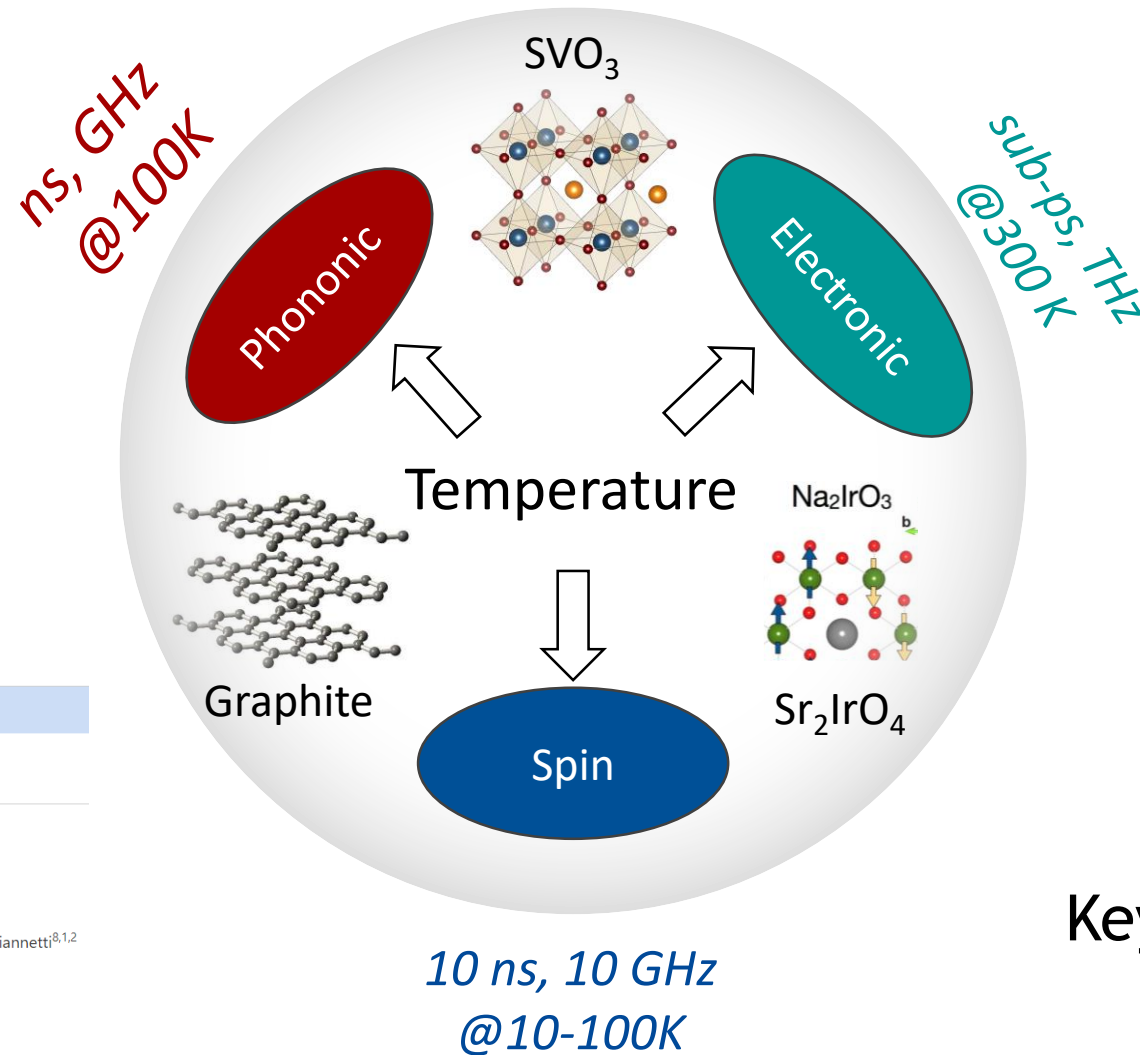
$$\tau_q > \tau_T$$

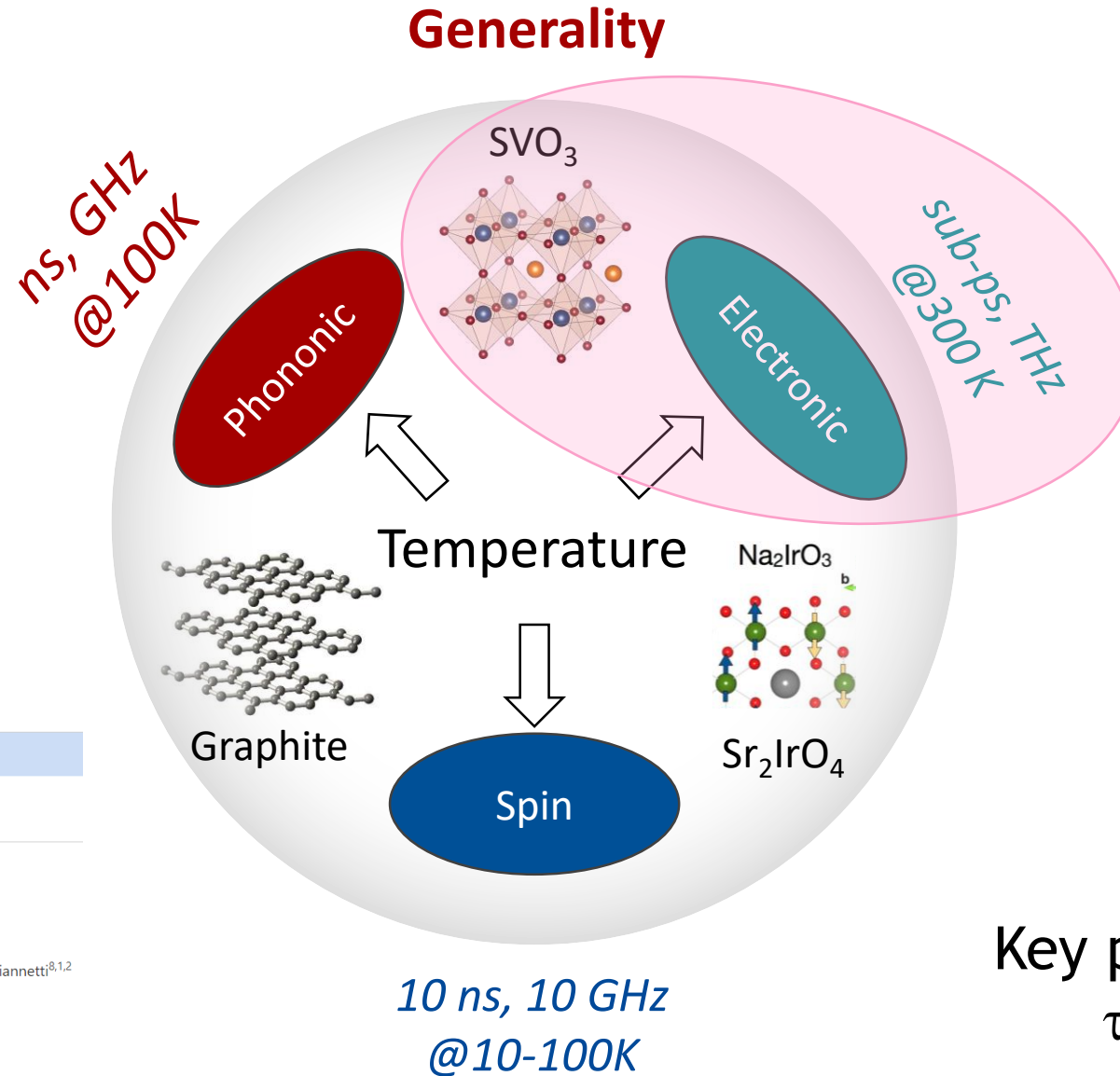


Temperature «wave»

