

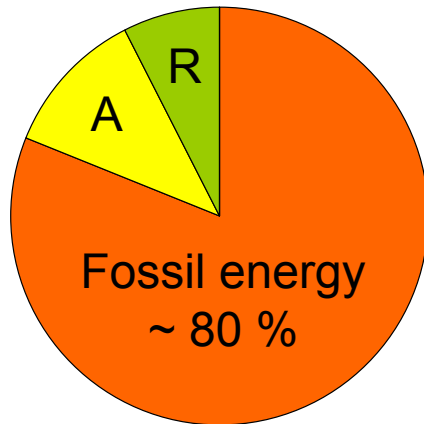
Modelica based simulation model of a Pulse Tube Engine

Stefan Moldenhauer and André Thess

TU Ilmenau (Germany)

- 1 Unused waste heat
- 2 Technologies for waste heat usage
- 3 The Pulse Tube Engine
- 4 Modelica based simulation model & results
- 5 Summary

Unused waste heat



Thermal
energy conversion



Problem: 30..60 % of waste heat

Usage ?

Large-scale

- Gas turbine combined cycle

Small-scale

- no practical solution!

Technologies for waste heat usage

Thermodynamic cycles

- Gas cycles (Stirling etc.)
 - low specific power output
- Organic–Rankine–Cycle (ORC)
 - complex systems, thermal instability of working fluids

Problem: accident-sensitive, cost-intensive, heavy

Thermoelectric materials

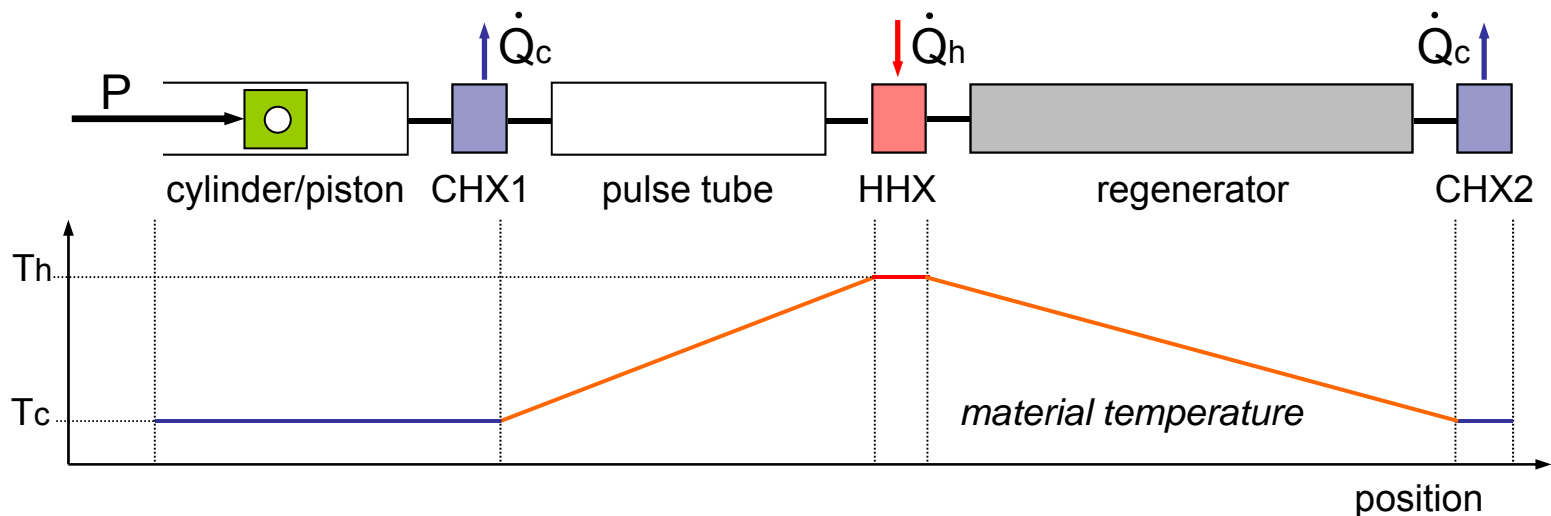
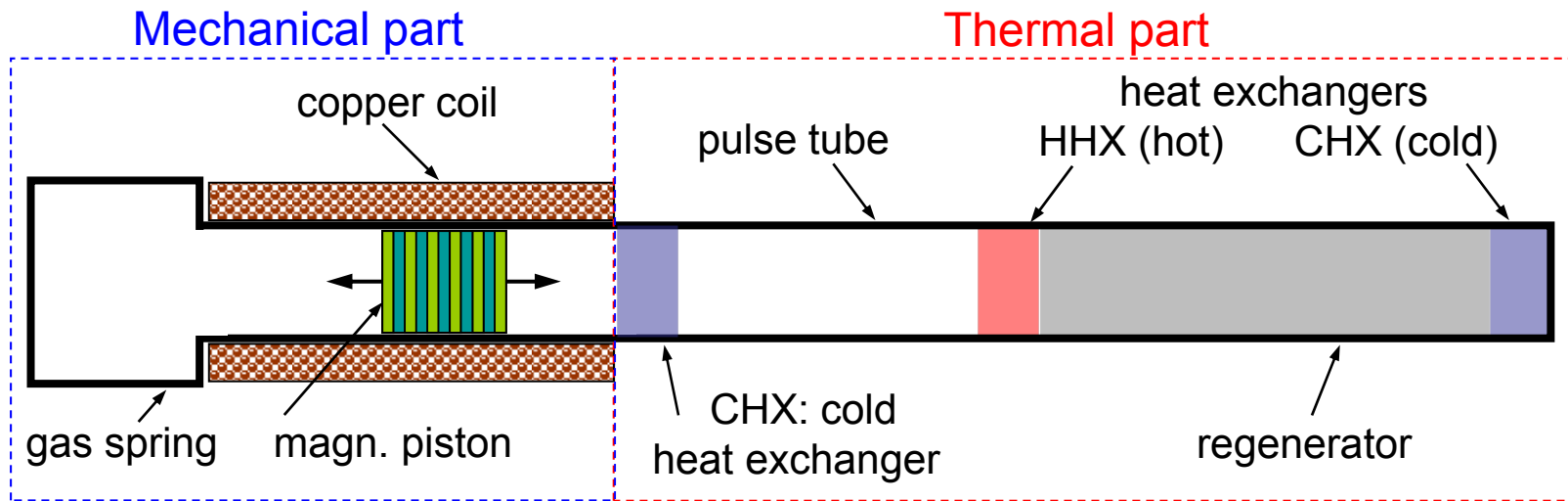
- Seebeck-Effect
 - low thermal efficiency, expensive materials

