



# Monte Carlo Ray Tracing methods for the determination of the radiative properties of materials



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# Laboratoire de Thermique et Energie de Nantes

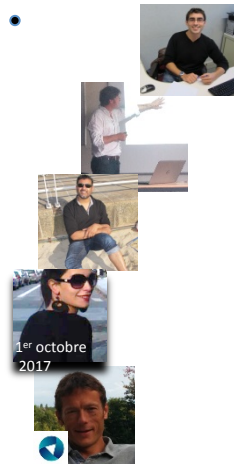
DU : Cathy Castelain

8 (+1) C CNRS, 17 EC UN, 4 EC ICAM, 5 IT CNRS- 4 BIATSS UN, 2 IE Cellule CAPACITES LTeN  
23 doctorants – 2 ATER/post-doctorants

## Transferts thermiques dans les matériaux et aux interfaces (S. Le Corre)

- Transferts aux interfaces et dans les micro-systèmes
- Transferts thermiques dans la mise en forme des polymères et composites

• Céfo<sup>P</sup>Ram



1<sup>er</sup> octobre 2017



Metti ACCORT

FédEsol  
FÉDÉRATION DE RECHERCHE  
SUR L'ÉNERGIE SOLAIRE



## Transferts dans les fluides et systèmes énergétiques (L. Luo)

- Transferts chaleur & masse dans les écoulements complexes
- Transferts chaleur & masse dans les fluides complexes
- Conception et optimisation des systèmes et procédés énergétiques

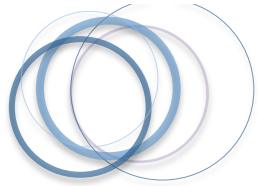


### Professeurs invités



Fév. 2018

Mai 2018



# Contrôle multi-échelle du transport de l'énergie

**Caractérisation** de la dépendance thermo-spectro-directionnelle des propriétés radiatives :  
spectroscopie IR/Vis

(réflexion, transmission, émission → 900 K)

D. Hakoume, AO, 2014, J. Mollicone, TSF, 2015  
V. Le Louet, IJHMT, 2017



**Modélisation** multi-échelle  
des propriétés radiatives :  
DFT, DM classique, Lorentz-Drude,  
Monte Carlo, Imagerie 3D

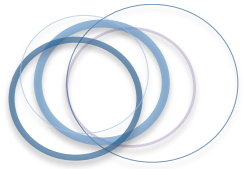
**nm → m**

B. Rousseau, AIP, 2016, B. Rousseau, AS, 2016  
S. Guévelou, IJHMT, 2016, S. Guévelou, JQSRT, 2017

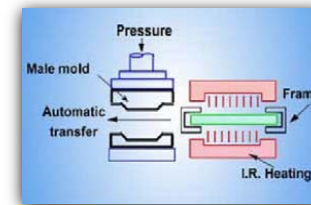


**Résolution numérique 3D** de  
l'Equation du Transfert Radiatif :  
estimation de propriétés (TO),  
optimisation énergétique

D. Le Hardy, JQSRT, 2016, D. Le Hardy, JCP, 2017  
D. Le Hardy, JQSRT, 2017



## Some thermal radiative issues...



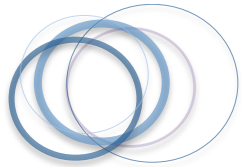
How to determine the temperature fields in a part or a component exposed to thermal radiation?



Need to achieve an energy balance between the energy provided by (the) source (s) heating (s) and the illuminated system



Resolving most often the Radiative Transfer Equation (**RTE**)  
in (fluids and solids) semi-transparent media



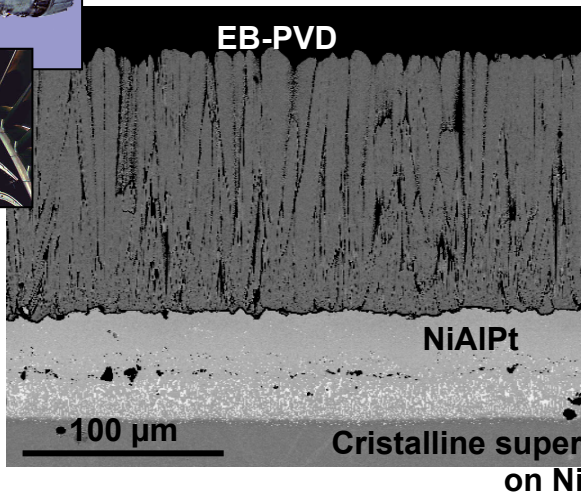
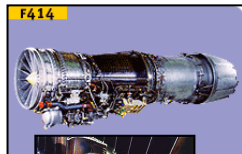
# Material characteristics



**Commercial glasses**



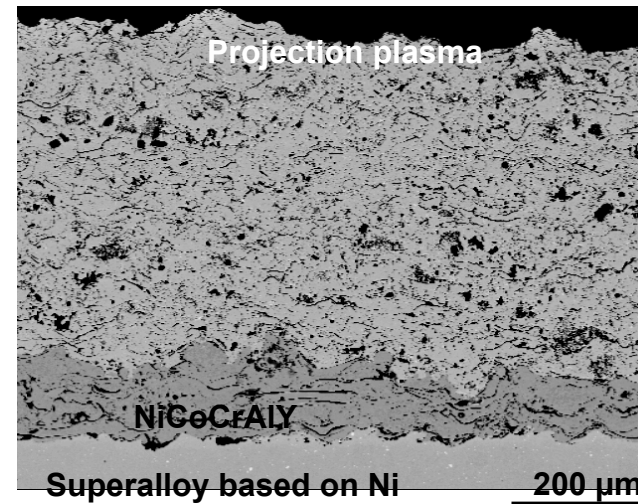
**Sapphire**



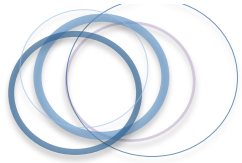
$ZrO_2 + 8\% \text{ (weight) } Y_2O_3$

Cristalline superalloy based on Ni

**Turbine blade**



**Combustion chamber**



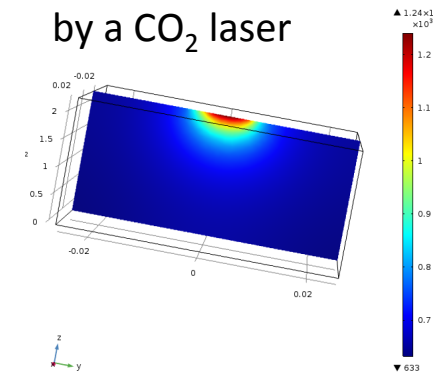
# How can we solve a thermal issue ?

$$\rho c_p \frac{\partial T}{\partial t}(s) = \nabla \cdot (k_{cond} \nabla T(s) - \dot{q}''(s))$$

conductive flux

radiative flux

SiC foam heated by a CO<sub>2</sub> laser



Tseng et al., High Temp.-High Pres., 2013, 42, pp. 387-403

$$\nabla \cdot \dot{q}''(s) = \int_0^{\infty} \kappa_{av} 4\pi I_{bv}(T) d\nu - \int_0^{\infty} \int_{4\pi} \kappa_{av} I_v(s, \hat{\Omega}) d\Omega d\nu$$

$$\frac{dI_v(s, \hat{\Omega})}{ds} = -(\kappa_{av} + \kappa_{dv}) I_v(s, \hat{\Omega}) + \kappa_{av} I_{bv}(T) + \frac{1}{4\pi} \int_{\Omega'=4\pi} \kappa_{dv} P_v(\hat{\Omega}' \rightarrow \hat{\Omega}) I_v(s, \hat{\Omega}') d\Omega'$$



## Boundary conditions for RTE solving

$$I_{\downarrow\nu}(s_{\downarrow p}, \Omega) = e_{\downarrow\nu} I_{\downarrow b\nu}(T(s_{\downarrow p})) + \int_{\Omega^{\uparrow}} \cdot n < 0 \uparrow \rho_{\downarrow\nu} \uparrow' (s_{\downarrow p}, \Omega^{\uparrow}, \Omega) \\ I_{\downarrow\nu}(s_{\downarrow p}, \Omega^{\uparrow}) / \Omega^{\uparrow} \cdot n \uparrow d\Omega^{\uparrow}$$

$$e_{\downarrow\nu} \equiv e_{\downarrow\nu}(\Omega, T(s_{\downarrow p})) = I_{\downarrow\nu}(\Omega, T(s_{\downarrow p})) / I_{\downarrow b\nu}(T(s_{\downarrow p}))$$

$$\rho_{\downarrow\nu} \uparrow' (s_{\downarrow p}, \Omega^{\uparrow}, \Omega) = I_{\downarrow\nu} \uparrow R (s_{\downarrow p}, \Omega) / I_{\downarrow\nu}(s_{\downarrow p}, \Omega) \Omega^{\uparrow} \cdot n \uparrow d\Omega^{\uparrow}$$

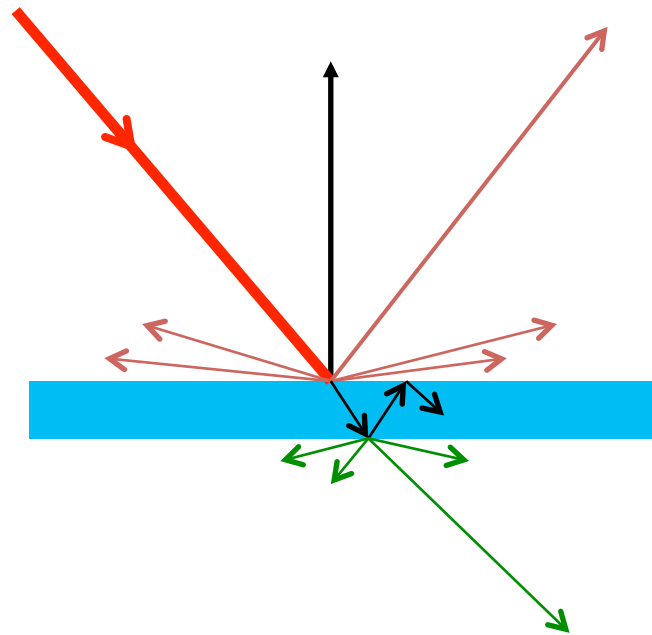
$$\rho_{\downarrow\nu} \uparrow S (s_{\downarrow p}, \Omega)$$

$$\rho_{\downarrow\nu} \uparrow D (s_{\downarrow p}, \Omega^{\uparrow})$$

$$\rho_{\downarrow\nu} \uparrow D (s_{\downarrow p}, \Omega^{\uparrow}) = \int 2\pi \uparrow \rho_{\downarrow\nu} \uparrow' (s_{\downarrow p}, \Omega^{\uparrow}, \Omega) \Omega \cdot n \uparrow d\Omega .$$



# Kirchhoff law and thermal balance on 1D slab



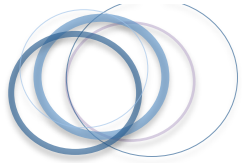
Heterogeneous material

$$e_{\downarrow\nu}(\Omega, T(s \downarrow p)) = 1 - \rho_{\downarrow\nu} \uparrow D(\Omega, T(s \downarrow p)) - t_{\downarrow\nu} \uparrow D(\Omega, T(s \downarrow p))$$

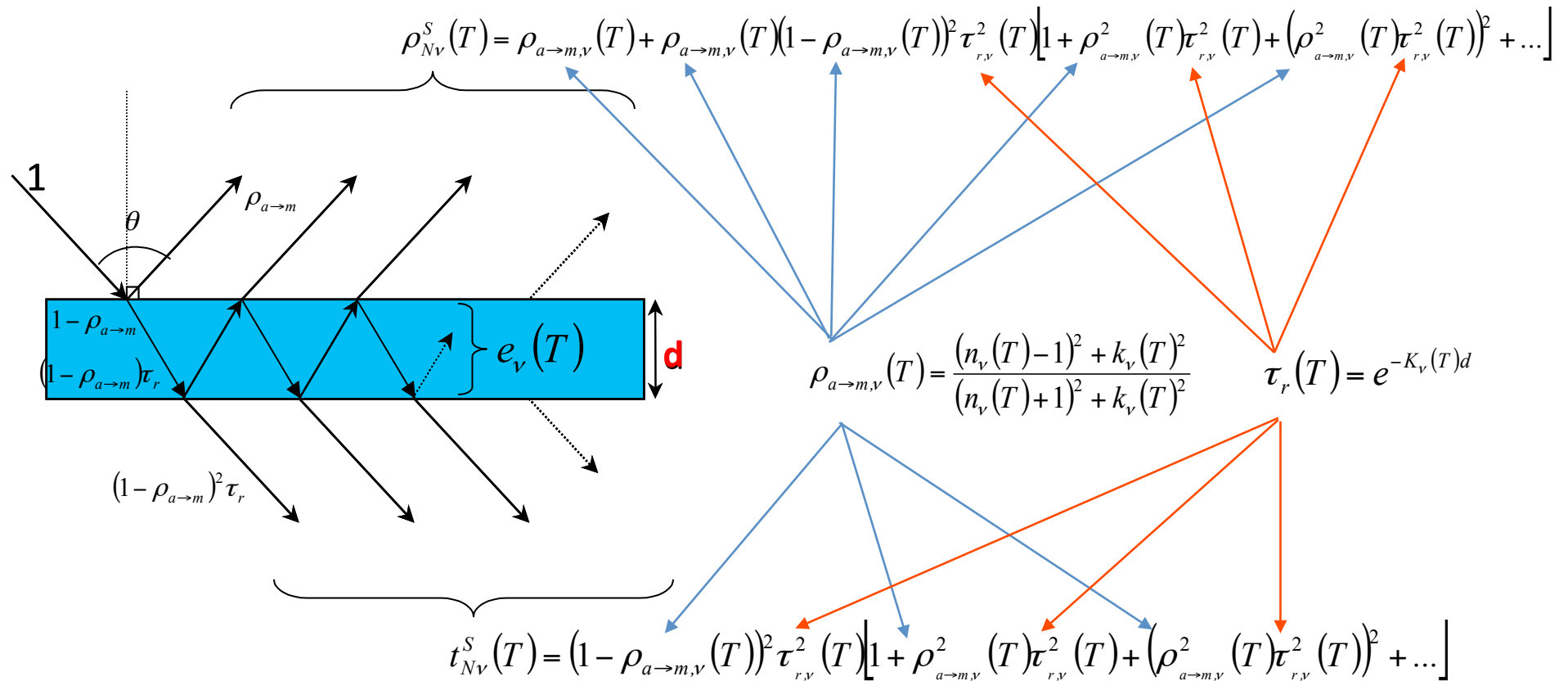
Homogeneous material

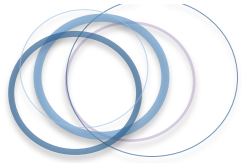
$$e_{\downarrow\nu}(\Omega, T(s \downarrow p)) = 1 - \rho_{\downarrow\nu} \uparrow S(\Omega, T(s \downarrow p)) - t_{\downarrow\nu} \uparrow S(\Omega, T(s \downarrow p))$$





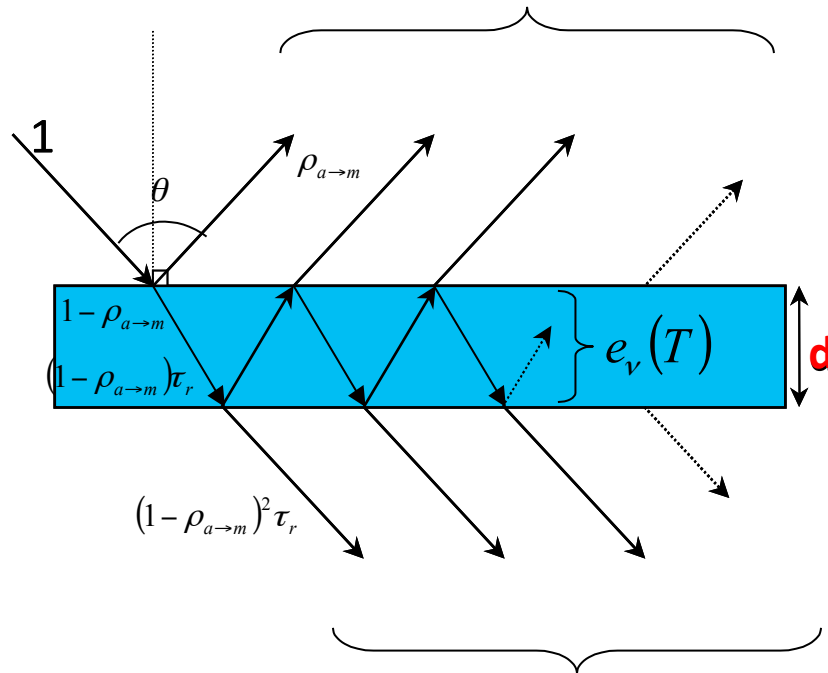
# Homogeneous 1D slab, optically polished with parallel faces





# Kirchhoff law and thermal balance on 1D slab

$$\rho_{N,v}^S(T) = \rho_{a \rightarrow m,v}(T) \left[ 1 + t_{Nv}^S(T) \tau_{r,v}(T) \right]$$



**Optical thickness**  $K_v(T)d$

$$K_v(T)d > 1$$

Optically thick media  
**opacity**

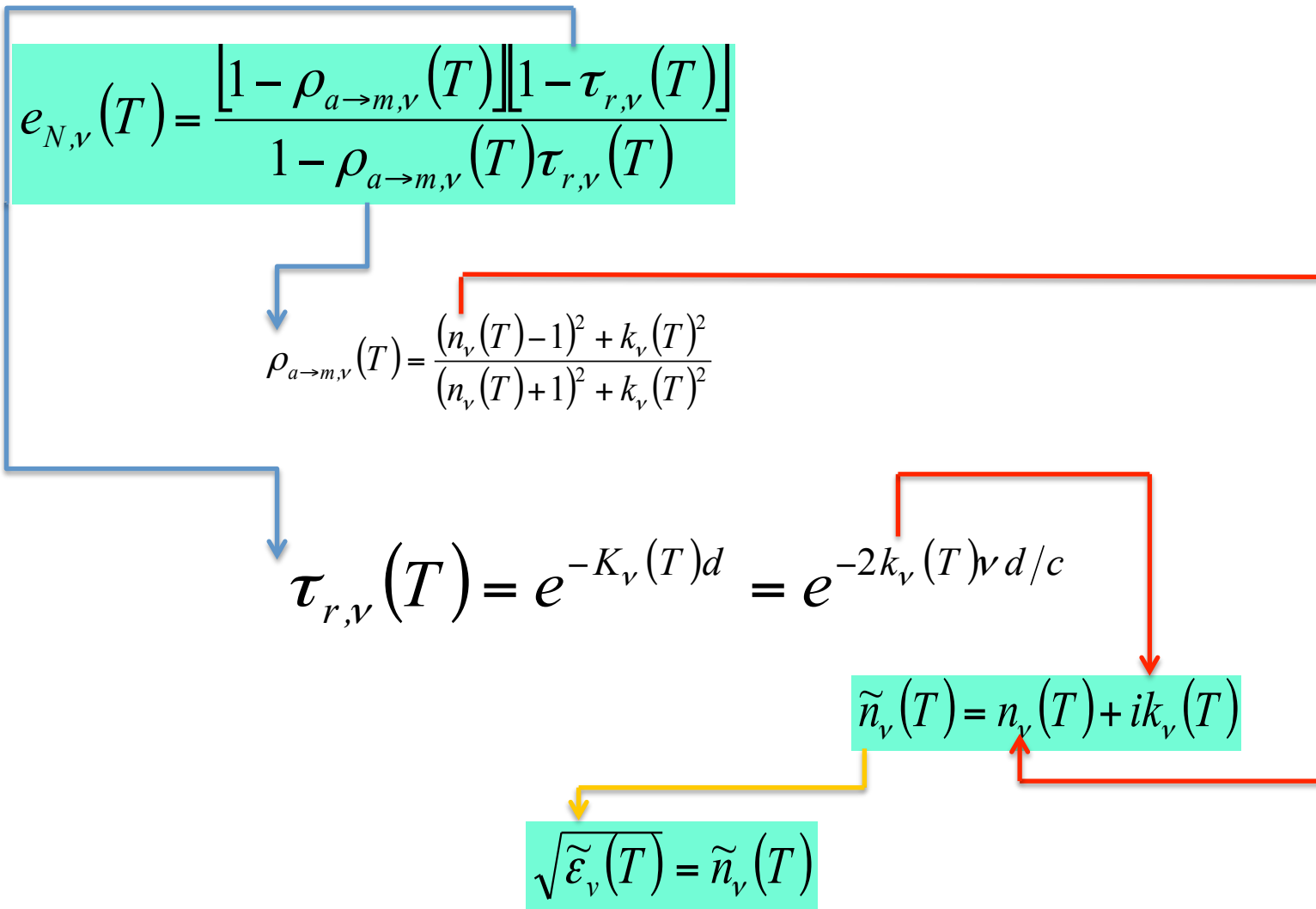
$$K_v(T)d < 1$$

Optically thin media  
**transparency**

$$t_{N,v}^S(T) = \frac{\left[ 1 - \rho_{a \rightarrow m,v}(T) \right]^2}{1 - \left( \rho_{a \rightarrow m,v}(T) \right)^2 \left( \tau_{r,v}(T) \right)^2} \tau_{r,v}(T)$$