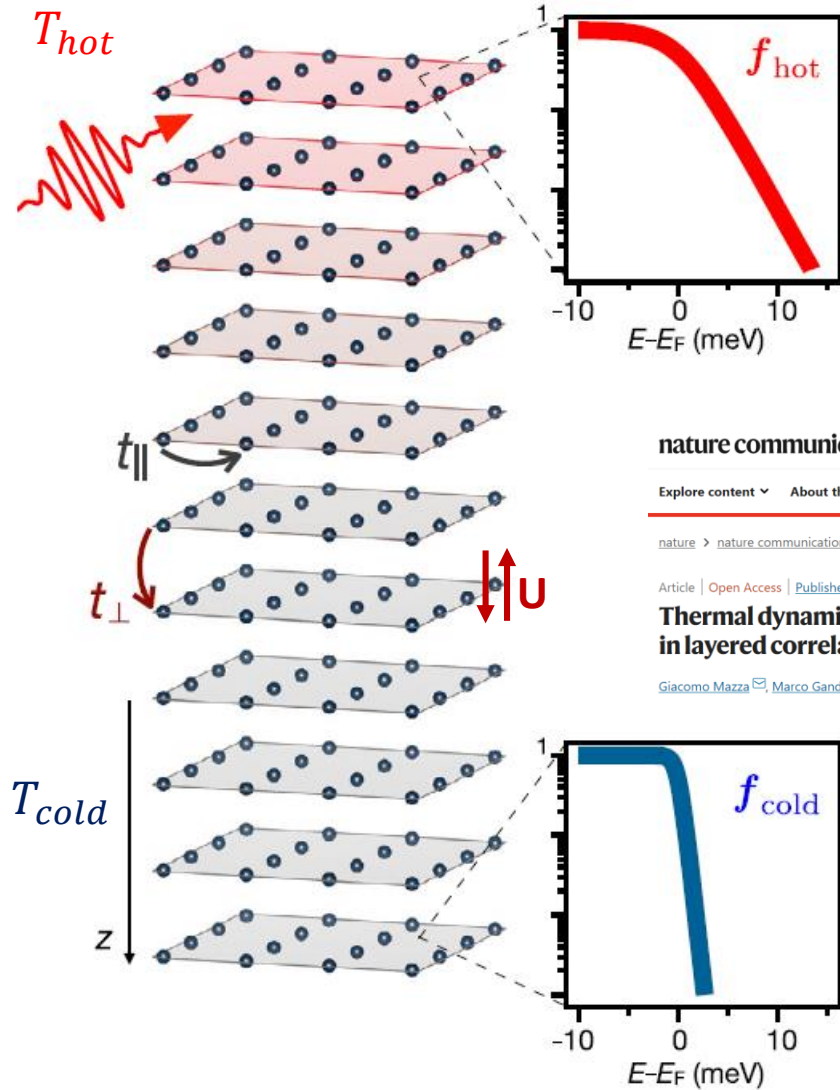


Generality





Layered Correlated Materials



Hubbard Model

$$H = \sum_{n=1}^L h_n + \sum_{n=1}^{L-1} \tau_{n,n+1}$$

$$h_n = \sum_{\langle i,j \rangle_{\sigma}} t_{\parallel} c_{in\sigma}^{\dagger} c_{jn\sigma} + U \sum_i n_{in\uparrow} n_{in\downarrow}$$

$$\tau_{n,n+1} = \sum_{\sigma} t_{\perp} c_{in\sigma}^{\dagger} c_{in+1\sigma} + h.c.$$