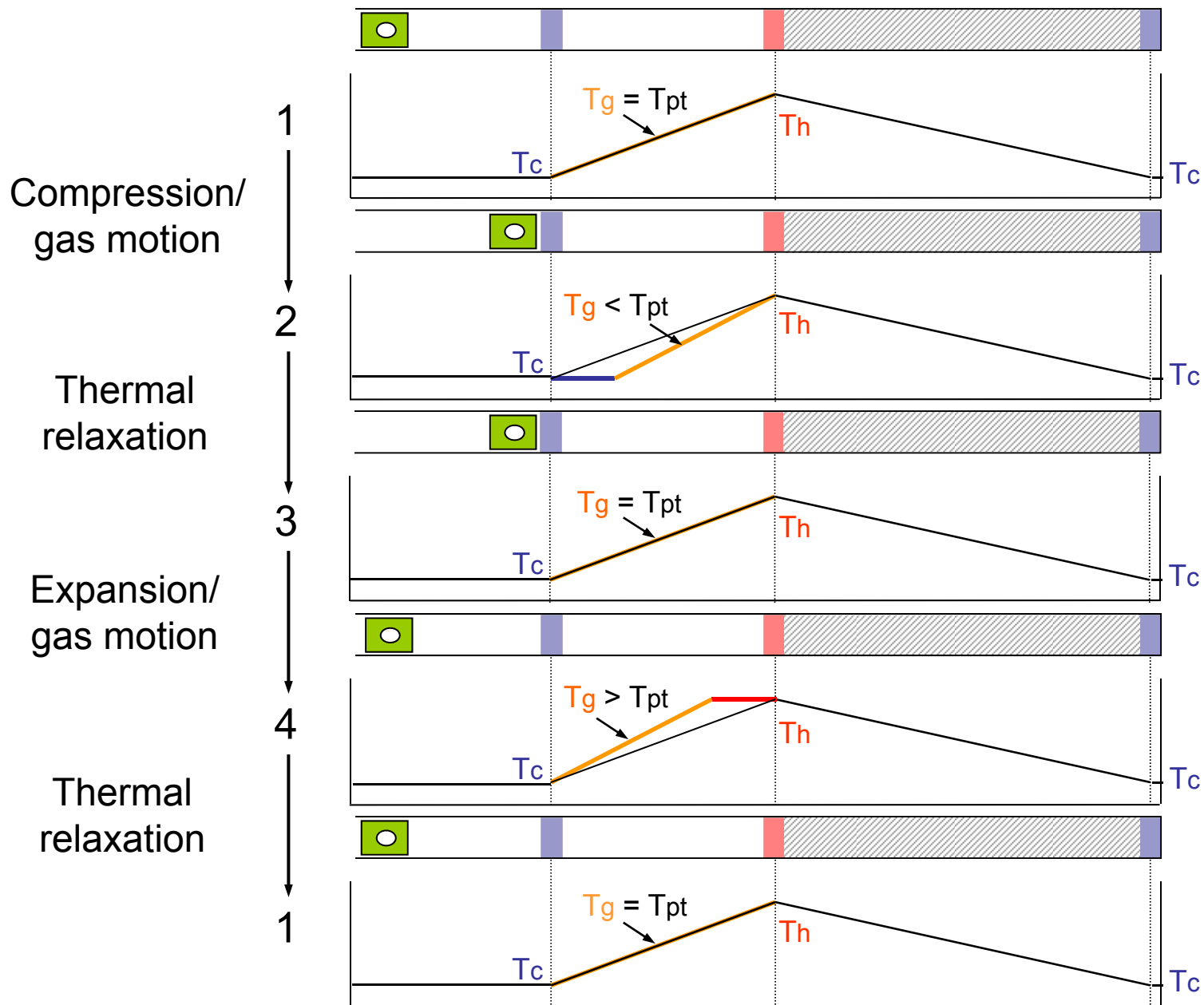
Problem: not profitable



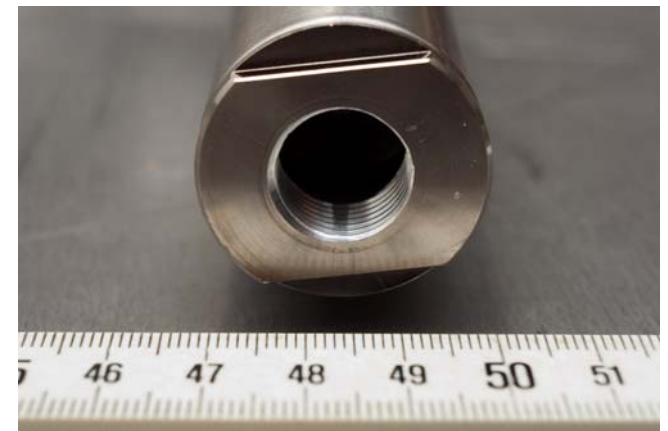