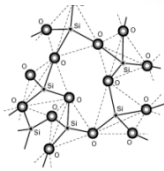


## Homogeneous 1D slab, optically polished with parallel faces





# Homogeneous 1D slab, optically polished with parallel faces



$$\tilde{n} = \sqrt{\tilde{\epsilon}}$$

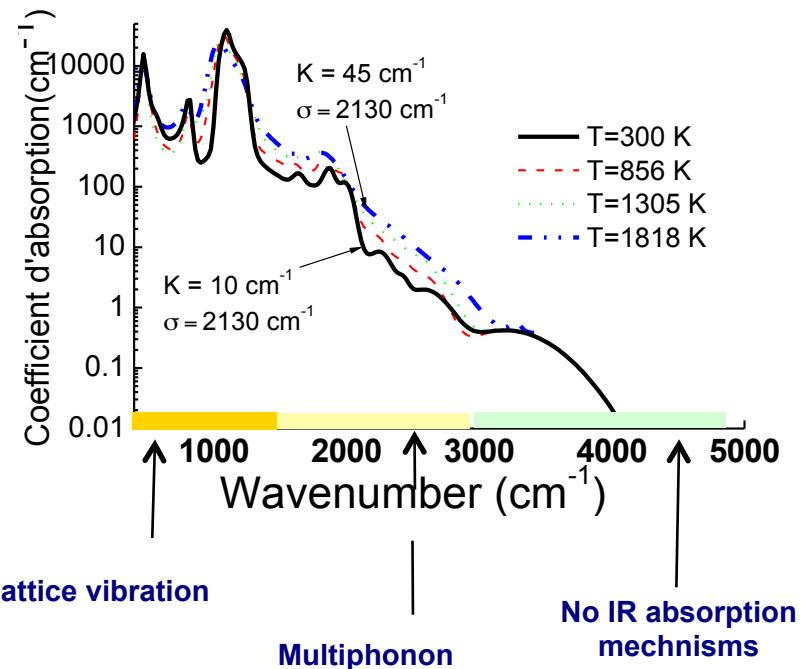
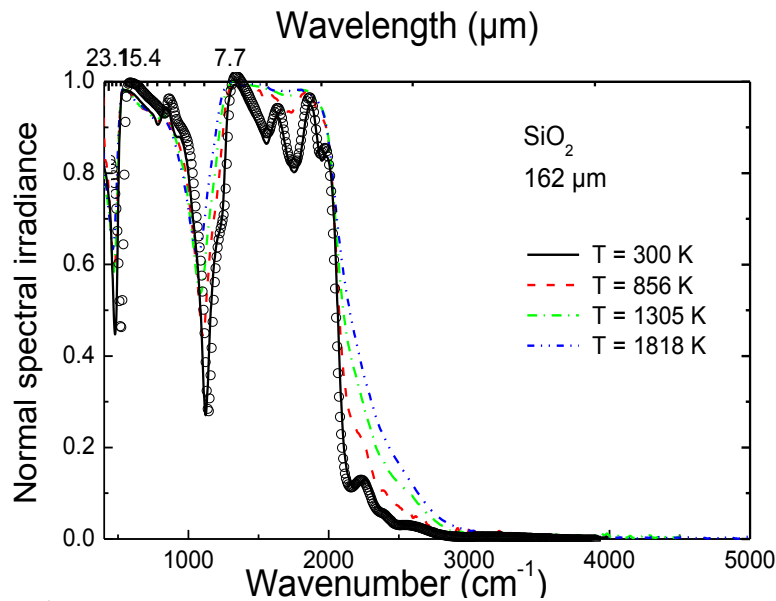
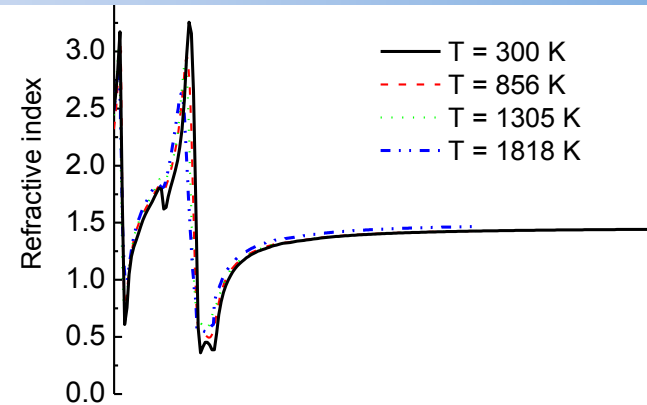
$$\tilde{n}(\nu, T) = n(\nu, T) + ik(\nu, T)$$

$$K(\nu, T) = 4\pi\nu k(\nu, T)$$

$$\tilde{\epsilon}(\nu, T) = \epsilon_{\infty} + \sum_j C_{V_j}(\nu; \nu_{0j}, \gamma_{Gj}, \gamma_{Lj})$$

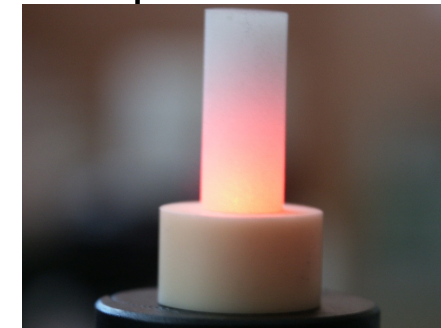
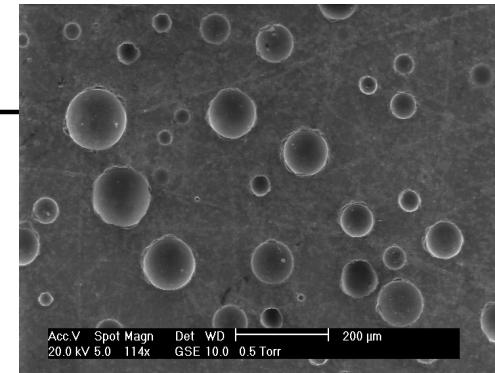
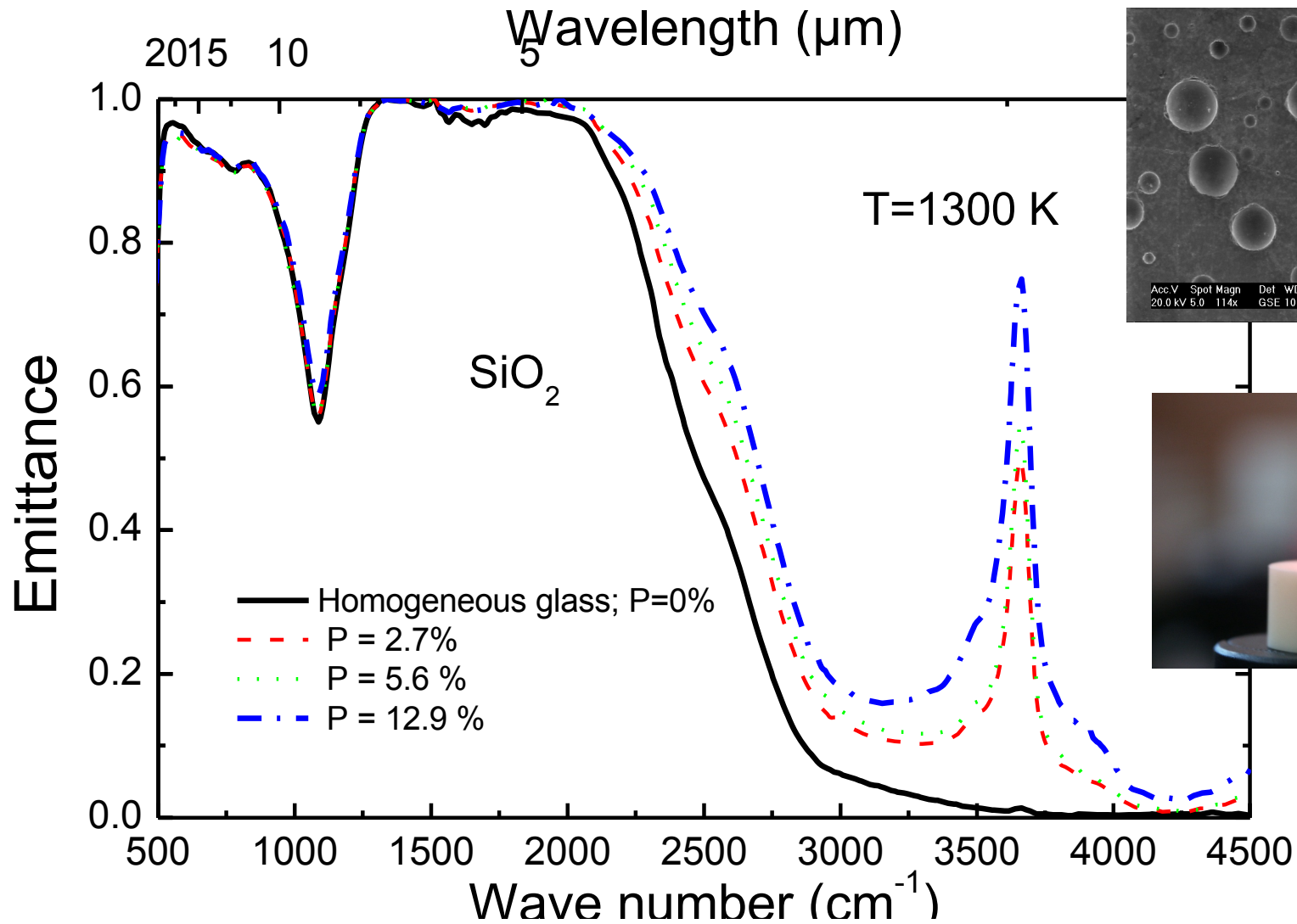
De Sousa Meneses et al., JNCS, 351, (2005)

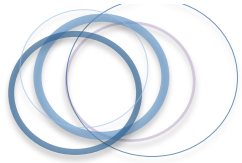
$$e(\nu, T) = \frac{(1 - \rho_{a \rightarrow m}(\nu, T))(1 - e^{-K(\nu, T)d})}{1 - \rho_{a \rightarrow m}(\nu, T)e^{-K(\nu, T)d}}$$



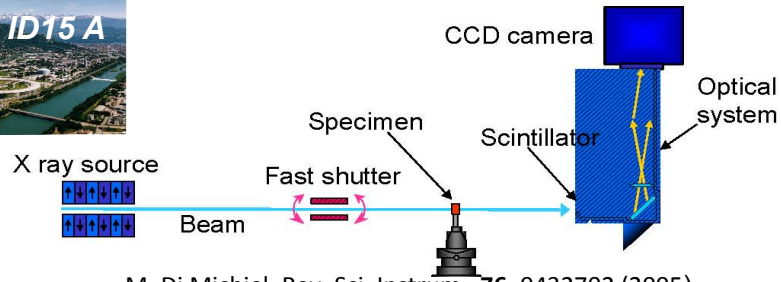


# Homogeneous 1D slab, optically polished with parallel faces





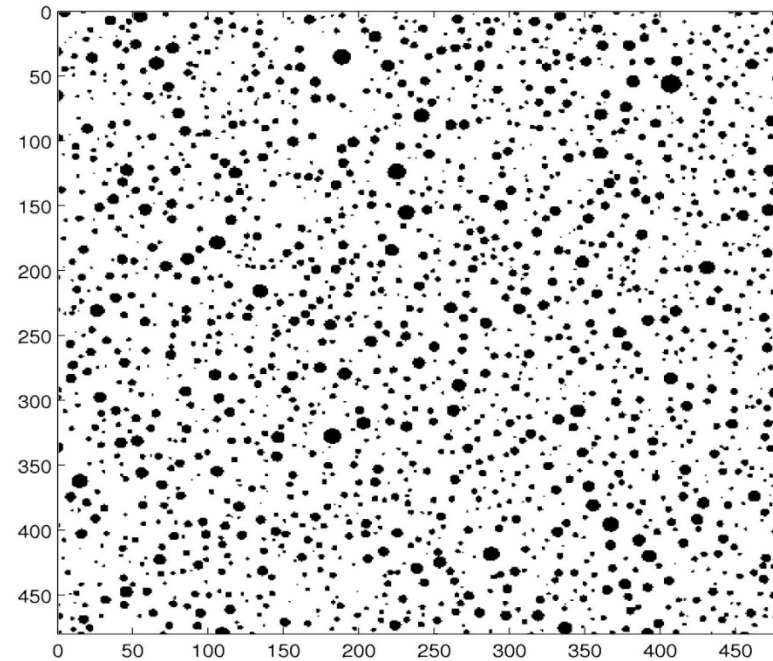
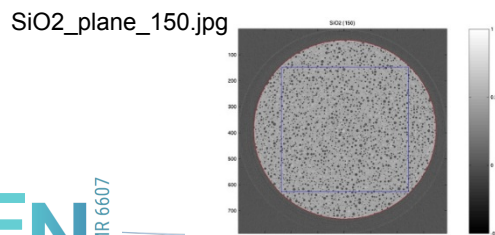
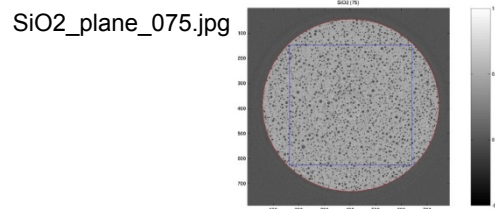
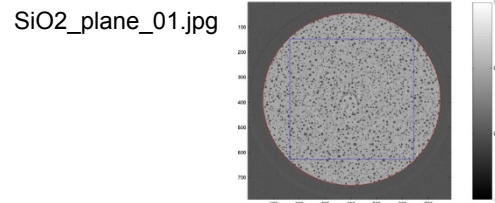
# A model case : silica glass with closed porosity



M. Di Michiel, Rev. Sci. Instrum. **76**, 0432702 (2005)

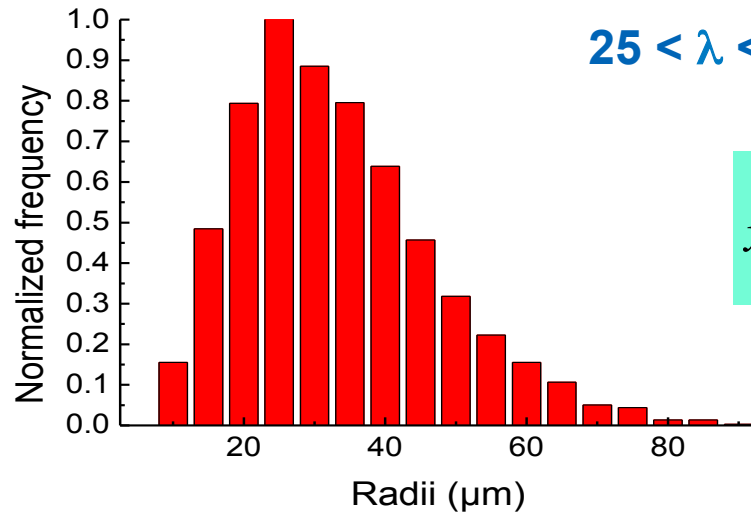
$$\frac{I}{I_0} = \exp[-(\mu/\rho)x]$$

$$\mu/\rho \approx (\sigma_{pe} + \sigma_{coh} + \sigma_{incoh} + \sigma_{pair} + \sigma_{trip} + \sigma_{ph.n})/uZ$$





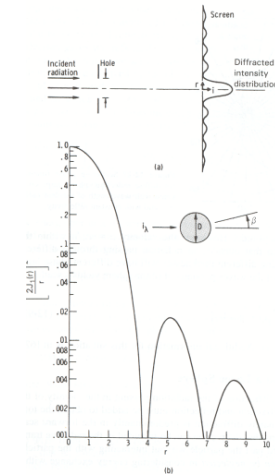
# Geometrical Optics Approximation



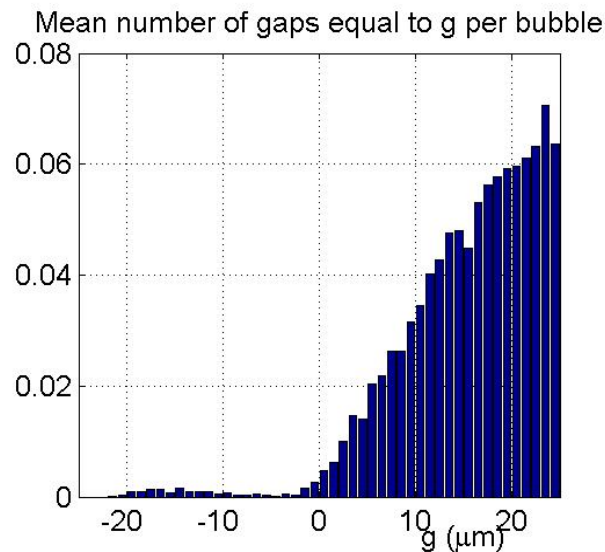
$$25 < \lambda < 2 \mu\text{m} \quad (400 < \sigma < 5000 \text{ cm}^{-1})$$

$$x = \frac{2\pi \langle r \rangle}{\lambda} > 1$$

- ❖ Geometrical optics
- ❖ No diffraction



Siegel & Howell, 1992



$$g/\lambda > 1/2$$

$$\langle r \rangle \approx g$$

- ❖ No interferences

- ❖ Multiple scattering

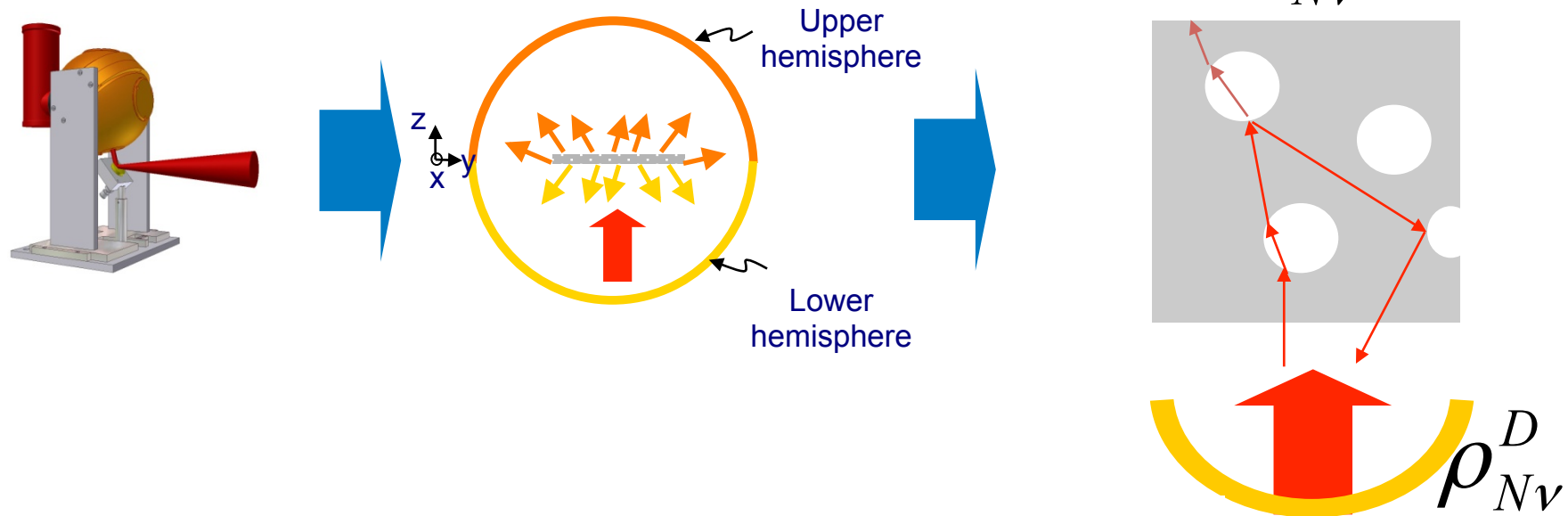


- ❖ Multiple reflection



# Radiative properties computation : MCRT

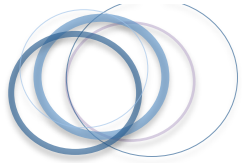
$$e_{\downarrow N\nu}(\Omega, T(s\downarrow p)) = 1 - \rho_{\downarrow N\nu}^D(\Omega, T(s\downarrow p)) - t_{\downarrow N\nu}^D(\Omega, T(s\downarrow p))$$