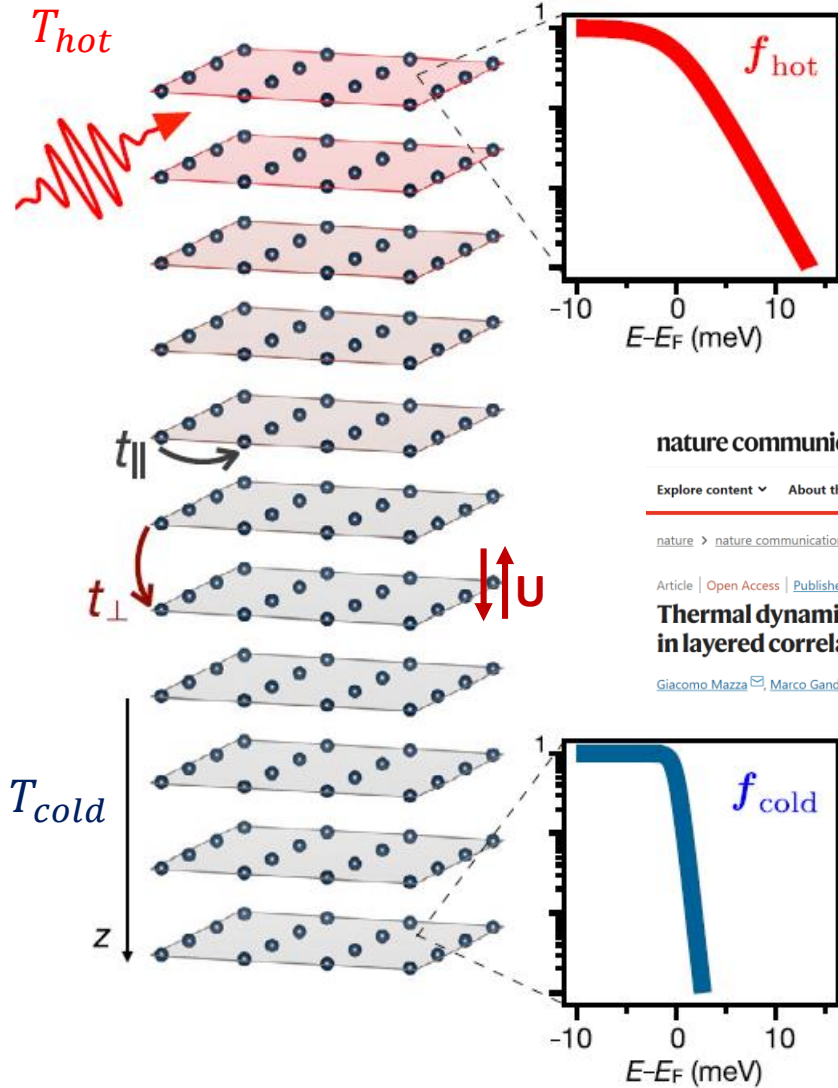
t_{\parallel} interlayer hopping

t_{\perp} intra-layer hopping

U Coulomb interaction

G. Mazza et al., *Nat. Comm.* (2021)

Layered Correlated Materials

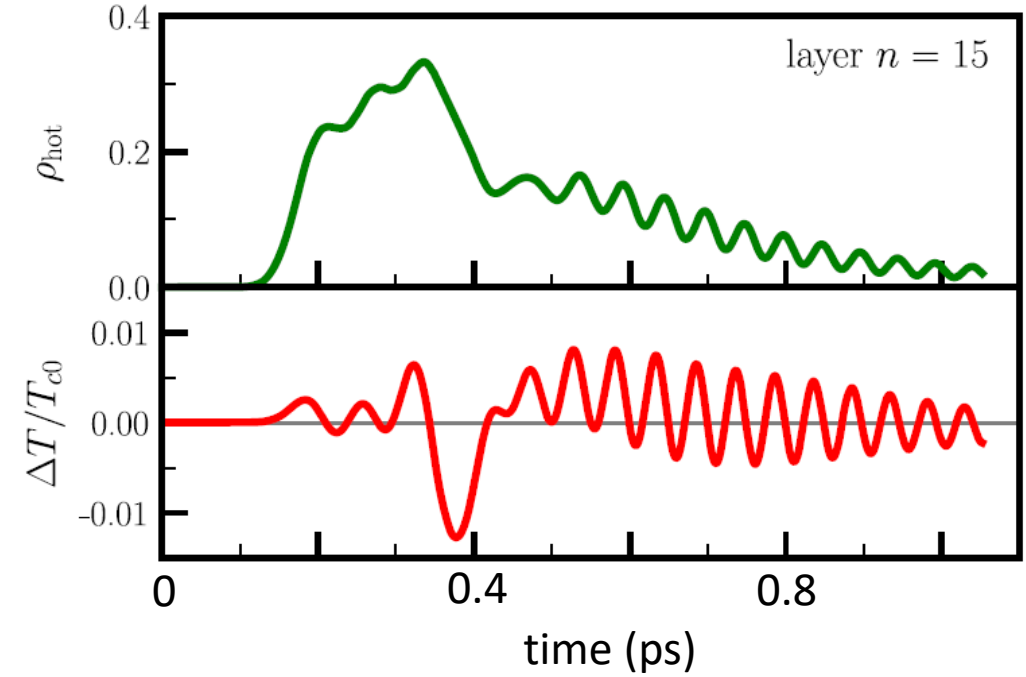


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Thermal dynamics and electronic temperature waves in layered correlated materials
 Giacomo Mazza, Marco Gandolfi, Massimo Capone, Francesco Banfi & Claudio Giannetti

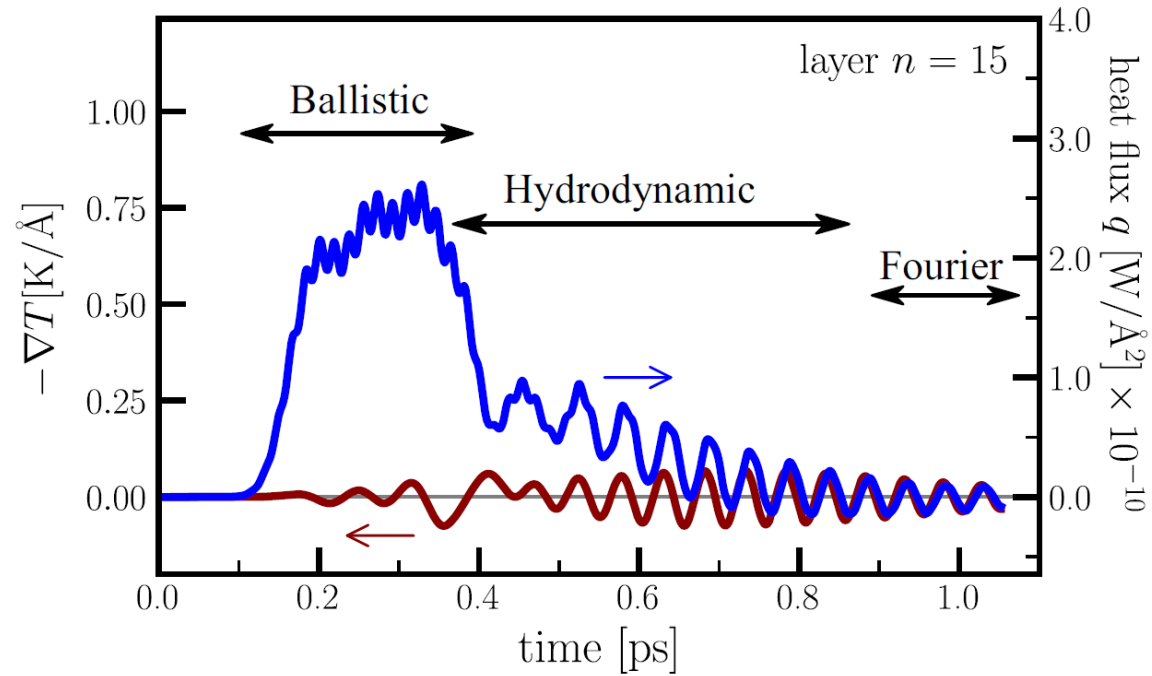
$$N_n^{neq}(\epsilon, t) = f_{hot}\rho_{hot} + f_{cold}(1 - \rho_{hot})$$

$$f_{hot} = \frac{1}{\exp\left(\frac{\epsilon}{k_B T_{hot}}\right) + 1}$$

$$f_{cold} = \frac{1}{\exp\left(\frac{\epsilon}{k_B T_{cold}(n, t)}\right) + 1}$$



Energy density $E_n(t)$ \longrightarrow Heat flux $\frac{\partial q_n}{\partial z} + \frac{\partial E_n}{\partial t} = 0$



- Ballistic: large heat flux, no temperature dynamics
- Hydrodynamic: positive heat flux, temperature oscillations
- Fourier: $q \propto -\nabla T$



For SrVO₃

$\tau_T \sim 5$ fs (scattering time from optics)

$\tau_q \sim 500$ fs (from neq. dynamics)