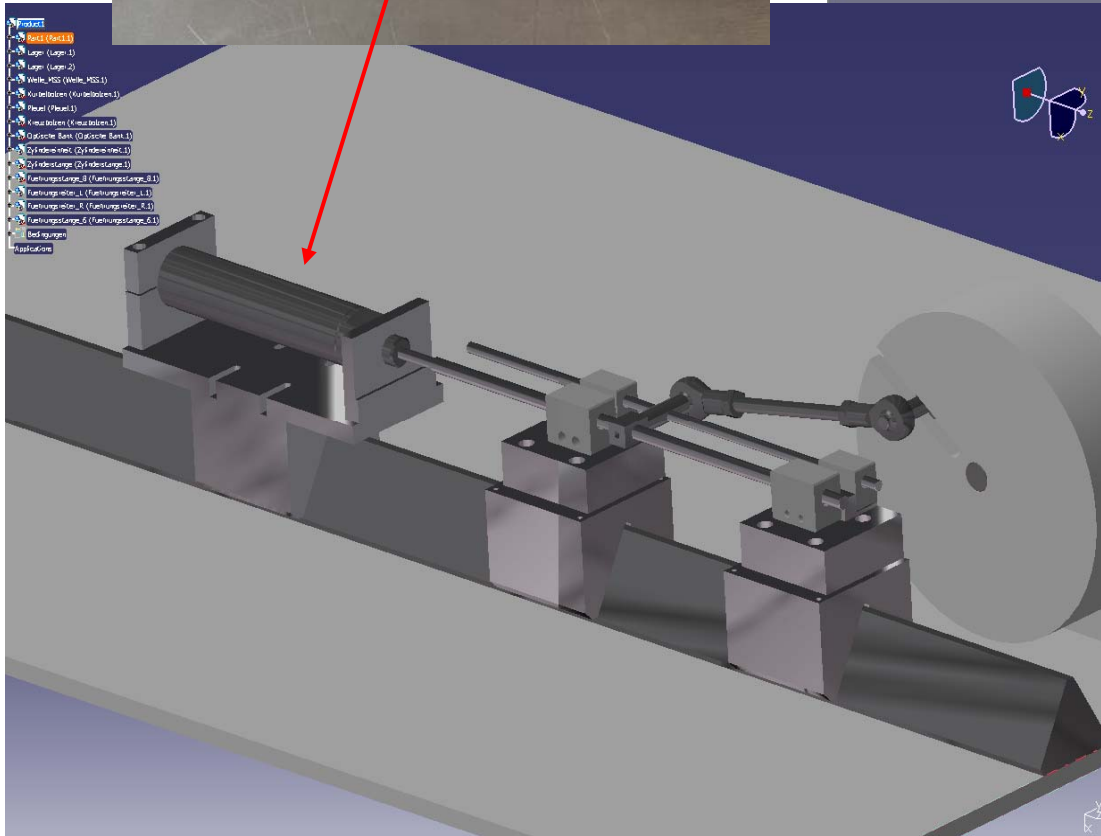
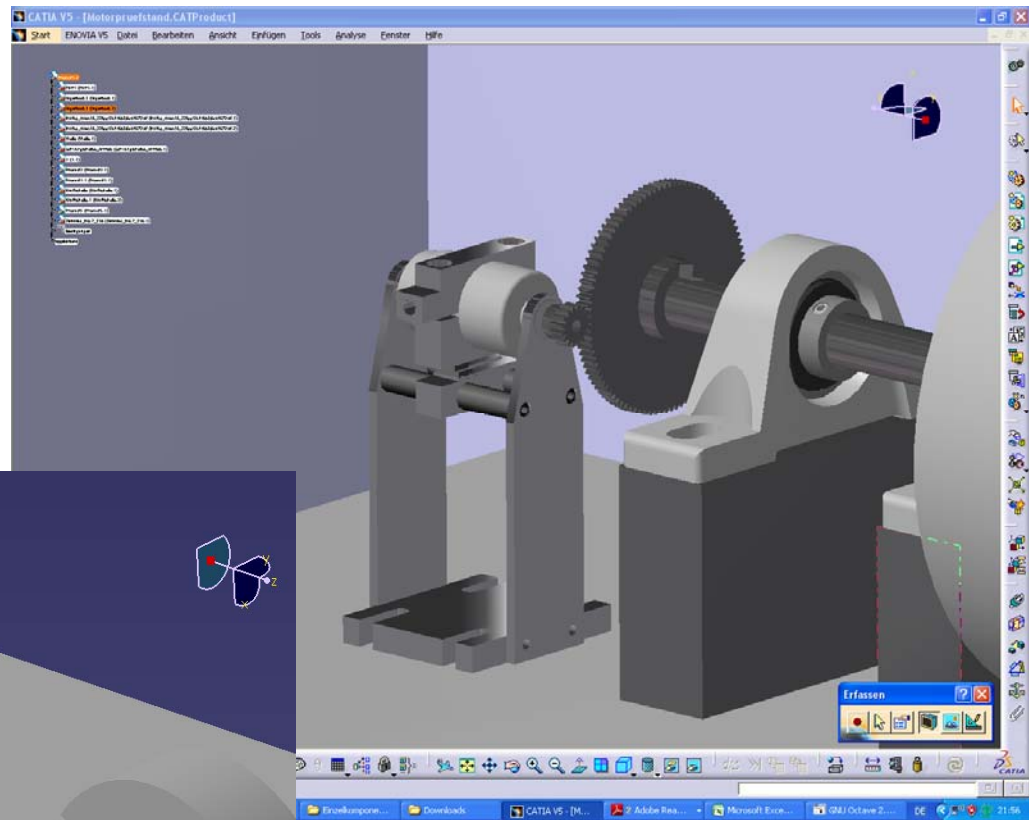
Objective: Simple and efficient prime mover