## Monte Carlo Ray Tracing code C++

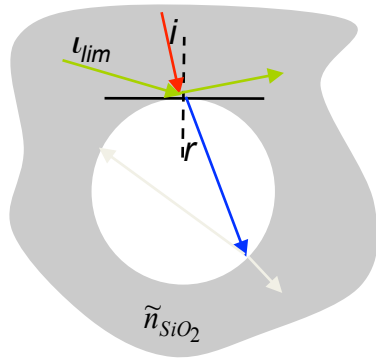
- Computing time:  $10^5$  rayons  $\rightarrow$   $\sim 40$  s/ wavelength ( standard deviation, 0.01)
- Mean free path scattering/absorption
- Scattering phase function
- Scattering geometry





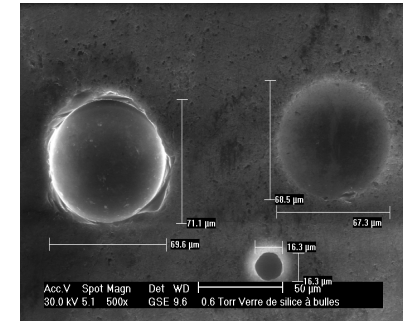
# Absorption/scattering behavior

❖ Refraction index gradient: **scattering**



➡ **MCRT process** ( $0 < \xi < 1$ )

$\xi < \rho$  : reflexion  
 $\xi > \rho$  : refraction



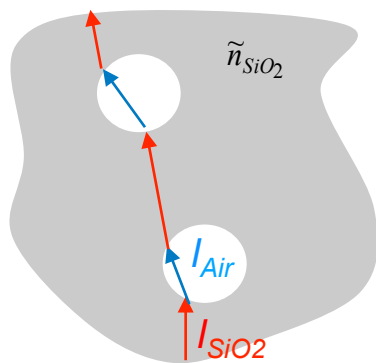
Fresnel law

$$\rho(v, T) = \frac{1}{2} \left[ \left| \frac{\cos i / \cos \tilde{r}(v, T) - \tilde{n}_1(v, T) / \tilde{n}_2(v, T)}{\cos i / \cos \tilde{r}(v, T) + \tilde{n}_1(v, T) / \tilde{n}_2(v, T)} \right|^2 + \left| \frac{\cos \tilde{r}(v, T) / \cos i - \tilde{n}_1(v, T) / \tilde{n}_2(v, T)}{\cos \tilde{r}(v, T) / \cos i + \tilde{n}_1(v, T) / \tilde{n}_2(v, T)} \right|^2 \right]$$

Snell-Descartes law

$$\tilde{n}_{SiO_2} \sin i = \sin \tilde{r}$$

❖ Optical path : **absorption**

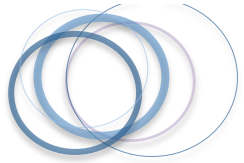


➡ **MCRT process**  $\sum_i I_i < 0.01$

Beer-Lambert law

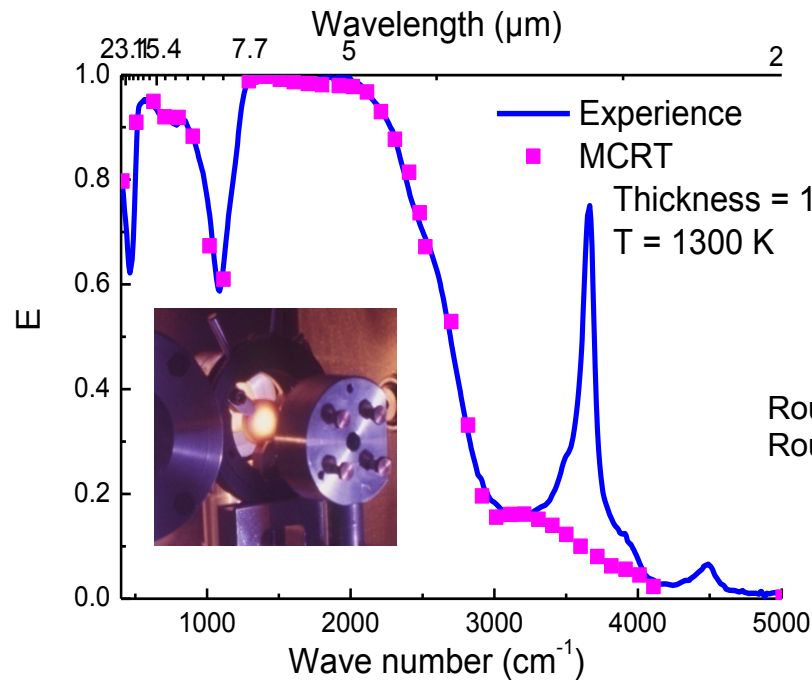
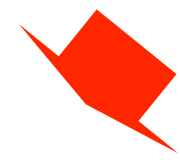
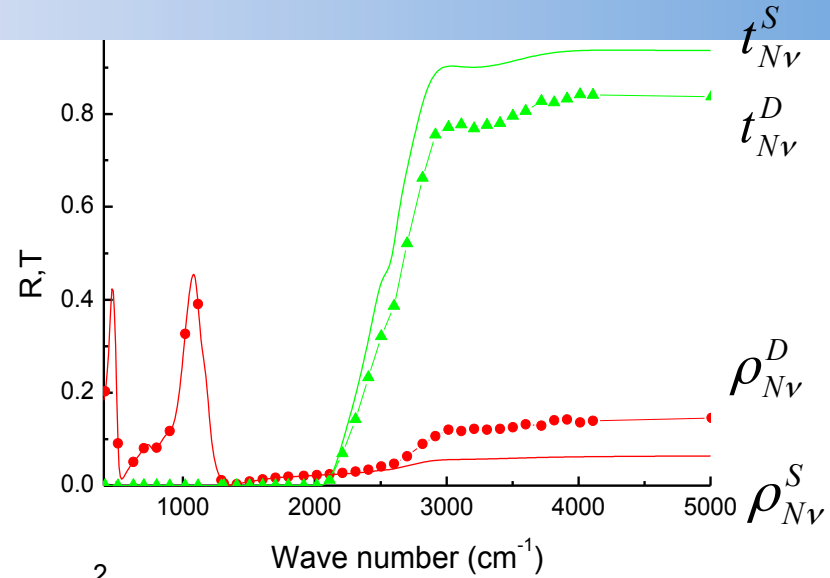
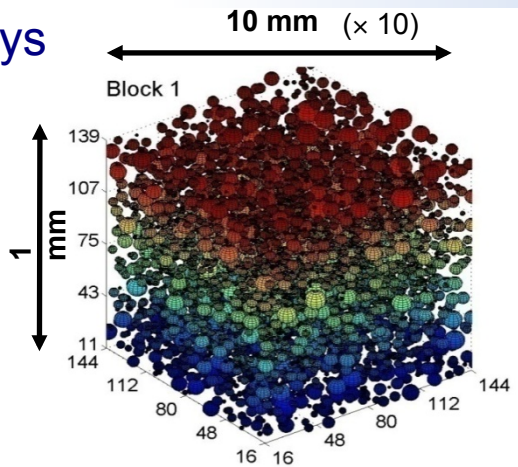
$$I_i = I_0 e^{-l_i K_i}$$

**Key roles:**  
**Optical function (n, k)**



# Validation : emittance computation

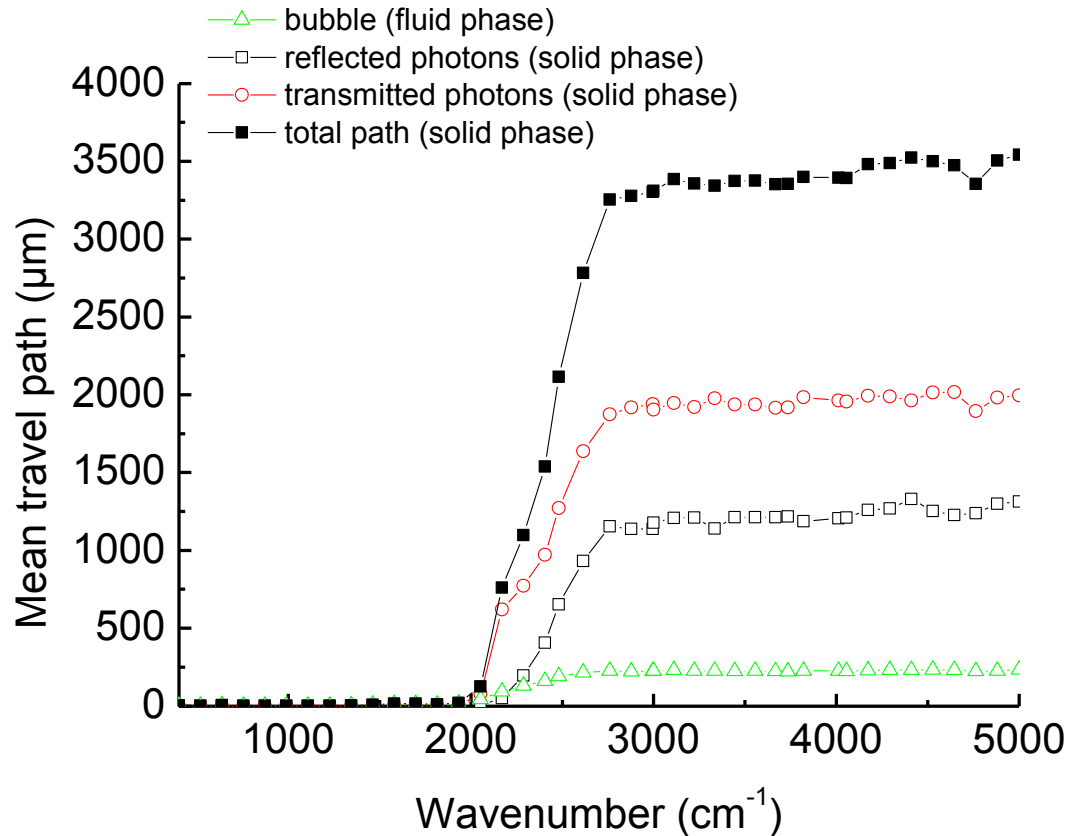
$10^5$  rays



Rousseau et al., AO, (2007)  
Rousseau et al., JQSRT (2006)



# Agreement between Mie Scattering Theory and MCRT?



Independent Scattering Theory + Mie Theory

$$\kappa_{dv} = \pi Q_{dv} \int_0^{\infty} f(r) r^2 dr \quad \Rightarrow \quad \frac{1}{\kappa_d} = 0.45 \text{ mm}$$

MCRT

$$\sum_i l_i = 3500 \mu\text{m}$$

$$n_{\text{interfaces}} = 8$$



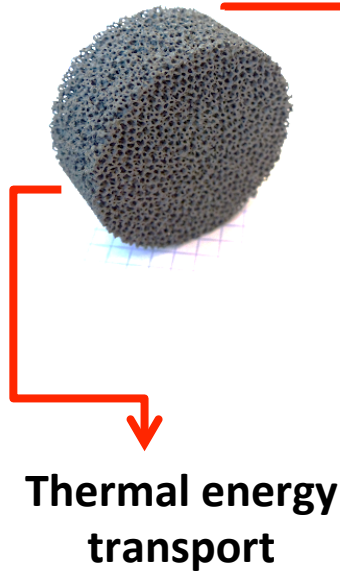
$$l_{MCRT} = 0.44 \text{ mm}$$

$$S_v = 3 p \frac{\int_0^{\infty} f(r) r^2 dr}{\int_0^{\infty} f(r) r^3 dr} = 8.9 \text{ mm}^{-1}$$

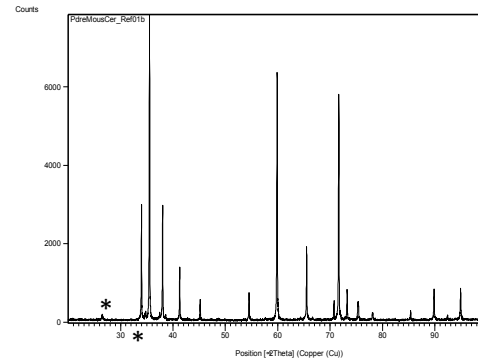
$$K_{dv} \approx \frac{4}{S_V}$$



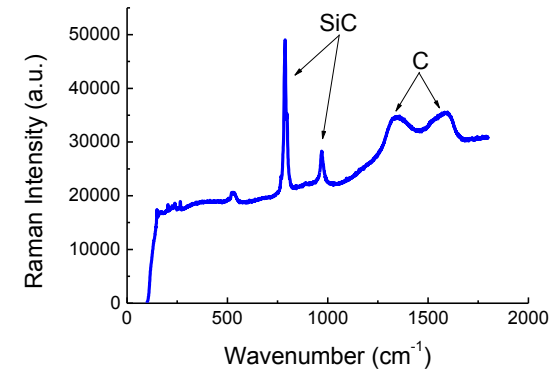
# Silicon carbide open-cell foams : how can we connect their TRP to their textural features ?



## ➤ Chemical composition → $\alpha$ -SiC

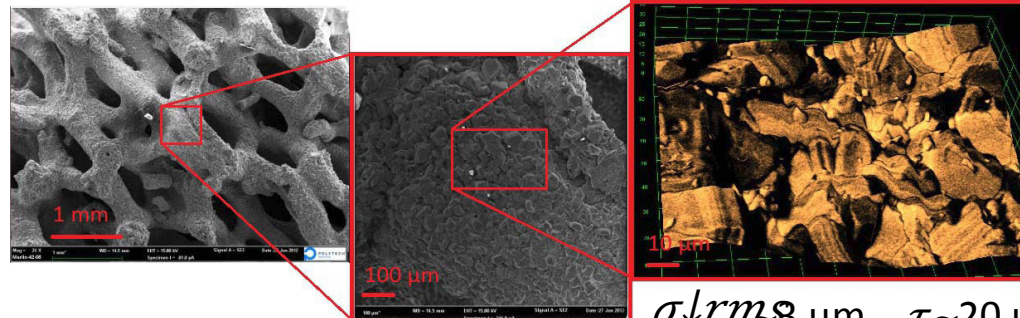


XRD (PROMES Odeillo, Eric Bèche)



Raman (IMN Nantes, France, J.-Y. Mevellec)

## ➤ 2D textural feature

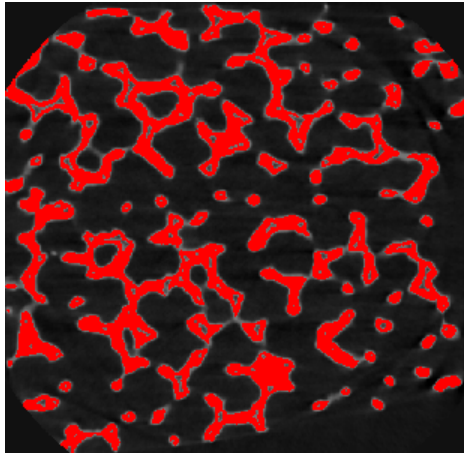
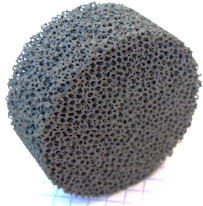


$\sigma \downarrow r_m \approx 3 \mu\text{m}$   $\tau \sim 20 \mu\text{m}$

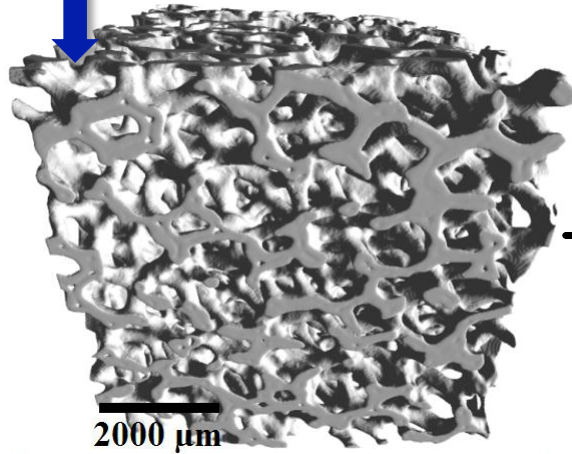


# Textural characterization

(iMorph software : <http://www.imorph.fr/>)

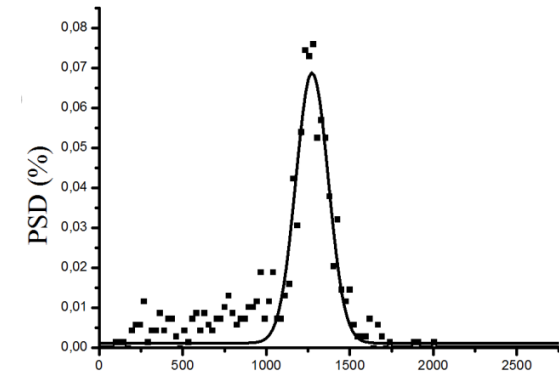
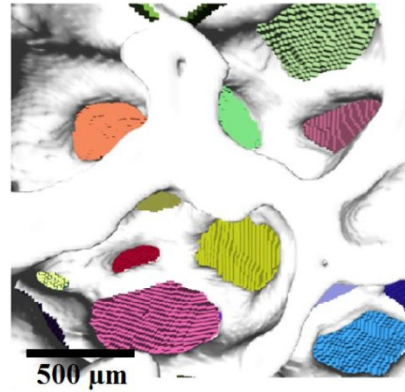