$k = 10 - 20$ W m⁻¹ K⁻¹

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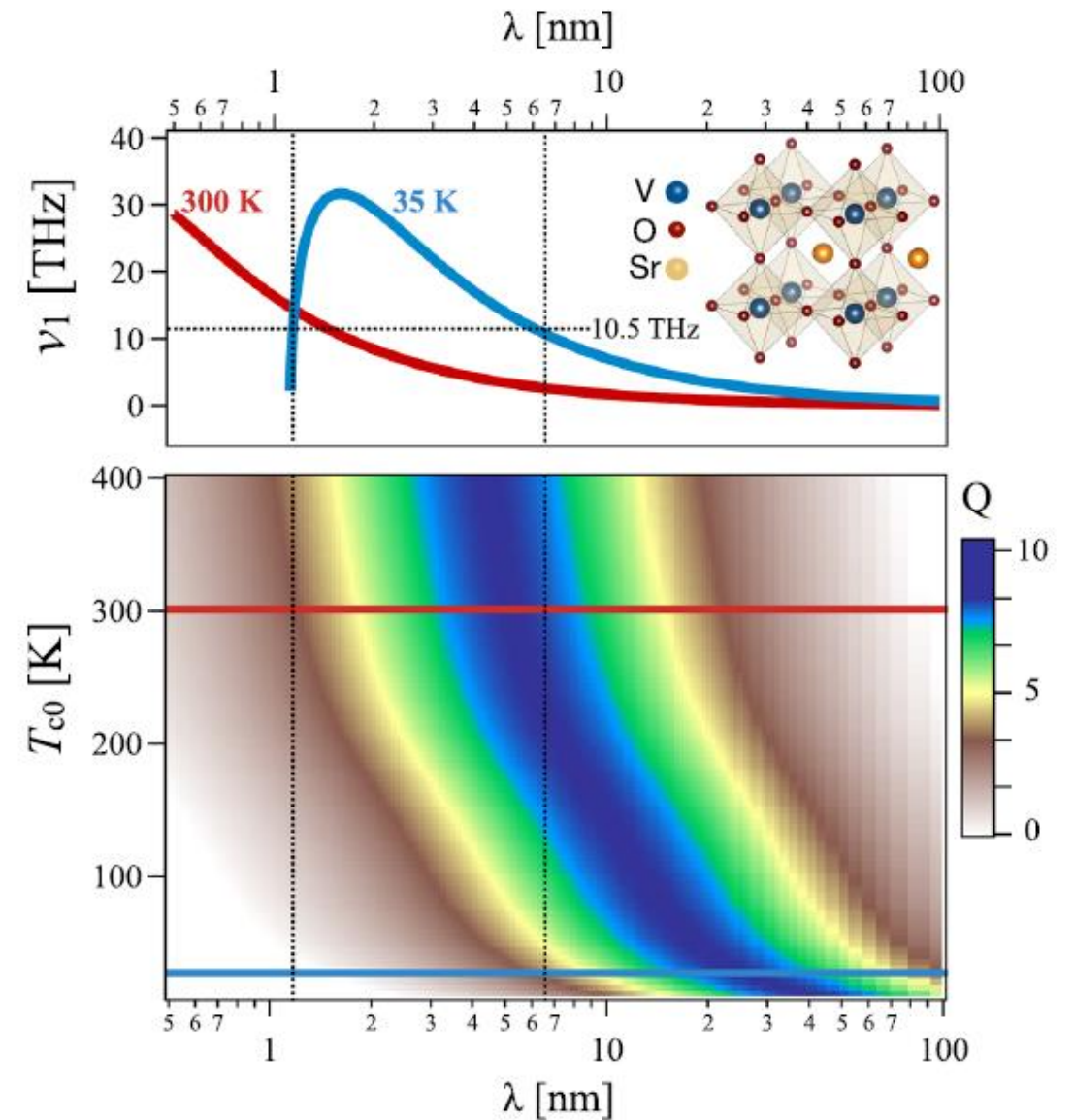
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Temperonic Crystal

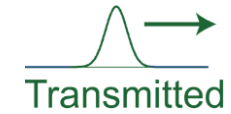
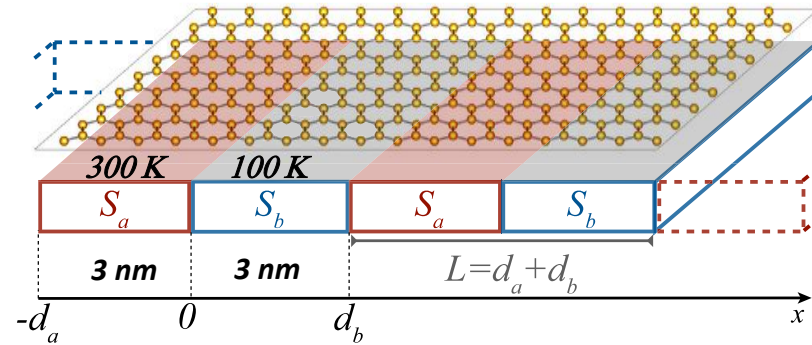
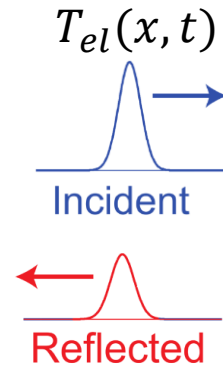
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Temperonic Crystal: A Superlattice for Temperature Waves in Graphene

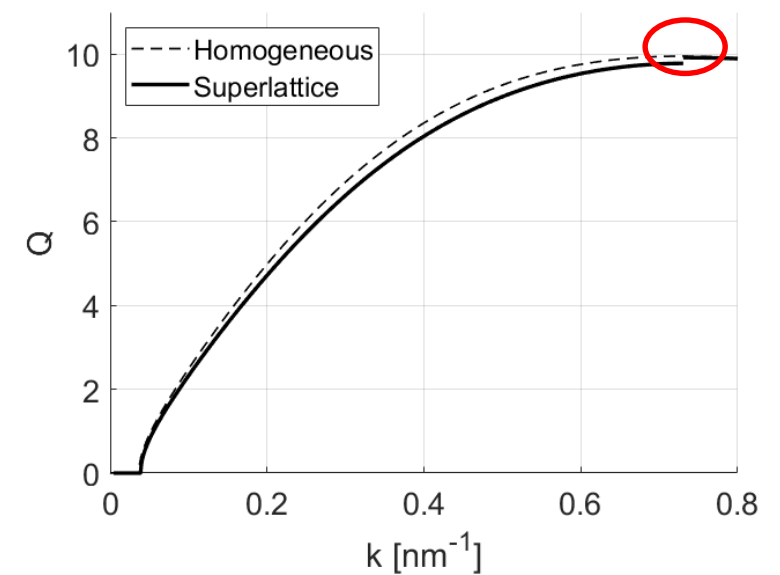
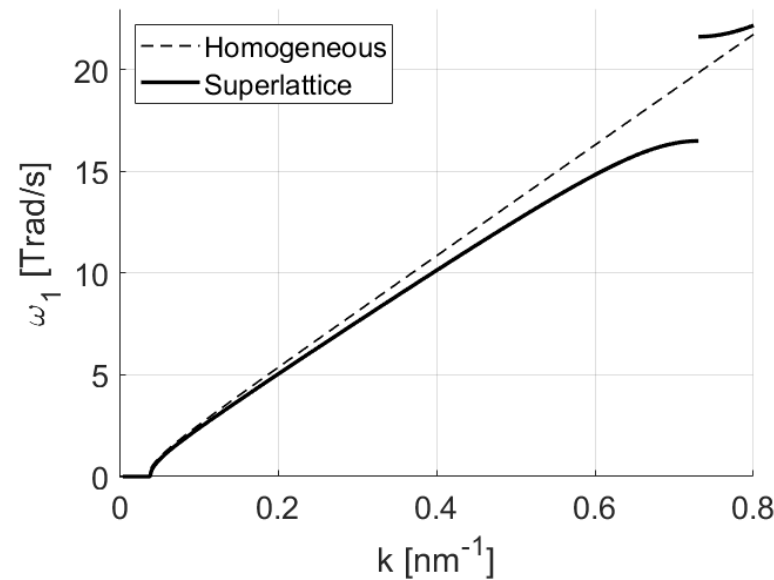
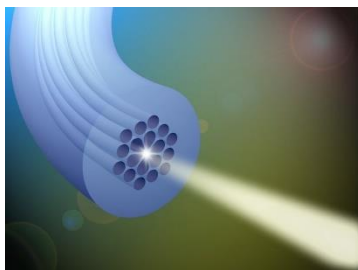
Marco Gandolfi, Claudio Giannetti, and Francesco Barfi
Phys. Rev. Lett. **125**, 265901 – Published 31 December 2020

A Superlattice for Temperature Waves in Correlated Materials

Phononic Crystal



Photonic Crystal



Temperonic Crystal

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Temperonic Crystal: A Superlattice for Temperature Waves in Graphene