X-Ray  $\mu$ -tomography

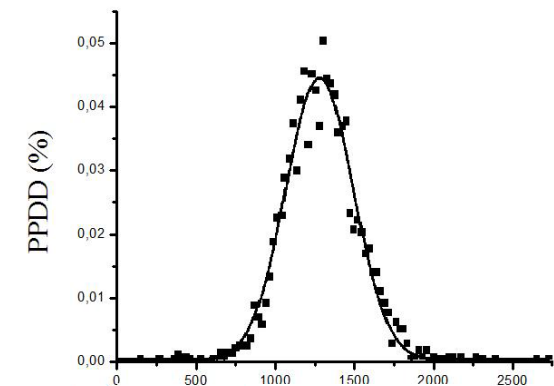
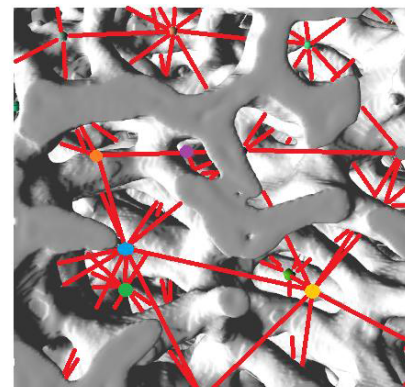


3D reconstruction .  
Spatial resolution : 24 $\mu$ m/voxel

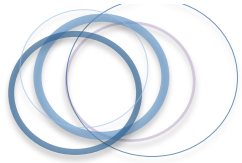
- Porosity= 70%
- Volumetric surface = 2800 m<sup>2</sup>/m<sup>3</sup>
- Pore size distribution



- Pore-pore distance distribution

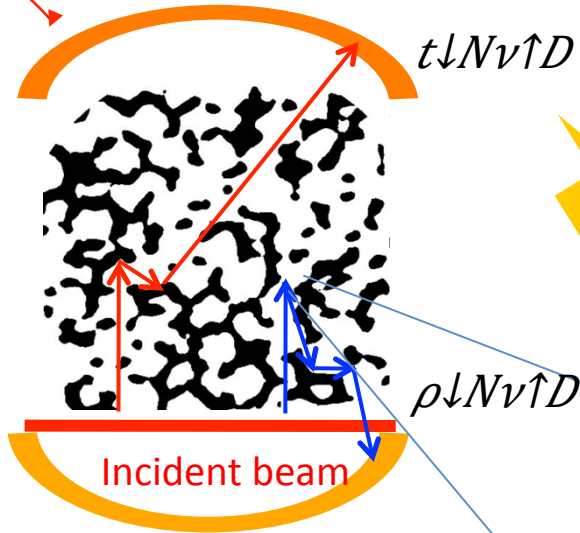
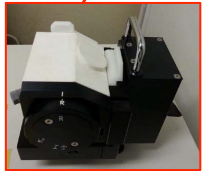


- Mean connectivity of 9,7



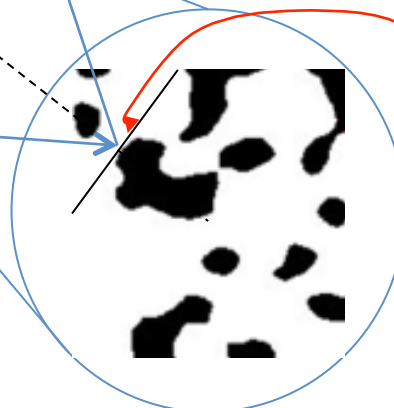
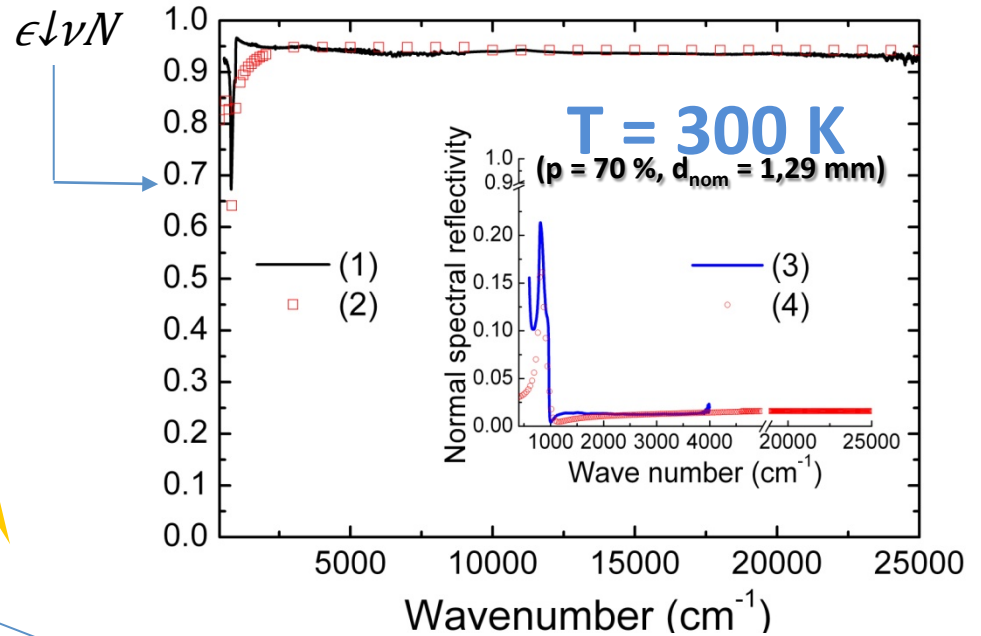
# genMat : a predictive tool for computing emittances from 3D images

Monte Carlo Ray-Tracing code : **iMorphRad (C++)**



**Macroscopic scale : ~10000 μm**

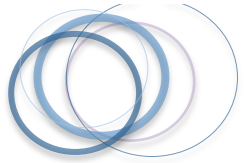
Rousseau et al., JCPS, 2012  
Guevelou et al., IHMT 2016



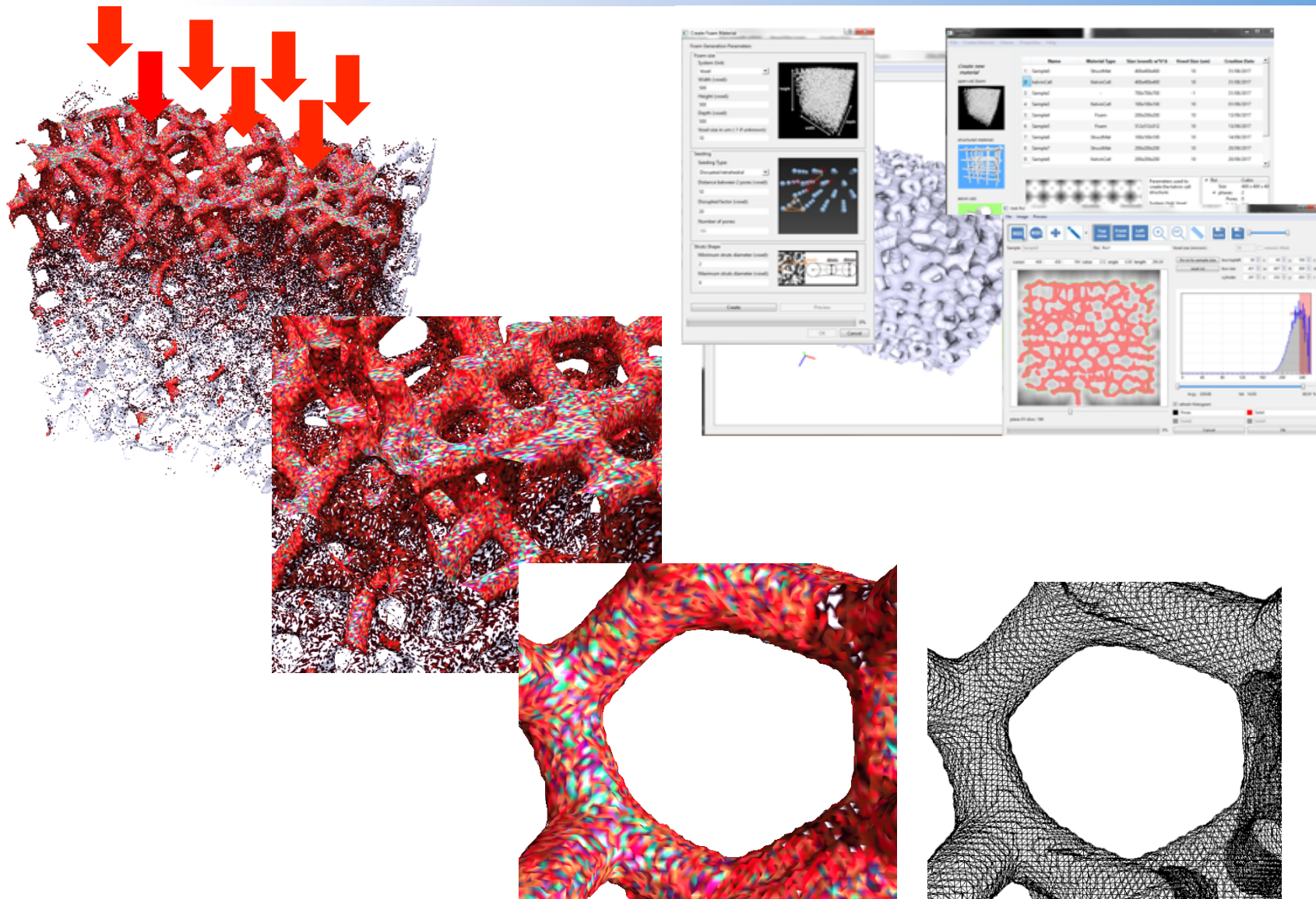
**Local scale : ~100 μm**



$$\rho_{n,\nu} = \left| \frac{\sqrt{\tilde{\epsilon}_{veff}} - 1}{\sqrt{\tilde{\epsilon}_{veff}} + 1} \right|^2$$

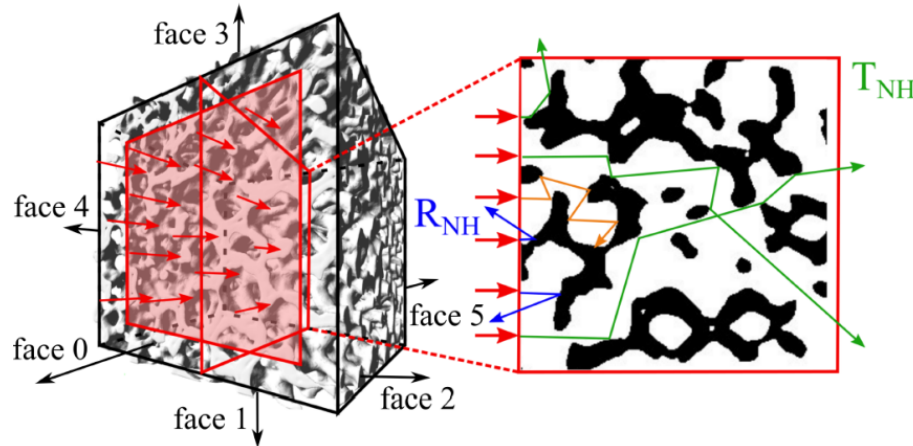


# genMat : a predictive tool for computing emittances from 3D images





# Integral formulation for MCRT?



$$q_{0,\lambda} = \int_{S_0} dS_0 \int_{2\pi} d\Omega(\vec{\omega}) I_{0,\lambda} \vec{n}_0 \cdot \vec{\omega} \delta(\vec{\omega} - \vec{\omega}_0) = I_{0,\lambda}$$

$$q_{i,\lambda} = \int_{S_0} p_{S_0} dS_0 [H(\vec{r}_1 \in S_f)R_1 + H(\vec{r}_1 \in S_i)W_0]$$

$$R_j = \int_{2\pi} p_{\Omega} d\Omega(\vec{\omega}_j) [H(\vec{r}_j \in S_f)R_{j+1} + H(\vec{r}_j \in S_i)W_j]$$

$$p_{S_0} = \frac{1}{S_0} \quad p_{\Omega} = \frac{\delta(\vec{\omega}_j - \vec{\omega}_{j-1})}{\vec{n}_j \cdot \vec{\omega}_j} \quad W_j = I_{0,\lambda} S_0 \prod_{k=1}^j \rho_F(\vec{r}_j, \vec{\omega}_j)$$

$$R_{NH} = q_{r,\lambda} / q_{0,\lambda} \quad T_{NH} = (q_{l,\lambda} + q_{t,\lambda}) / q_{0,\lambda}$$

International Journal of Heat and Mass Transfer 93 (2016) 118–129



Contents lists available at ScienceDirect

International Journal of Heat and Mass Transfer

journal homepage: [www.elsevier.com/locate/ijhmt](http://www.elsevier.com/locate/ijhmt)



Representative elementary volumes required to characterize the normal spectral emittance of silicon carbide foams used as volumetric solar absorbers



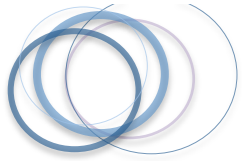
Simon Guévelou<sup>a</sup>, Benoit Rousseau<sup>a,\*</sup>, Gilberto Domingues<sup>a</sup>, Jérôme Vicente<sup>b</sup>, Cyril Caliot<sup>c</sup>

<sup>a</sup> CNRS, LTN, UMR 6607, Université de Nantes, Rue Christian Pauc, 44306 Nantes Cedex 3, France

<sup>b</sup> Aix-Marseille Université, CNRS, IUSTI UMR 7343, 13453 Marseille Cedex 13, France

<sup>c</sup> Processes, Materials and Solar Energy Laboratory, PROMES, UPR CNRS 8521, 66120 Font-Romeu-Odeillo-Via, France

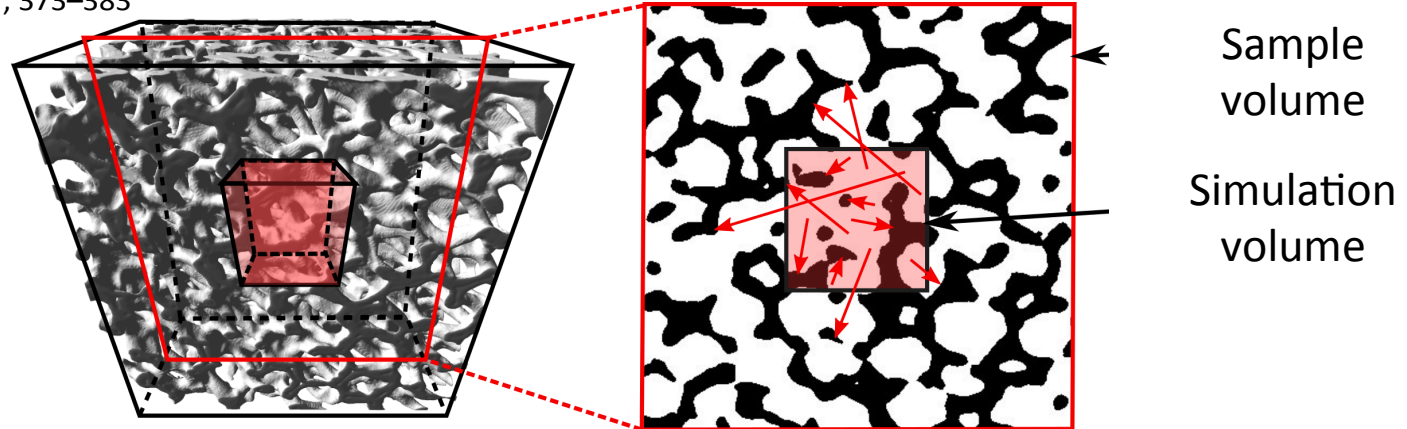




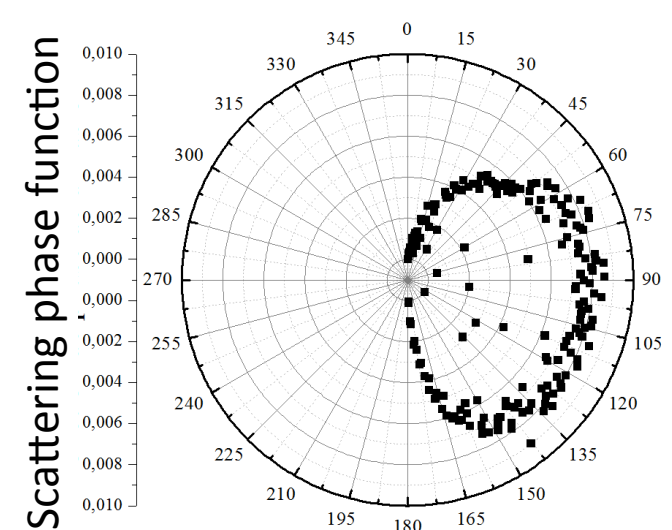
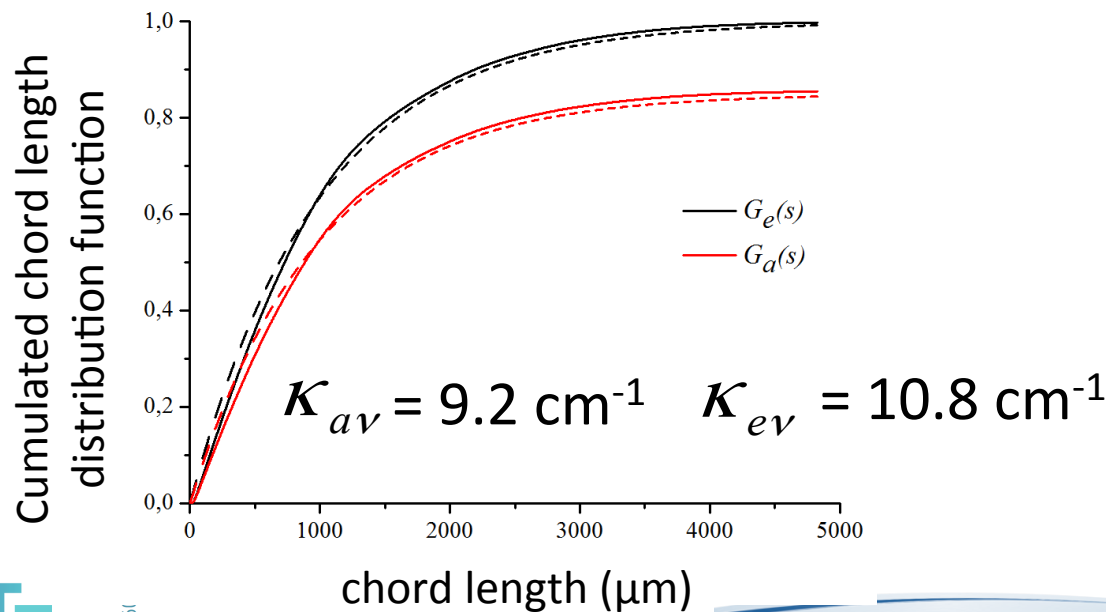
# iMorphRad : a predictive tool for computing TRP from 3D images

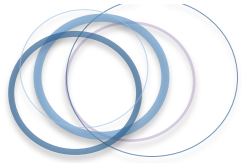
## RDFI method

Tancrez et al., IJHMT, 2004, 47, 373–383



Guévelou et al., JPM, 2015, 18, 1031-1045





# How can we go one step further now ?

TRP up to  $T = 1300$  K and not only at  $T = 300$  K !