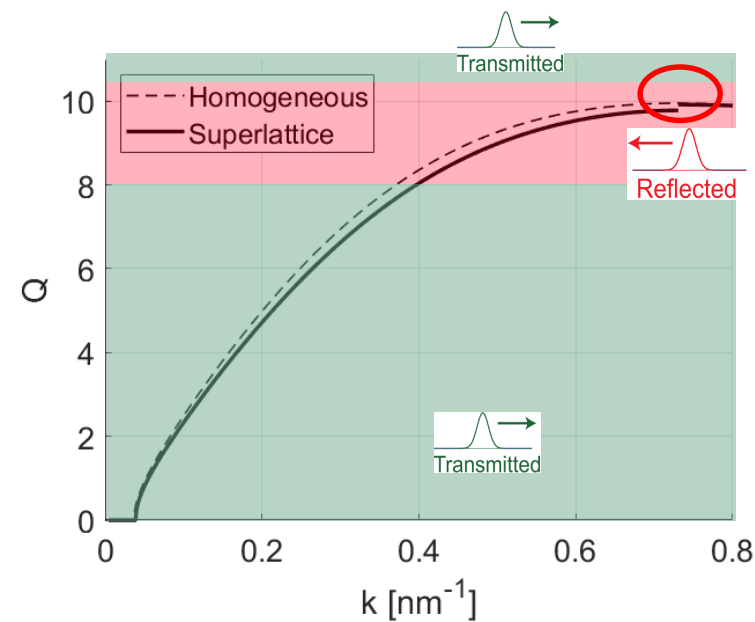
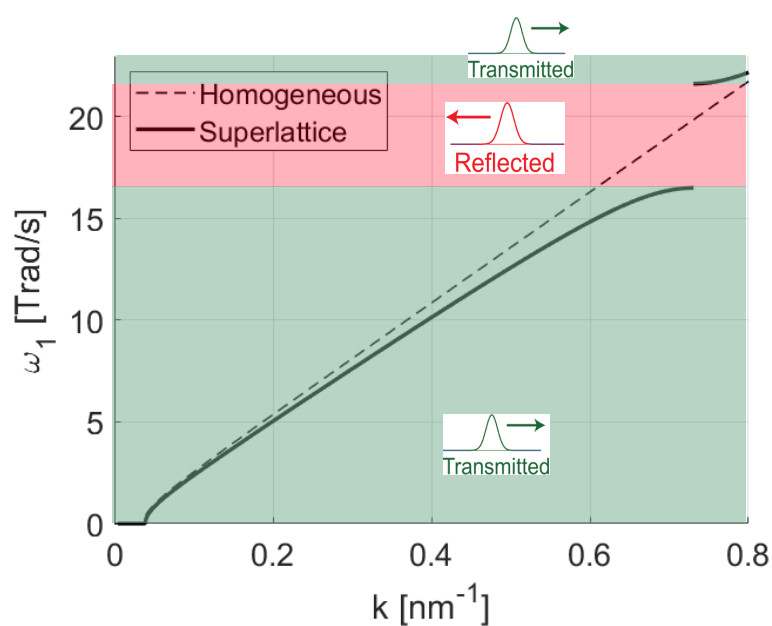
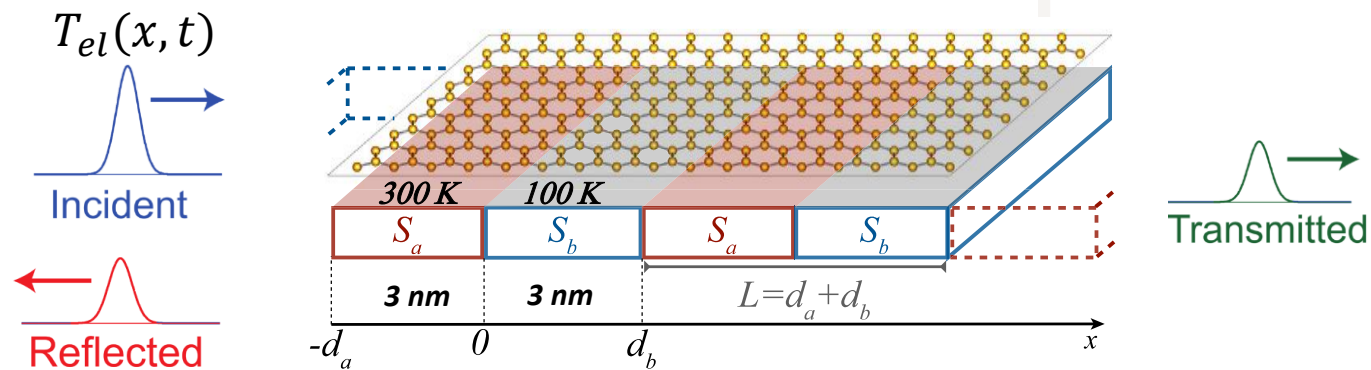
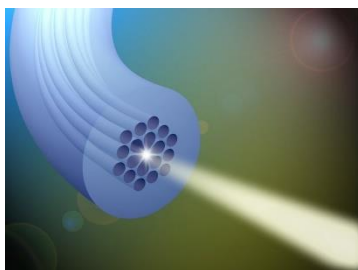
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A Superlattice for Temperature Waves in Correlated Materials

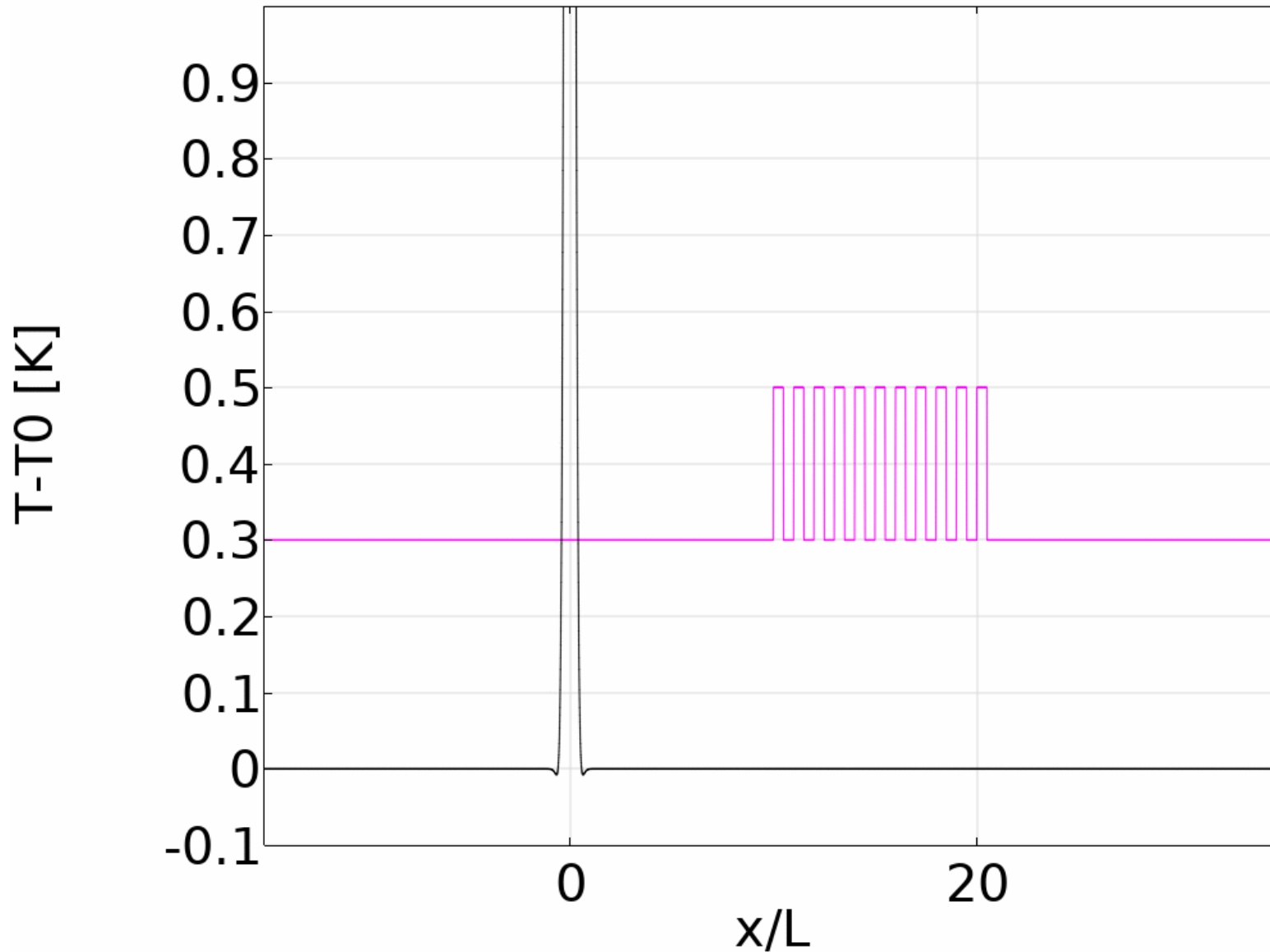
Phononic Crystal



Photonic Crystal



Spatio-temporal evolution of temperature



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Temperonic Crystal: A Superlattice for Temperature Waves in Graphene

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Temperonic crystal:

extendible to graphene...



Beyond Fourier's Law ... a dispersion relation perspective

Temperonic Materials

Temperonic Crystal

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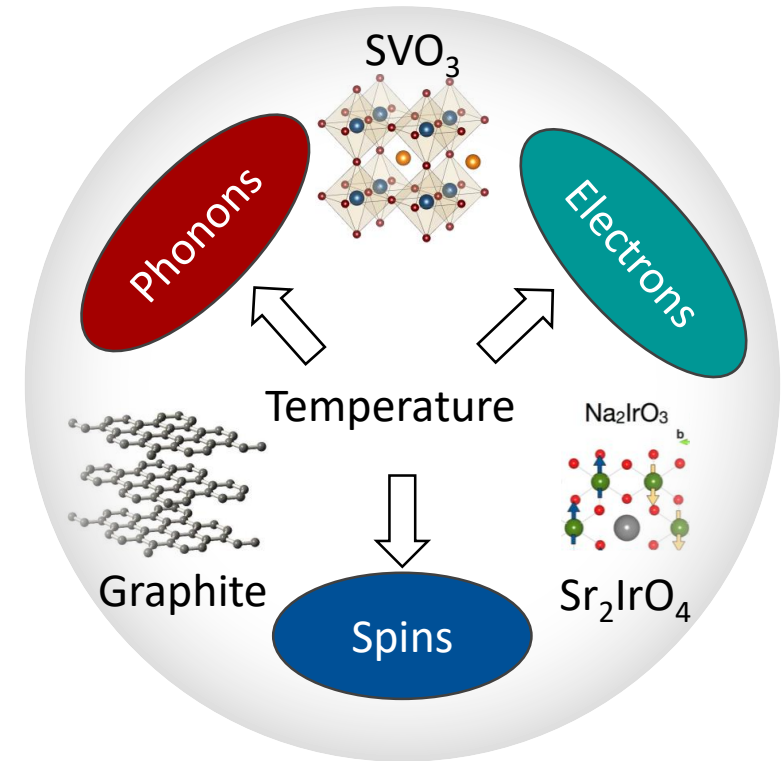
M Gandolfi^{1,2,3}, G L Celardo^{1,2,4}, F Borgonovi^{1,2,4}, G Ferrini^{1,2}, A Avella^{5,6,7}, F Banfi^{1,2} and C Giannetti^{8,1,2}

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Citation M Gandolfi *et al* 2017 *Phys. Scr.* **92** 034004



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