Numerical foam generator : emissivity → texture (300 K)  $\cong$  texture (1300 K)

**iusti**  
UMR 7343



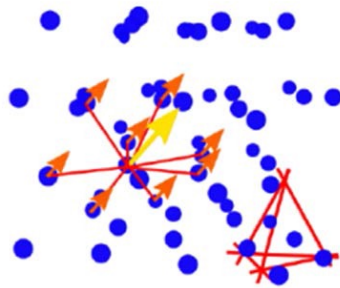
Infrared emission spectroscopy (SiC single crystals up to 1300 K)

**Cemhti**

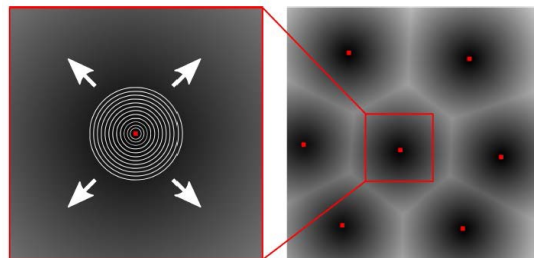


# Numerical foam generator (genMat, C++) $\rightarrow p, d_{nom}, \dots$

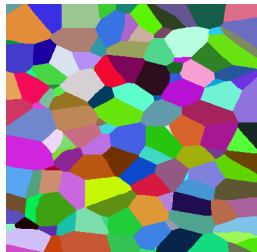
## Specific algorithm



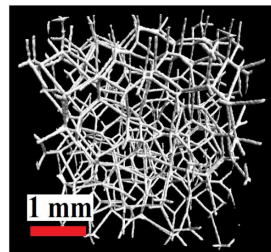
grain seed



fast-marching algorithm



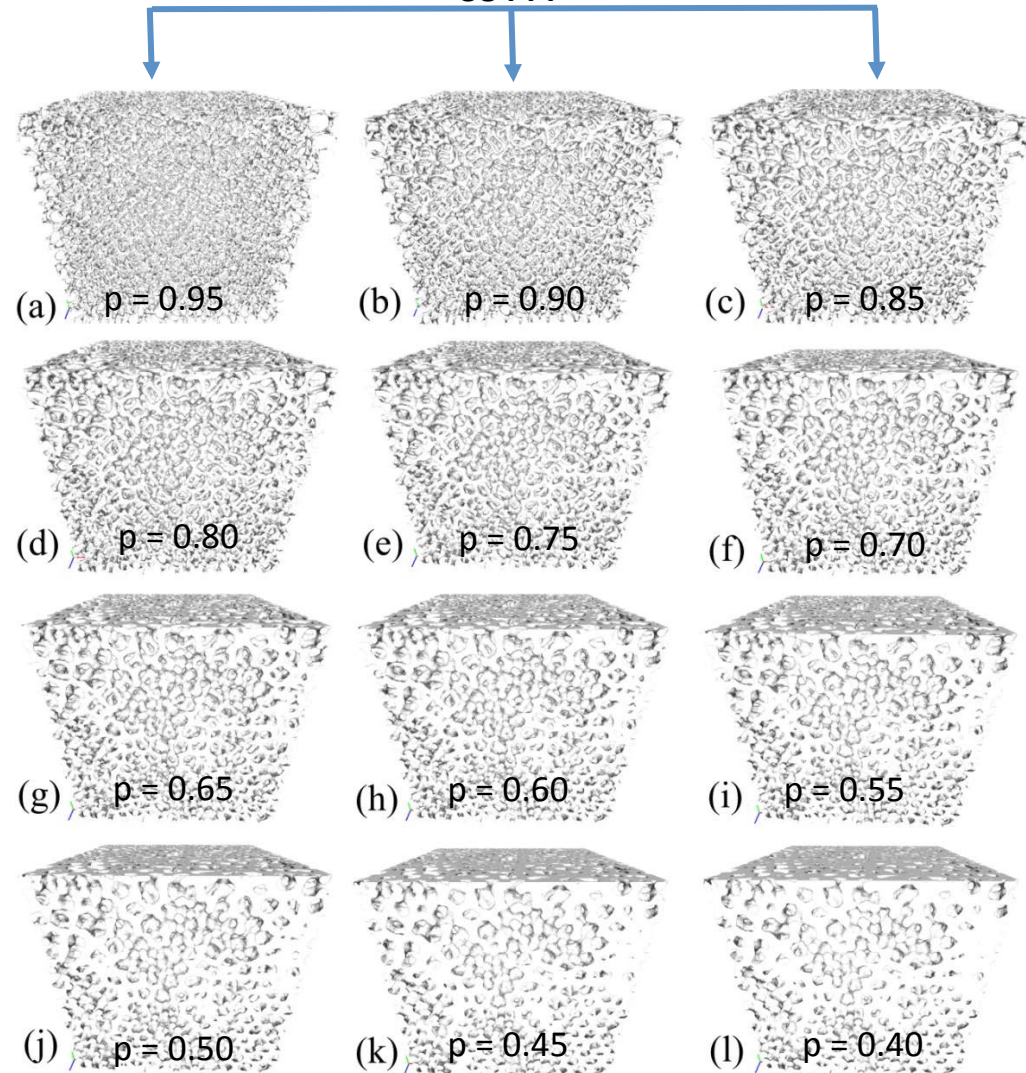
segmentation



squelettisation

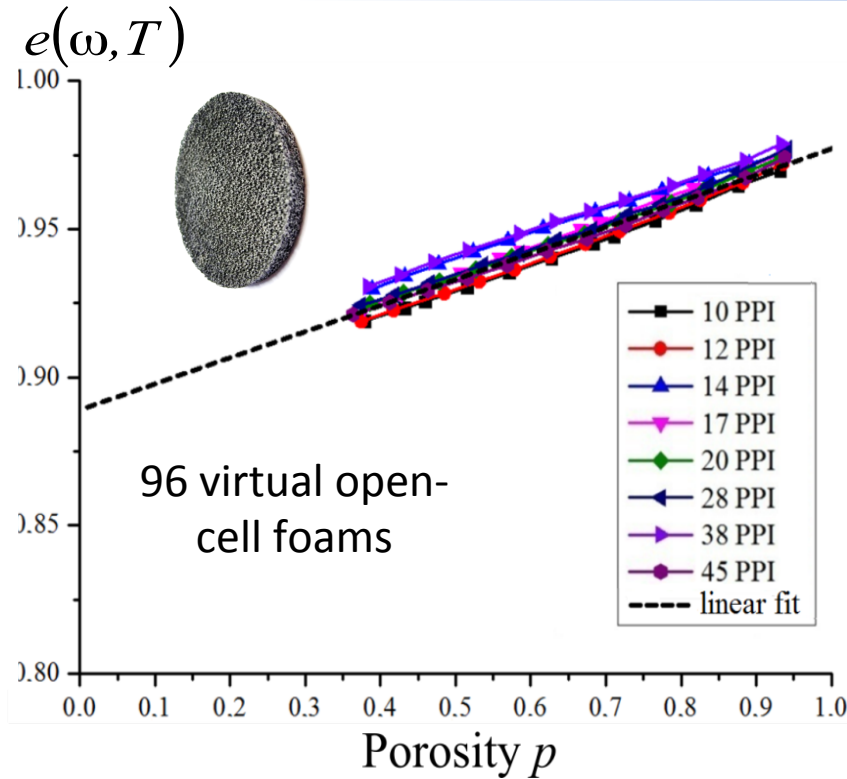
Guévelou et al., JPM 2015 ; Guévelou et al., IHTC, Kyoto 2015

38 PPI

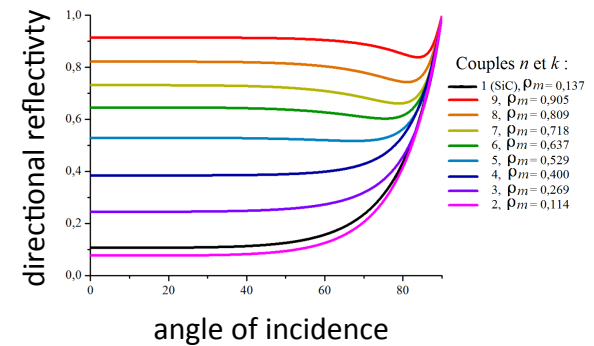
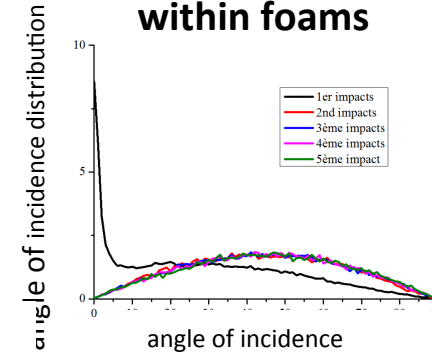




# Thorough statistical study of ray paths with iMorphRad for 600 virtual open cell foams



## Statistical study of ray transportation within foams



$V_{foam} > REV_{emissivity}$   
 Optically thick struts  
 optically smooth struts



$$e_{foam,\nu}(T) = 1 - \rho_{strut,\nu}(T)(1 - 0.8p)$$

Guévelou et al., JQSRT, 2017, 189, p. 329-338

$$\rho_{strut,\nu}(T) = \left| \frac{\sqrt{\tilde{\epsilon}_\nu(T)} - 1}{\sqrt{\tilde{\epsilon}_\nu(T)} + 1} \right|^2$$



# Extraction of the dielectric function with an improved Lorentz-Drude model for an heavily doped SiC

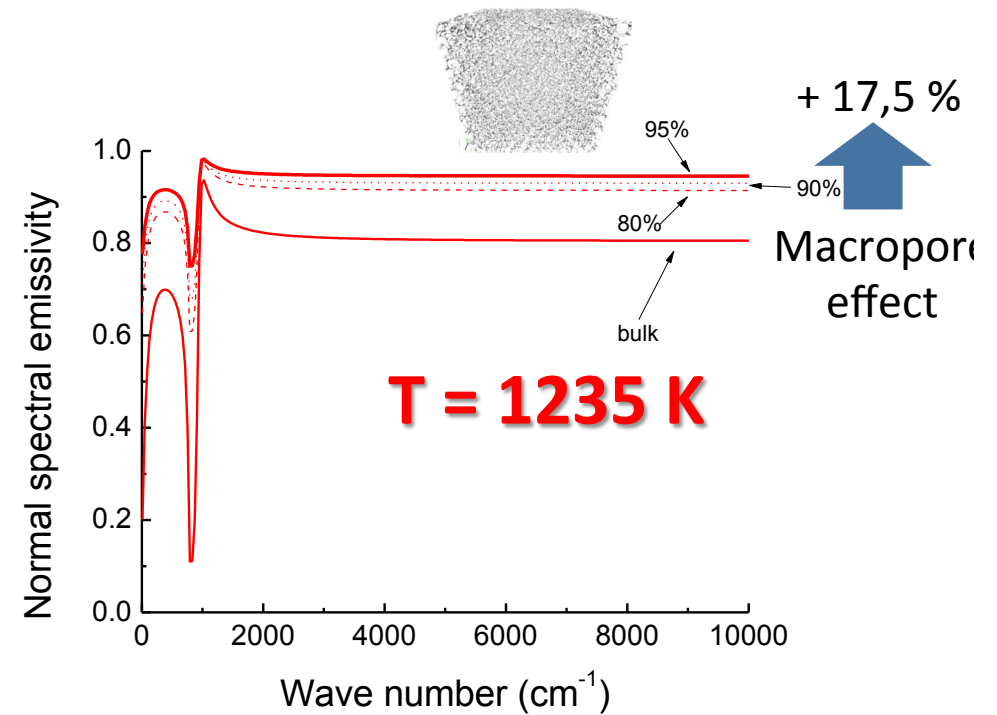
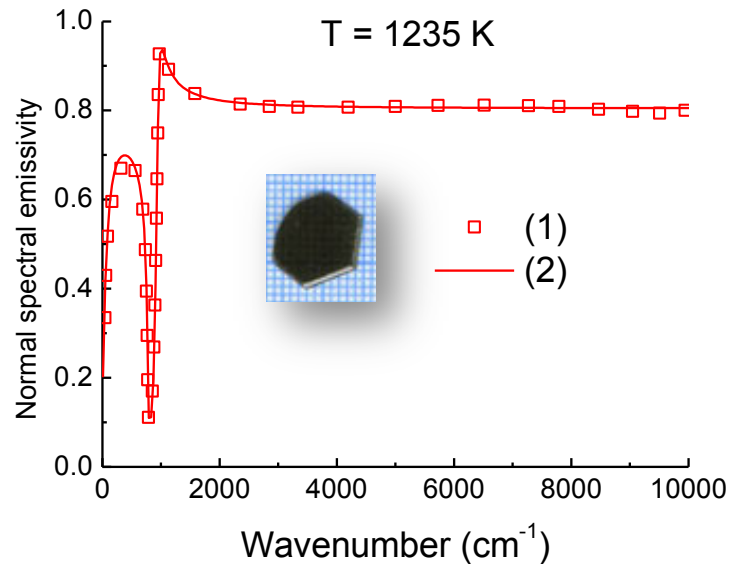
MICROSCALE

MACROSCALE

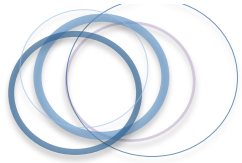
$$\tilde{\epsilon}_{crystal,\nu}(T) \xleftrightarrow[\text{method : LM}]{\text{minimization}} e_{crystal,\nu}(T)$$

$$e_{foam,\nu}(T) = 1 - (1 - e_{crystal,\nu}(T))(1 - 0.8p)$$

$$\tilde{\epsilon}_{crystal}(\nu, T) = \epsilon_{\infty} \left( 1 - \frac{\Omega_p^2(T)}{\nu^2 - i\gamma_p(T)\nu} \right) + \frac{\Delta\epsilon \nu^2(0, T)}{\nu^2(0, T) - \nu^2 - 2\nu(0, T)P(0, T; \nu)}$$

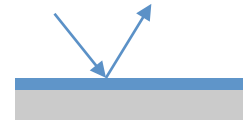
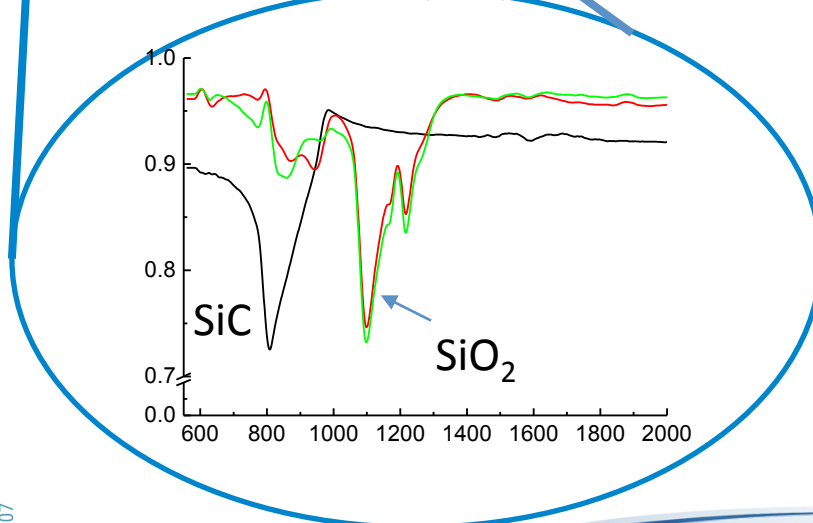
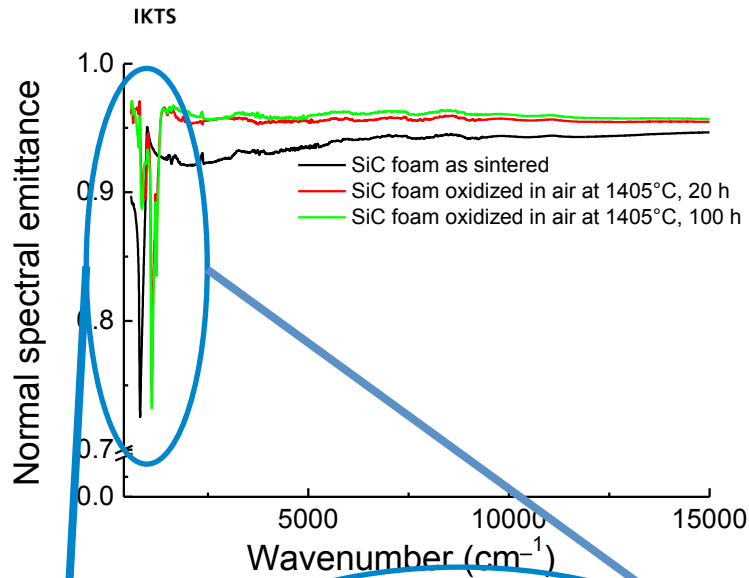


B. Rousseau et al., AIP Advances 2016 6 065226



# First oxidation at T = 1700 K, SiC foam p= 70 %

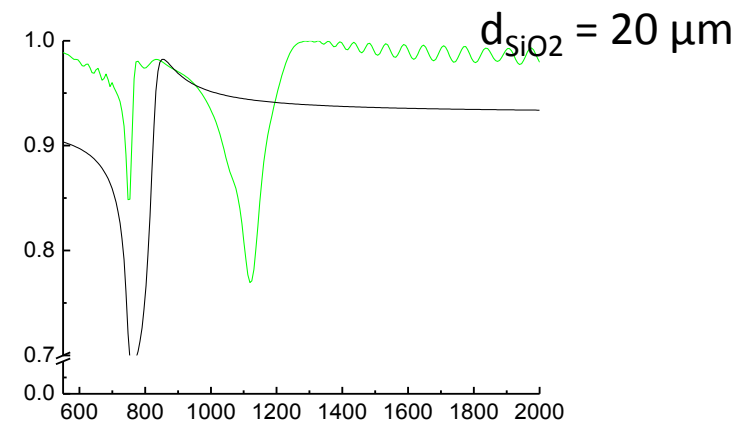
Fraunhofer



$$\rho_{film/strut}(\omega) = \left| \frac{r_{af}(\omega) + r_{fs}(\omega) e^{-i2\omega \tilde{\epsilon}_{SiO_2}(\omega) d/c}}{1 + r_{af}(\omega) r_{fs}(\omega) e^{-i2\omega \tilde{\epsilon}_{SiO_2}(\omega) d/c}} \right|^2$$

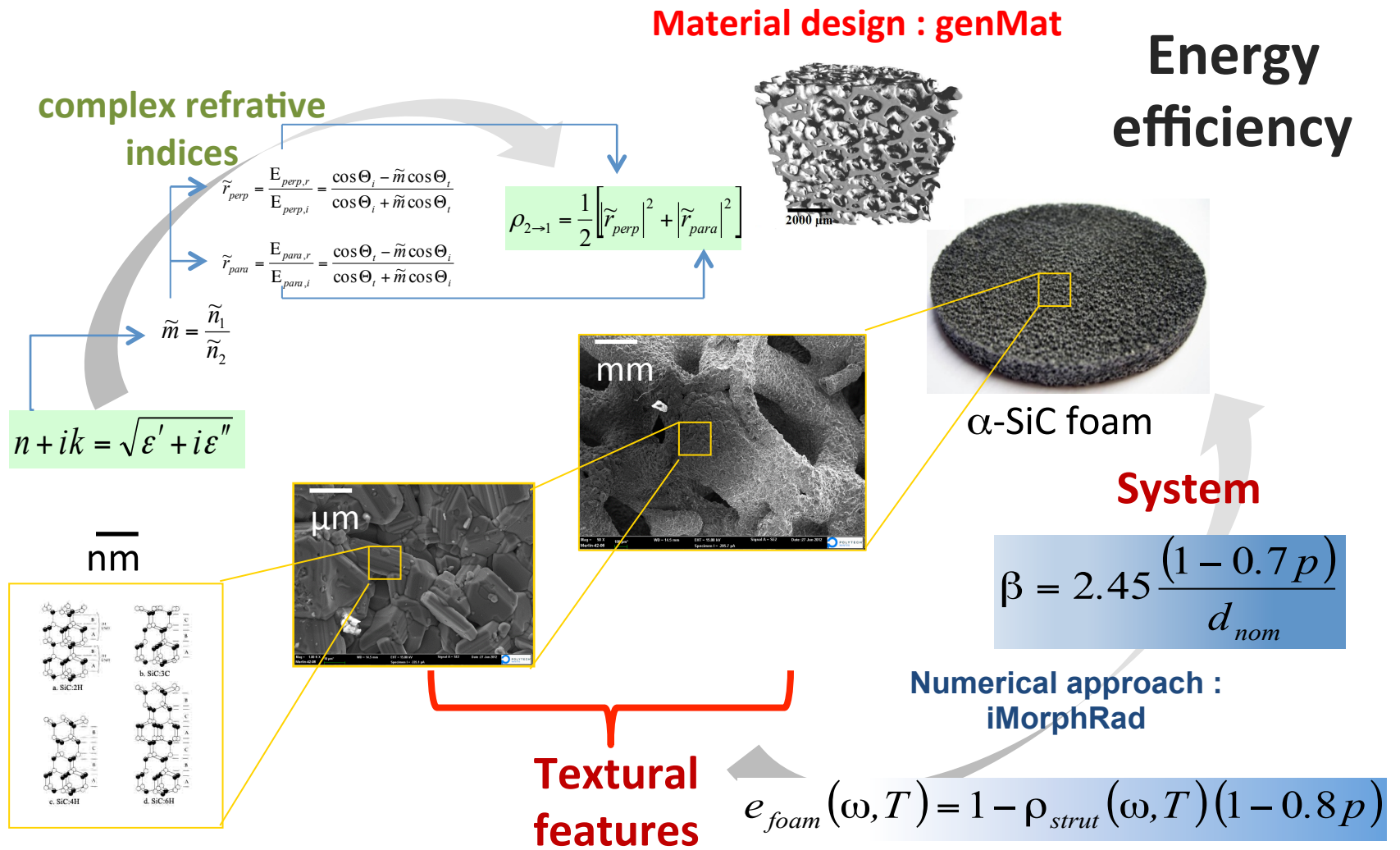
$$r_{af}(\omega) = \frac{1 - \sqrt{\tilde{\epsilon}_{SiO_2}(\omega)}}{1 + \sqrt{\tilde{\epsilon}_{SiO_2}(\omega)}} \quad r_{fs}(\omega) = \frac{\sqrt{\tilde{\epsilon}_{SiO_2}(\omega)} - \sqrt{\tilde{\epsilon}_{SiC}(\omega)}}{\sqrt{\tilde{\epsilon}_{SiO_2}(\omega)} + \sqrt{\tilde{\epsilon}_{SiC}(\omega)}}$$

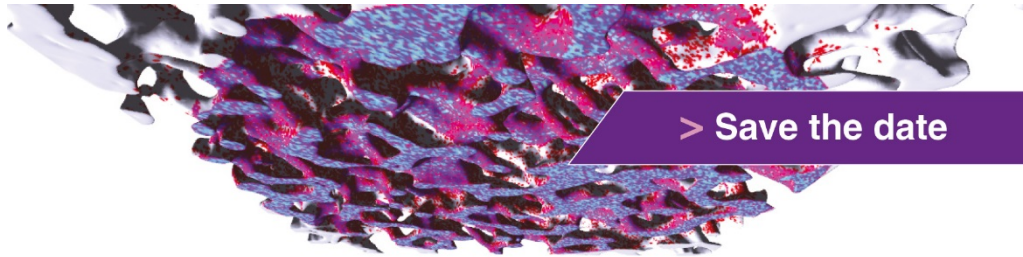
$$e_{film/foam}(\omega, T) = 1 - \rho_{film/strut}(\omega, T)(1 - 0.8p)$$





# Multi-length scale methods for computing the radiative properties of heterogeneous materials





> Save the date

# French Interpore Conference on Porous Media

8 -10 October 2018 - La Cité Nantes Event Center  
Nantes (France)

Biennial conference  
Understanding of the complex behavior of porous media

- > Registration opening and abstract submission : 15<sup>th</sup> January 2018
- > Deadline for abstract submission : 30<sup>th</sup> March 2018
- > Notification of acceptance : 13<sup>th</sup> April 2018
- > Standard registration deadline : 15<sup>th</sup> June 2018

Ideal place for scientific exchanges where fundamental and applied topics, often interdisciplinary, are discussed :

- > Energy storage
- > Pollution
- > Renewable energy
- > Petroleum engineering
- > Natural environment
- > Food and health

## > Scientific topics

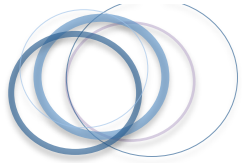
Mechanical and thermal behavior of porous media - Multi-physics coupling and numerical modelling - Fluid mechanics in Engineering processes - Porous media for energy production and storage - Imaging, numerical generation of porous media - Geotechnical and petroleum engineering - Reactive and dispersive transport - Multiscale fibrous media - Wave propagation



<https://jemp2018.sciencesconf.org/>

 [twitter.com/JEMP2018](https://twitter.com/JEMP2018)





# Acknowledgements



P. Echegut  
D. De Sousa Meneses  
H. Gomart, M. Niezgodá, J.-Y. Rolland, M. Tri Ta



J.-F. Thovert



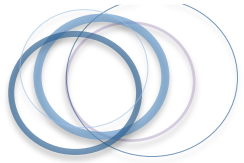
J. Vicente



C. Caliot, G. Flamant



Y. Favennec  
G. Domingues  
S. Le Corre, N. Boyard, D. Delaunay  
D. Hakoume, S. Guévelou, F. Dubot, D. Le Hardy, A. Mekeze-Monthe,  
Md Afeef Badri, V. Le Louet  
J.-Y. Rolland, V. Le Nader, J. Dausseins, A. Biallais



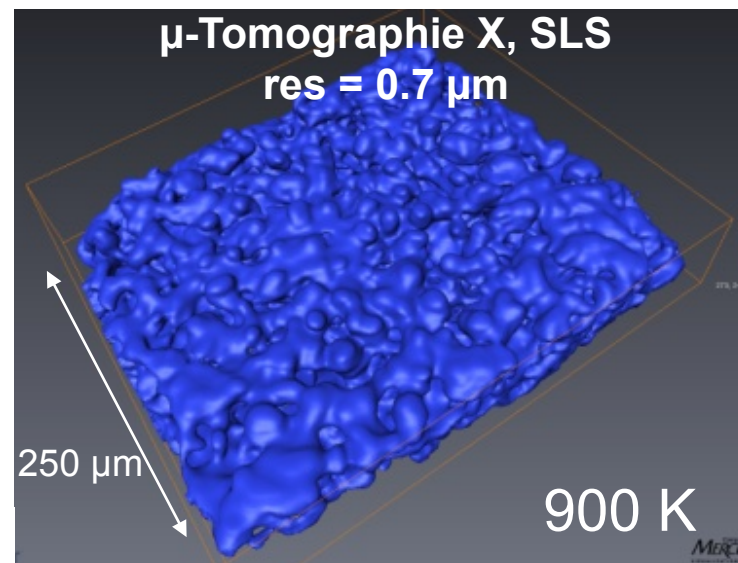
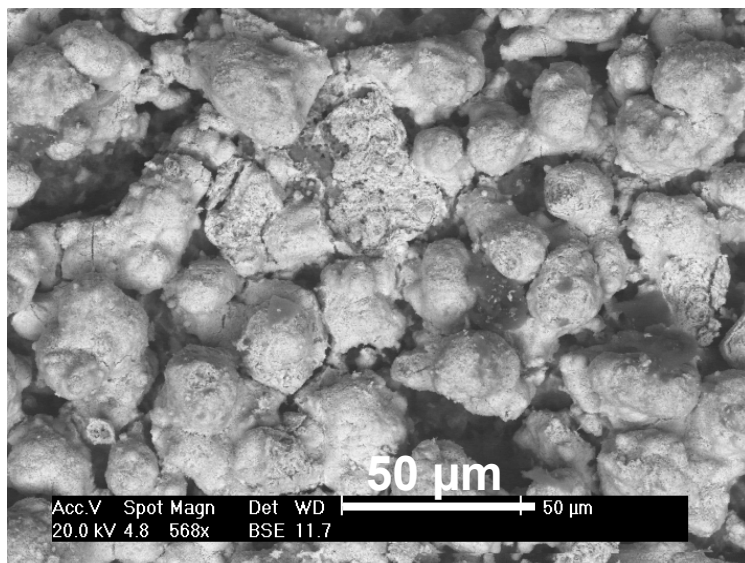
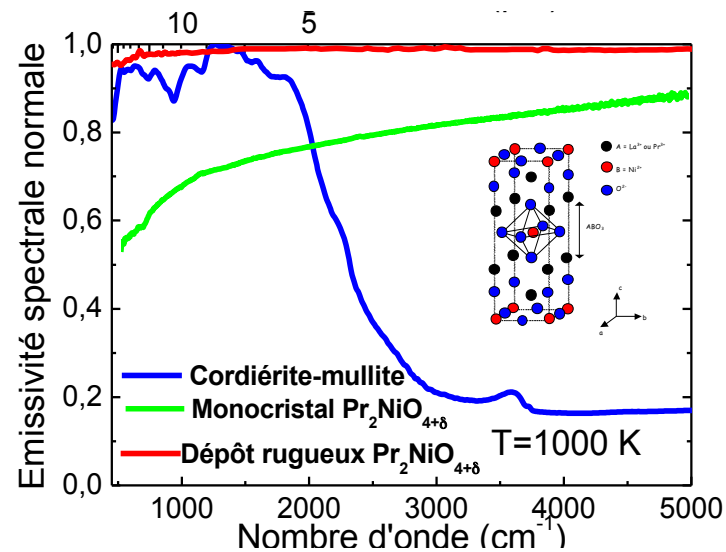
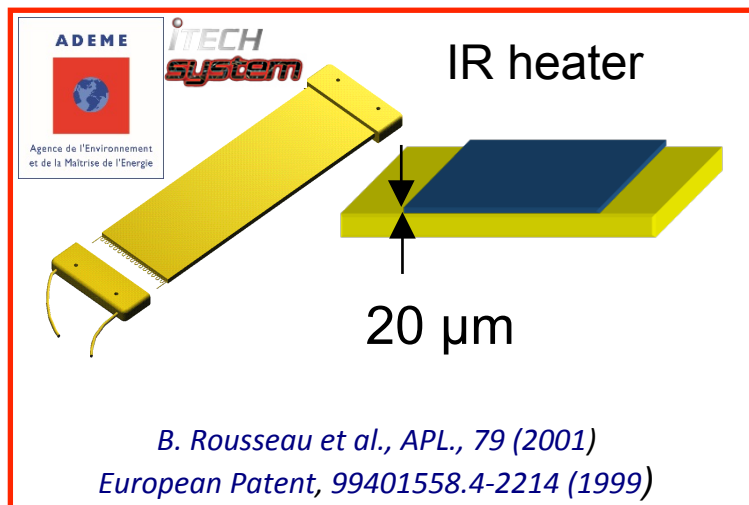
**Thank you for your  
attention !  
Some questions?**



**“Royal de Luxe” Theatre Company : an incredible show at Nantes!**

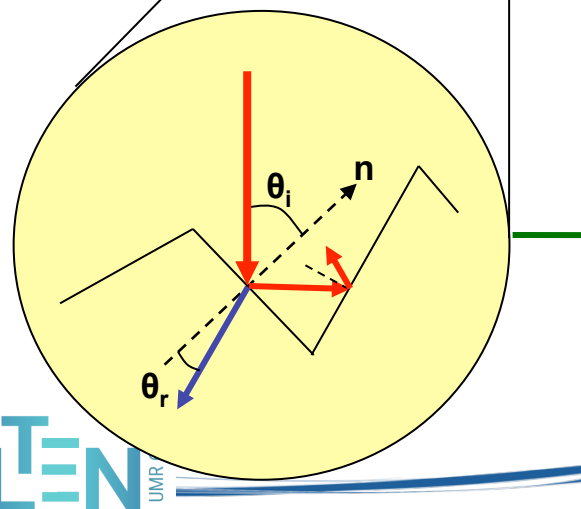
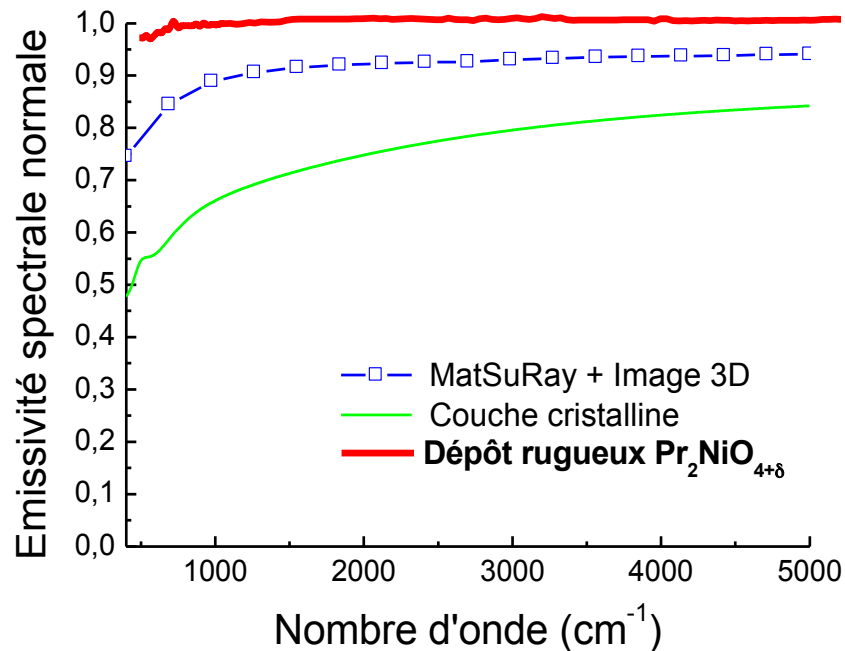
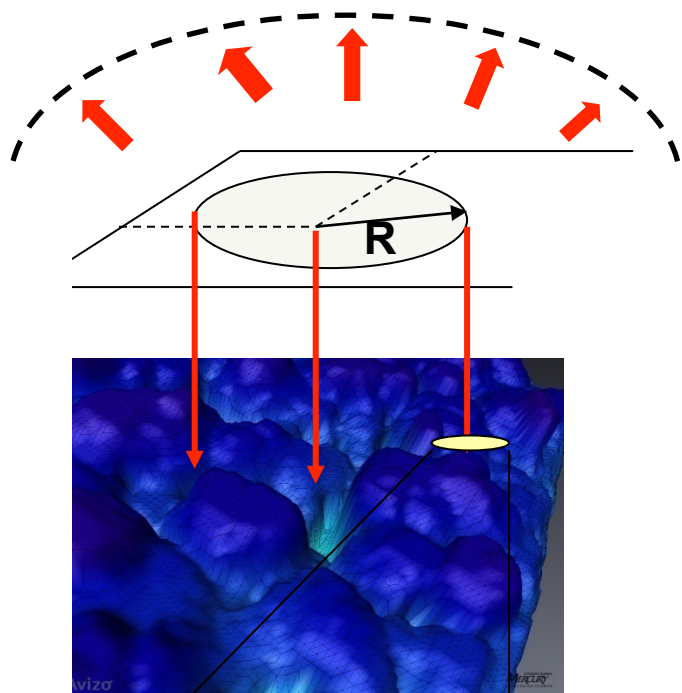


# "Plate" black body



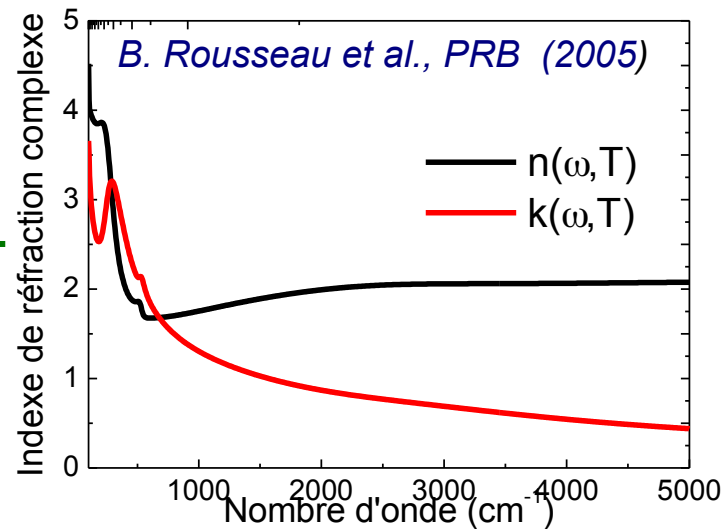


# Role of the “macro” roughness : GOA



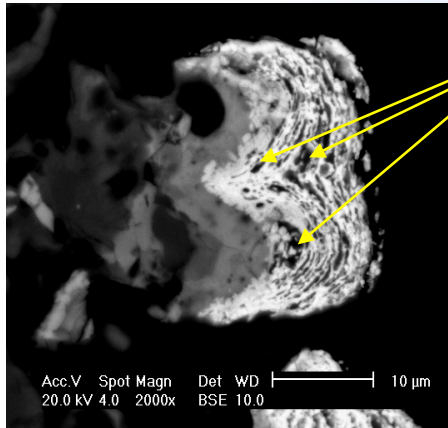
Local scale

$$\rho \downarrow \nu N \uparrow S$$





# Role of the “micro” porosity : EMA

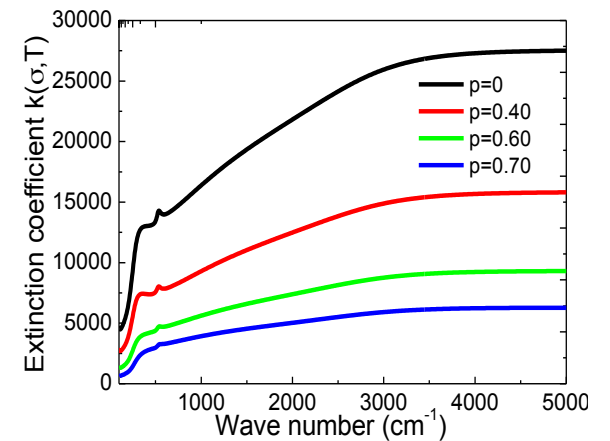
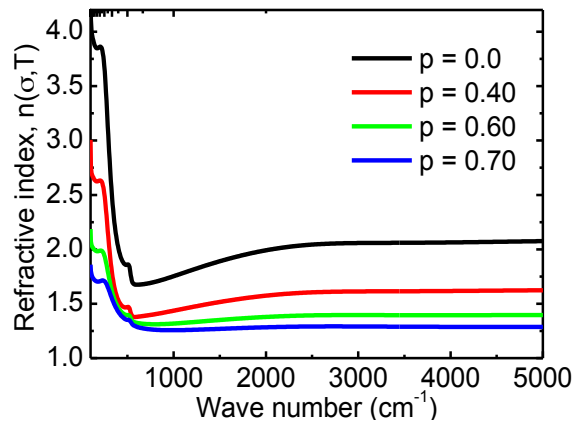
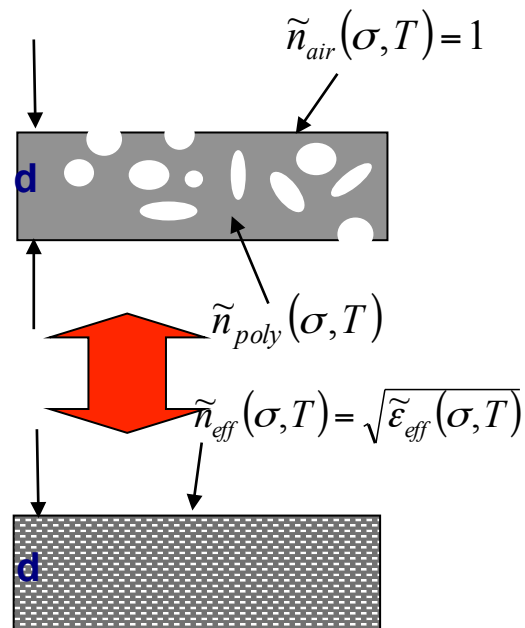


pore : 50 -200 nm

$d_{pore} \ll \lambda_{IR} (2-20 \mu m)$

$$(1-p) \frac{\tilde{\epsilon}_{poly}(\sigma, T) - \tilde{\epsilon}_{eff}(\sigma, T)}{\tilde{\epsilon}_{eff}(\sigma, T) + \gamma_{poly}(\tilde{\epsilon}_{poly}(\sigma, T) - \tilde{\epsilon}_{eff}(\sigma, T))} + p \frac{\tilde{\epsilon}_{pore}(\sigma, T) - \tilde{\epsilon}_{eff}(\sigma, T)}{\tilde{\epsilon}_{eff}(\sigma, T) + \gamma_{pore}(\tilde{\epsilon}_{pore}(\sigma, T) - \tilde{\epsilon}_{eff}(\sigma, T))} = 0$$

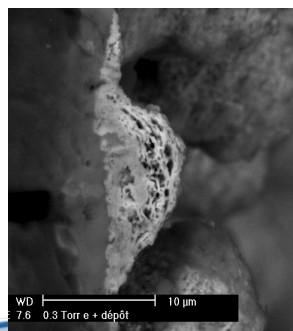
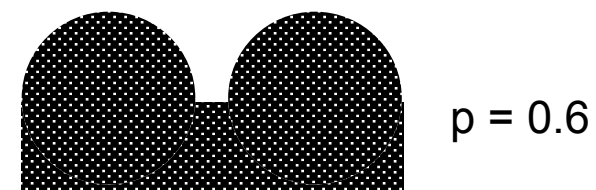
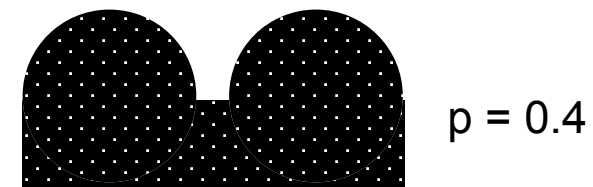
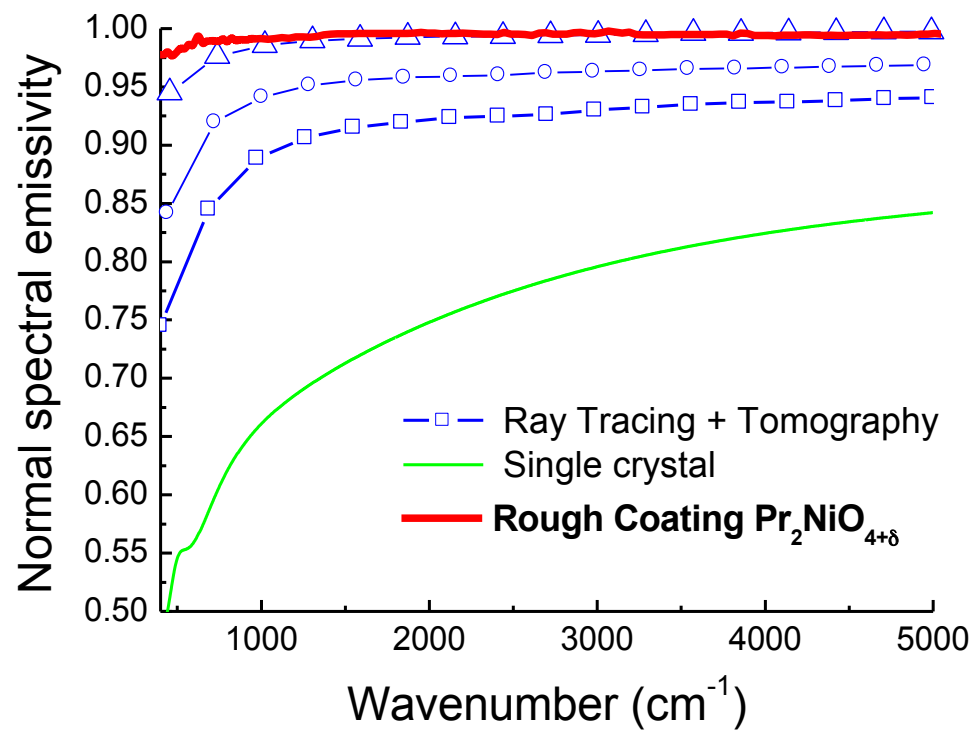
D.E. Apnes, optical properties of thin films, Thin Solid Films 89 (1982) 249



$p = 70\% d > 11 \mu m$  (opaque)



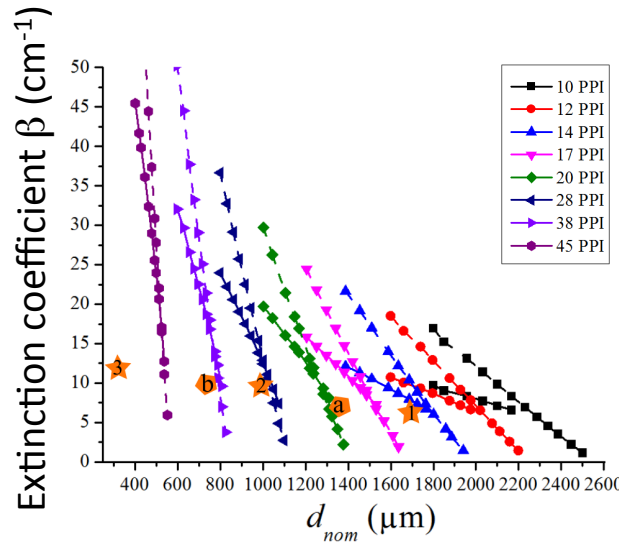
# Hybrid methodology : GOA+EMA



USAXS? SANS? Nanotomo X? FIB-SEM?



# RDFI METHOD → extinction coefficient, albedo, scattering phase function

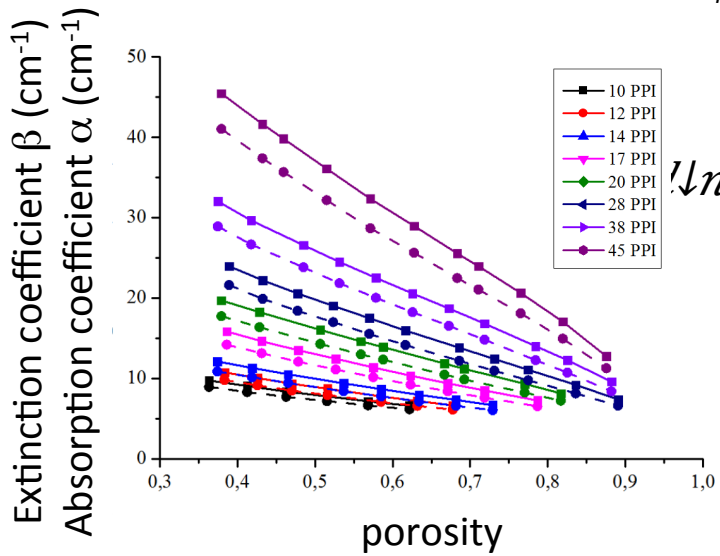


$$\kappa_{ev} = 2.45 \frac{(1 - 0.7p)}{d_{nom}}$$

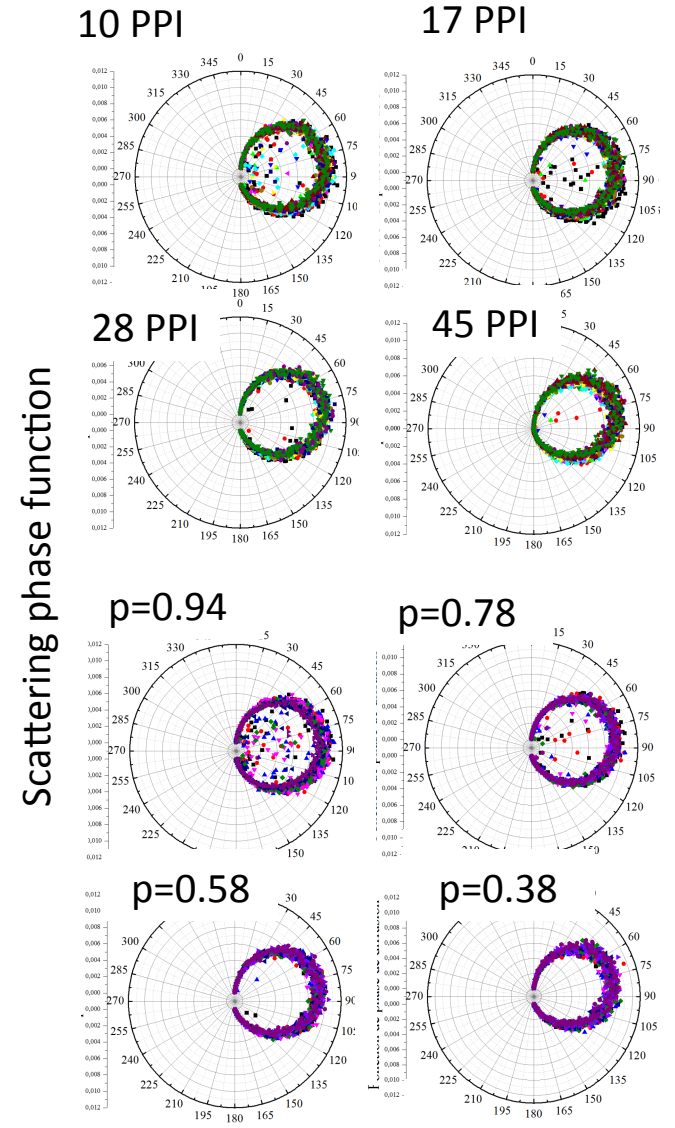


$$\kappa_{ev} = 4.8 \frac{(1 - p)}{d_{nom}}$$

Hendricks & Howell, Journal of Heat Transfer, 118(1):79-87 (1996)



$$d_{nom} = a \downarrow PPI p + b \downarrow PPI$$





# Radiative conductivity : optically thick media

## Rosseland approximation

asymmetry factor

$$\Gamma_v = 3\kappa_{ev} - g_v \kappa_{dv}$$

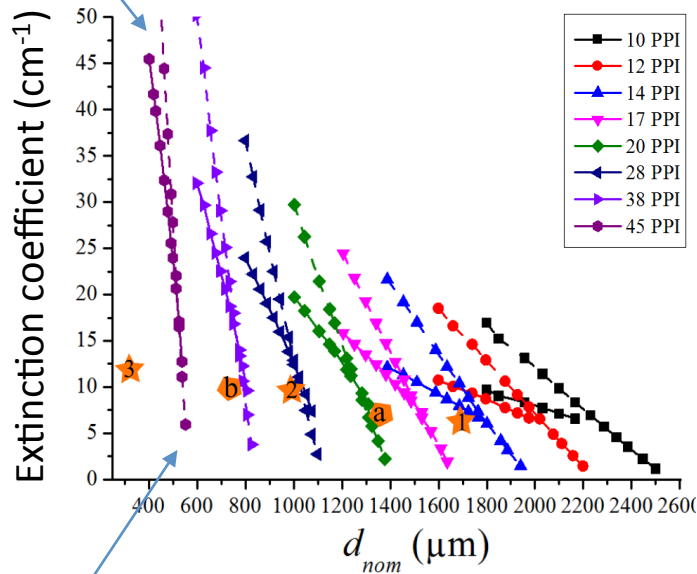


$$\Gamma_R = \frac{\int_0^\infty \frac{dI_v^0(T)}{dT} dv}{\int_0^\infty \frac{1}{\Gamma_v} \frac{dI_v^0(T)}{dT} dv}$$

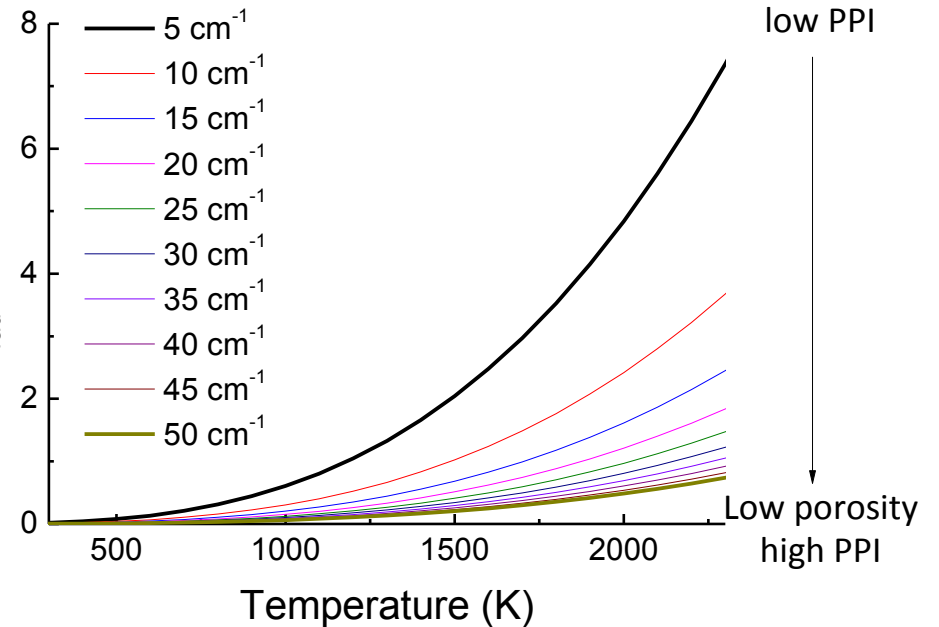


$$k_{rad} = \frac{16n^2 \sigma_B T^3}{\Gamma_R}$$

p=0.4



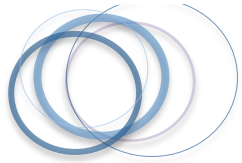
$k_{rad} W(m.K)^{-1}$



p=0.9

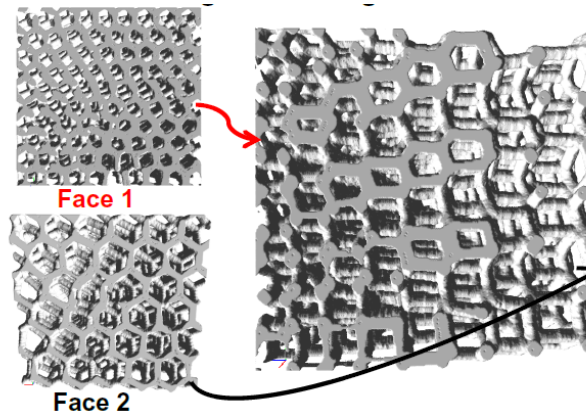




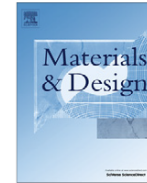


## Future works...

- To characterize the thermal behavior (conduction/radiation) of SiC open-cell foams above  $T = 1300$  K in relation with degradation mechanisms (corrosion, mechanical failures,...)
- To play, by numerical modelling, on the surface properties of the struts (roughness, selective/protective coatings) at high temperature
- To compute thermal conductivities with FEM (Freefem++)
- To design foam with pore size gradient : effect on the REV ? → 3D printing?



- Applications with thermal insulators, heat exchangers, radiant gas burners,...

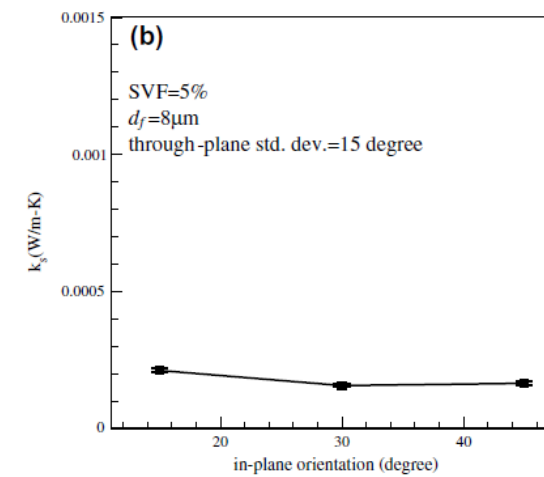
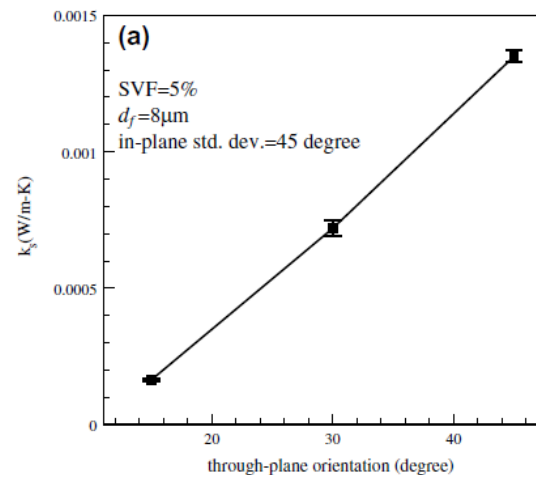
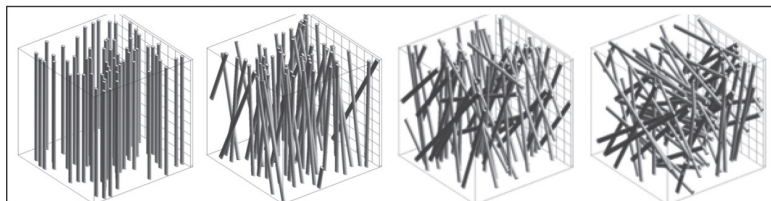
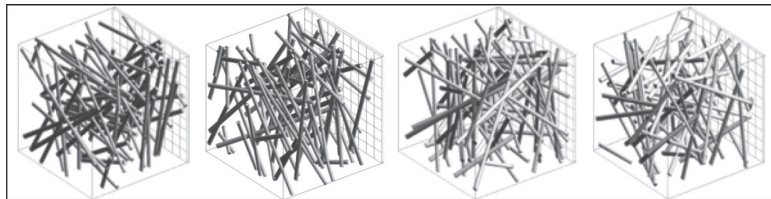
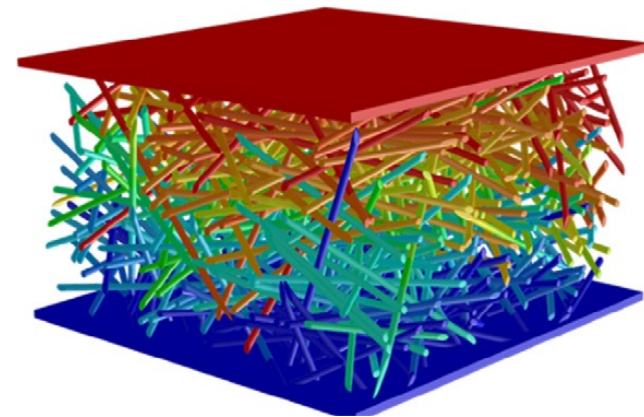


## A simple simulation method for designing fibrous insulation materials

R. Arambakam<sup>a</sup>, H. Vahedi Tafreshi<sup>a,\*</sup>, B. Pourdeyhimi<sup>b</sup>

<sup>a</sup>Department of Mechanical and Nuclear Engineering, Virginia Commonwealth University, Richmond, VA 23284-3015, United States

<sup>b</sup>Nonwovens Cooperative Research Center, The Nonwovens Institute, NC State University, Raleigh, North Carolina 27695-8301, United States





## Five selected papers

**2007** : B. Rousseau, D. de Sousa Meneses, P. Echegut, M. Di Michiel, and J.-F. Thovert, "Prediction of the thermal radiative properties of an x-ray  $\mu$ -tomographed porous silica glass," *Applied Optics*, 46[20] 4266-76 (2007).

**2010** : B. Rousseau, H. Gomart, D. Zanghi, D. Bernard, and S. M., "Synchrotron x-ray  $\mu$ -tomography to model the thermal radiative properties of an opaque ceramic coating at T = 1000 K," *Journal of Materials Research*, 25 1890-97 (2010).

**2011** : B. Rousseau, D. De Sousa Meneses, P. Echegut, and J.-F. Thovert, "Textural parameters influencing the radiative properties of a semitransparent porous media," *International Journal of Thermal Sciences*, 50[2] 178-86 (2011).

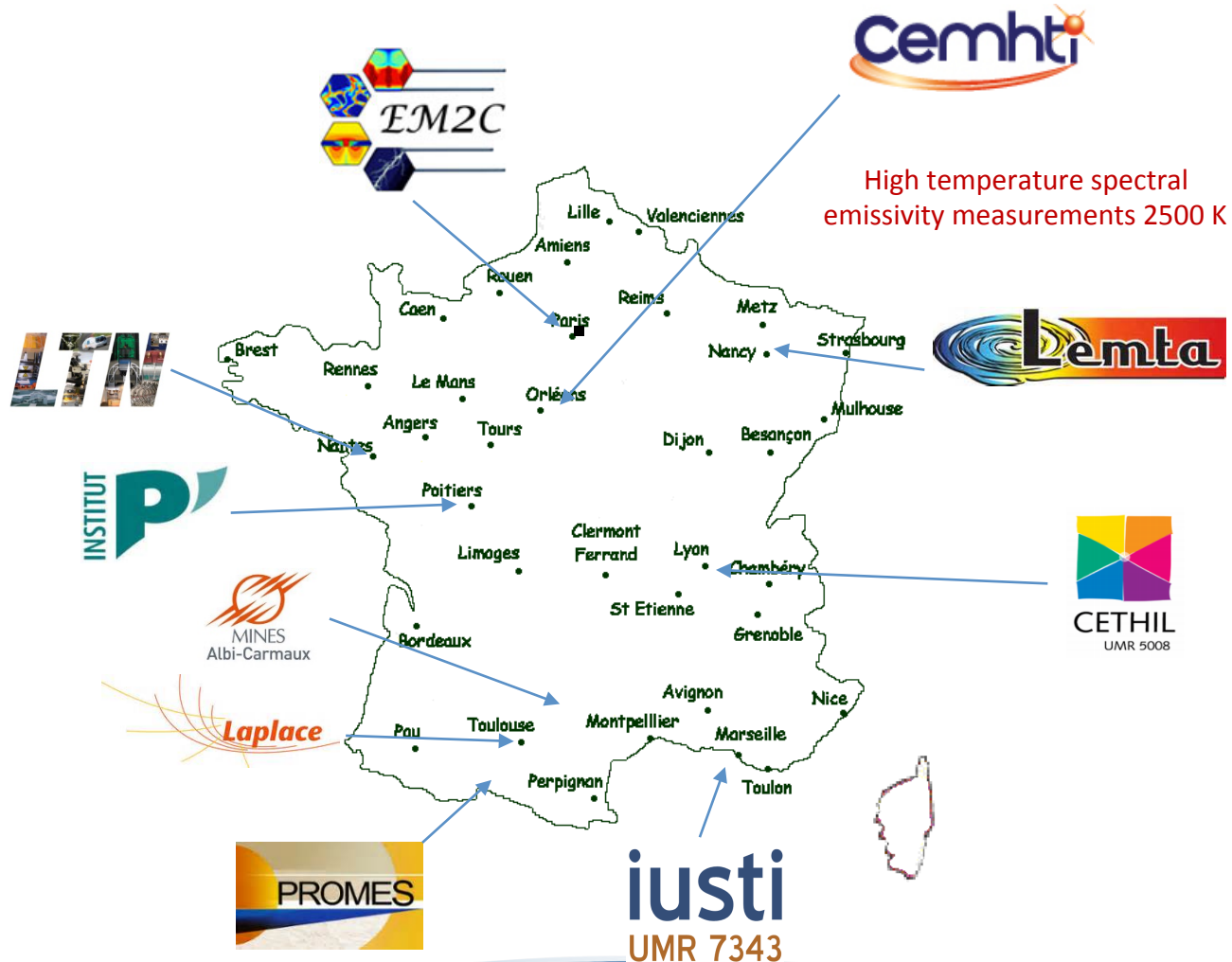
**2015** : S. Guevelou, B. Rousseau, G. Domingues, J. Vicente, G. Flamant, and C. Caliot, "Evolution of the homogeneized volumetric radiative properties of a family of  $\alpha$ -SiC foams with growing nominal pore diameter " *Journal of Porous Media*, 18[10] (2015).

**2017** : S. Guévelou, B. Rousseau, G. Domingues, and J. Vicente, "A simple expression for the normal spectral emittance of open-cell foams composed of optically thick and smooth struts," *Journal of Quantitative Spectroscopy and Radiative Transfer*, 189 329-38 (2017)



# GDR ACCORT : French research network from CNRS Radiative heat transfer in semi-transparent materials

<http://www.gdr-accort.cnrs.fr/>



# ETR 2017 “Ecole thématique transferts radiatifs en milieux semi-transparentes”

Piriac-sur-Mer, France, May 13-19 2017

<http://www.etr2017.cnrs.fr/>

Responsable : Benoit Rousseau

ETR 2017  
Ecole Thématique ETR 2017



OBJECTIFS    COMITÉ SCIENTIFIQUE    COMITÉ D'ORGANISATION    PROGRAMME ET INTERVENANTS    INSCRIPTIONS    INFOS PRATIQUES

**NOS TUTELLES**



**NOS PARTENAIRES**



**RECHERCHER**

Sur ce site  OK  
Sur le Web du CNRS  OK

**Ecole Thématique ETR 2017**  
publié le 10 janvier, mis à jour le 2 décembre 2016 à 11h07min  
ECOLE TRANSFERTS RADIATIFS EN MILIEUX SEMITRANSARENTS  
13-19 mai 2017  
VVF Piriac-sur-Mer  
Cette école est organisée dans le cadre du GDR ACTION Concertée en Rayonnement Thermique (ACCORT) qui regroupe dix laboratoires universitaires possédant chacun de fortes activités de recherche, expérimentales et numériques, dans le domaine des transferts radiatifs.  
Elle vise un public composé d'ingénieurs de l'industrie ou des établissements publics, de chercheurs universitaires et d'étudiants doctorants, confrontés à des problèmes de transferts thermiques où le rayonnement volumique joue un rôle important, notamment dans les matériaux denses ou divisés (mousses, fibreux, céramiques, etc) et dans les gaz, éventuellement en présence de particules (suies, gouttelettes, etc.)  
Cette école fera un focus particulier sur la prise en compte des transferts radiatifs dans les matériaux, des nano-échelles aux macro-échelles.

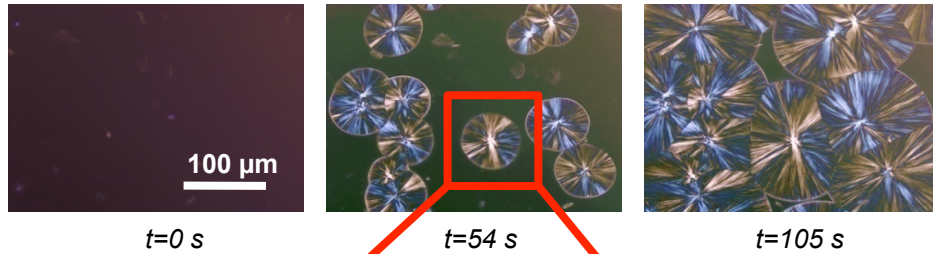




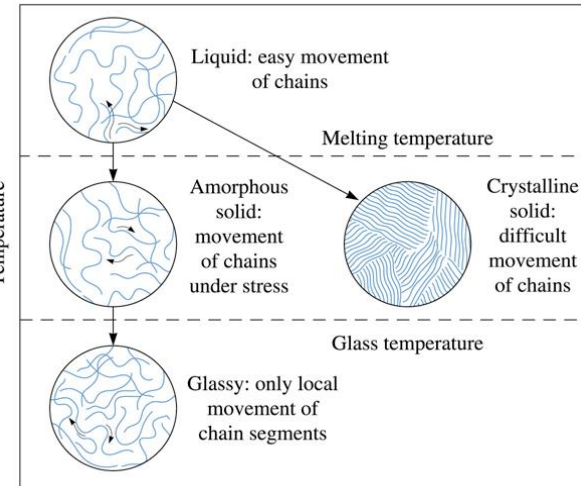
# Isotactic PolyPropylene (iPP)\* : a multi scale medium for scattering and absorbing thermal radiations

iPP pellets  $\xrightarrow{T,P,s}$  iPP slab

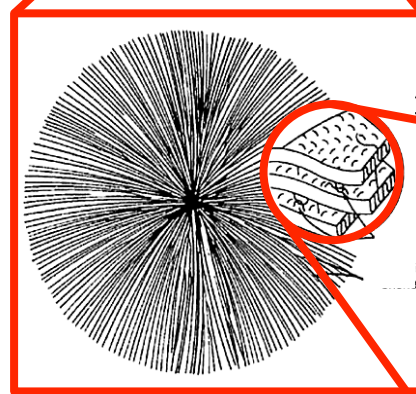
Thermal history  $\leftrightarrow$  elaboration process



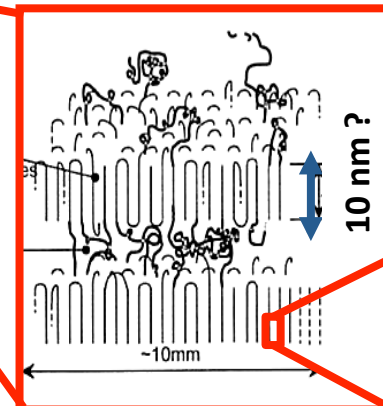
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Semicrystalline matrix

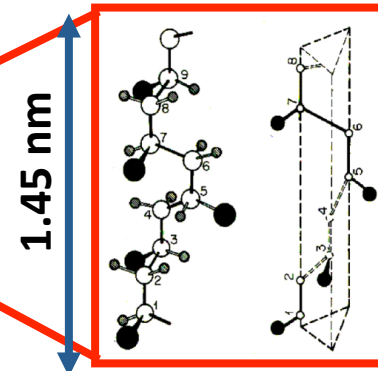


10-100 μm



10-100 μm

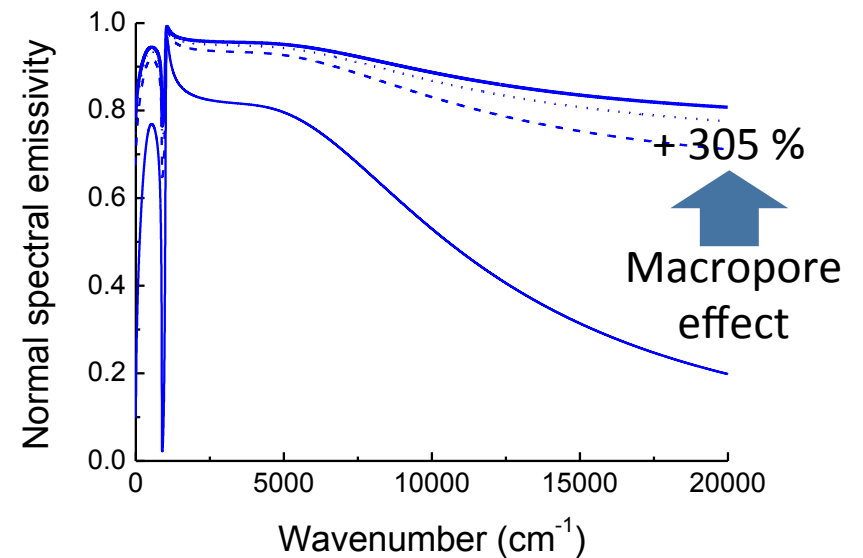
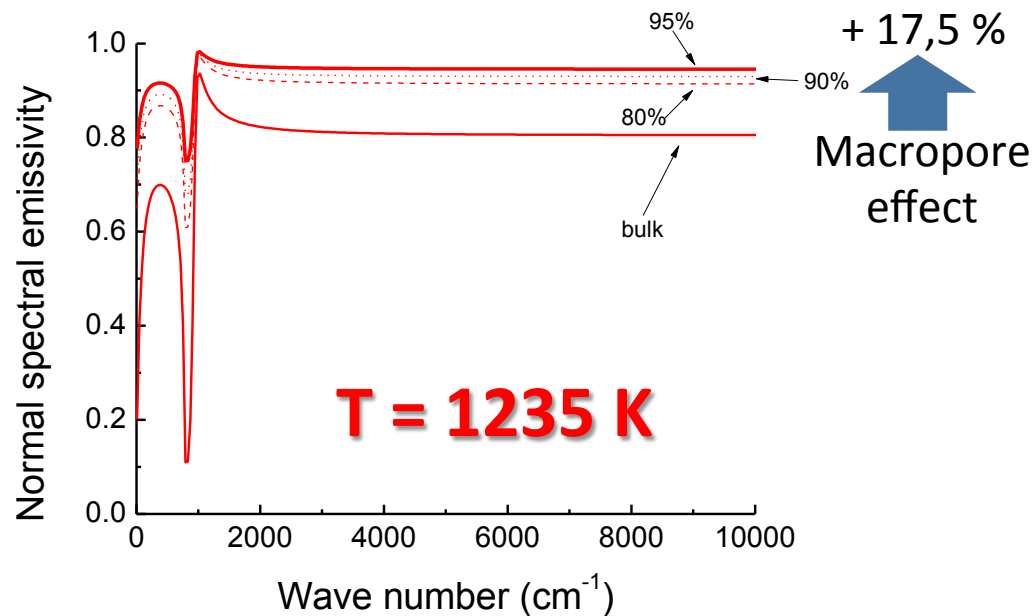
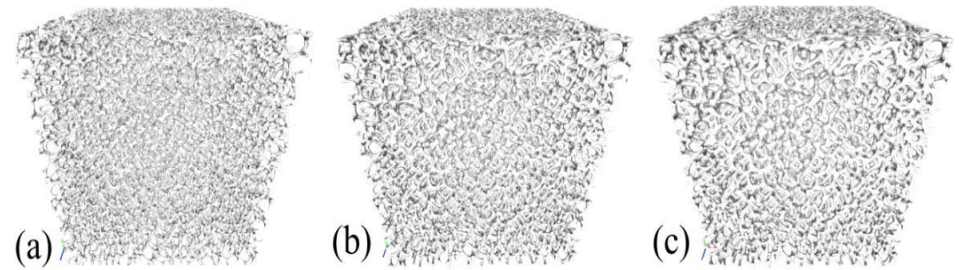
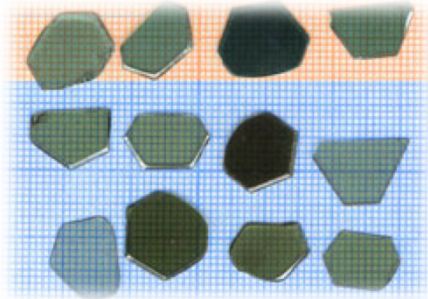
Helicoidal chains : low symmetry crystal



\*Polymerization of iPP discovered by Natta & Rehn in 1954



# Is there an additional phenomenon than that associated with texture?

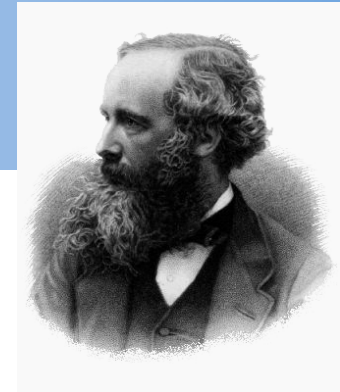


B. Rousseau et al., AIP Advances 2016 6 065226

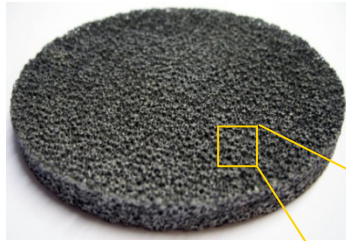




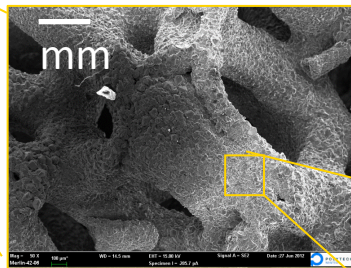
# Need to develop a multi-length scale approach for modelling TRPs



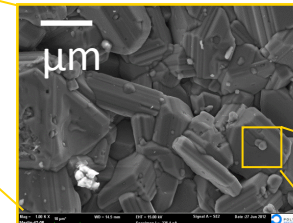
complex refractive indexes



$\alpha$ -SiC foam



$$\rho_{2 \rightarrow 1} = \frac{1}{2} \left[ |\tilde{r}_{perp}|^2 + |\tilde{r}_{para}|^2 \right]$$

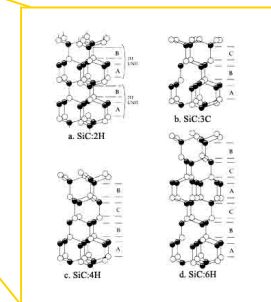


$$\tilde{r}_{perp} = \frac{E_{perp,r}}{E_{perp,i}} = \frac{\cos \Theta_i - \tilde{m} \cos \Theta_t}{\cos \Theta_i + \tilde{m} \cos \Theta_t}$$

$$\tilde{r}_{para} = \frac{E_{para,r}}{E_{para,i}} = \frac{\cos \Theta_t - \tilde{m} \cos \Theta_i}{\cos \Theta_t + \tilde{m} \cos \Theta_i}$$

$$\tilde{m} = \frac{\tilde{n}_1}{\tilde{n}_2}$$

$$n + ik = \sqrt{\epsilon' + i\epsilon''}$$



nm



# Spectroscopie de réflexion/transmission/émission

→ 900 K

BRDF/BTDF → 700 K

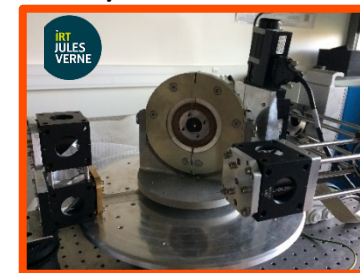
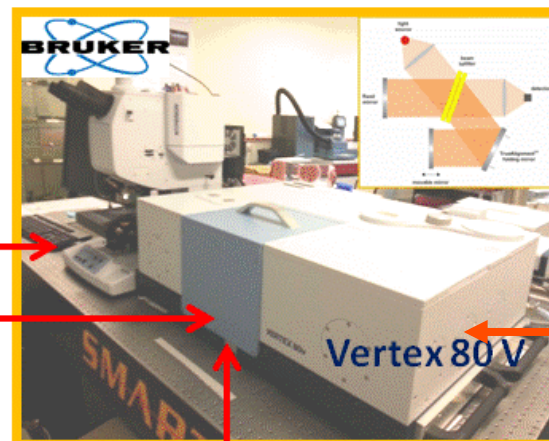
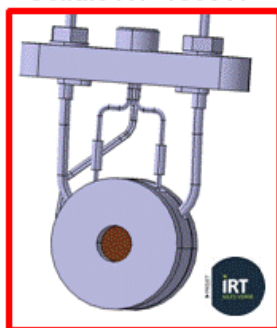
Financement : CPER 2007-2013



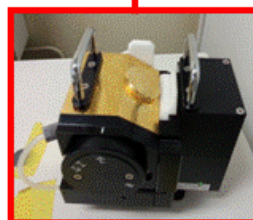
IR lointain → Visible ( $0.4 < \lambda < 200 \mu\text{m}$ )

Microscope IR réflexion/transmission  
( $2 < \lambda < 25 \mu\text{m}$ )

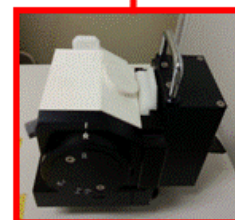
Cellule HT → 900 K



Platine réflexion/transmission  
( $1.4 \mu\text{m} < \lambda < 200 \mu\text{m}$ )



Sphère intégrante dorée  
 $\phi = 75 \text{ mm}$   
( $1.4 \mu\text{m} < \lambda < 25 \mu\text{m}$ )



Sphère intégrante téflon  
 $\phi = 75 \text{ mm}$   
( $0.4 \mu\text{m} < \lambda < 1.4 \mu\text{m}$ )