Proposition: The Pulse Tube Engine (Hamaguchi 2005, Organ 2007)



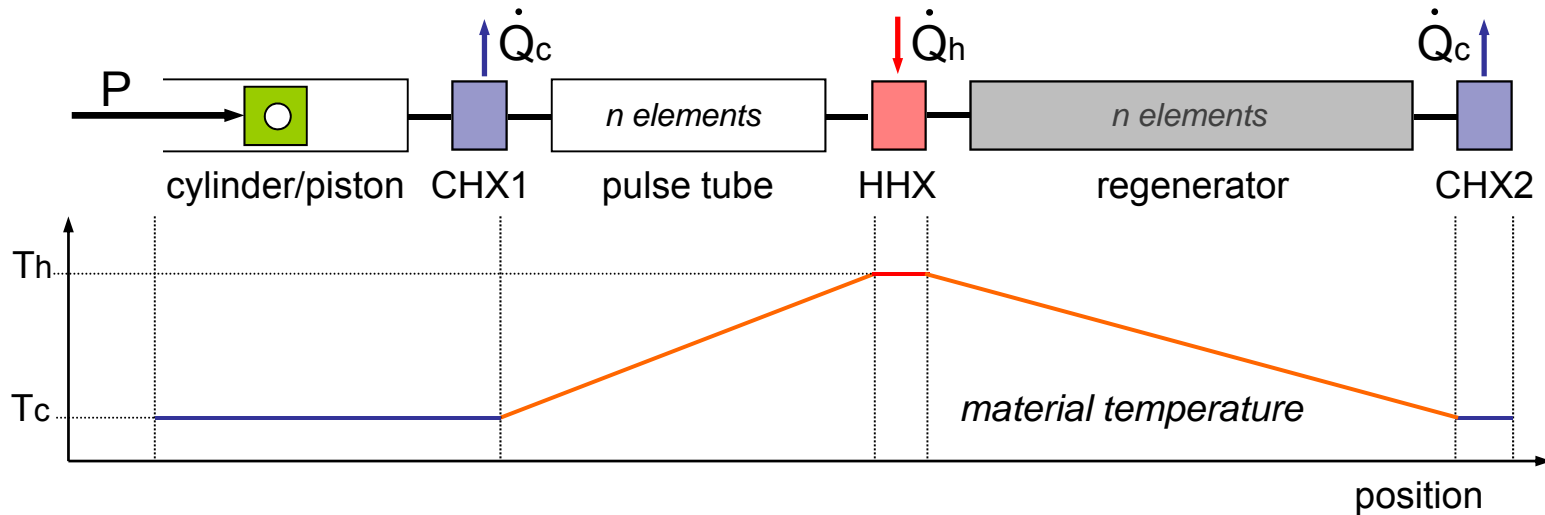


Experiment



Modelica based simulation model

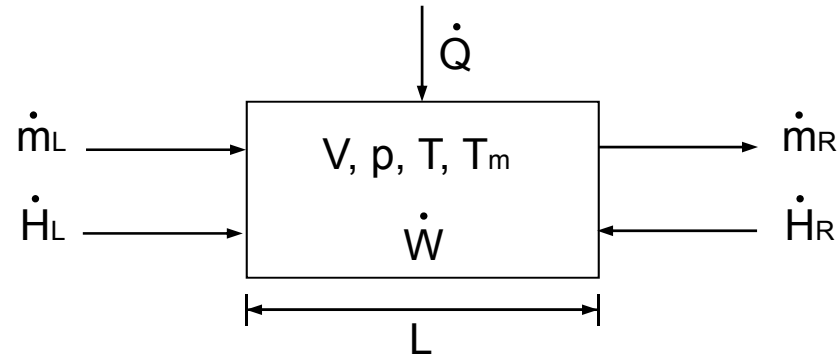
Step 1: Segmenting in components



Step 2: Simplifications & assumptions

- working fluid is a perfect gas
- one-dimensional flow
- no temporal change in material temperature
- experimental relations for heat transfer and friction

Step 3: Balance for mass, energy and momentum



$$\dot{Q} = \alpha A_w (T_m - T), \quad \dot{W} = -p \frac{dV}{dt}, \quad \dot{H} = \dot{m} c_p T$$

System of coupled differential equations

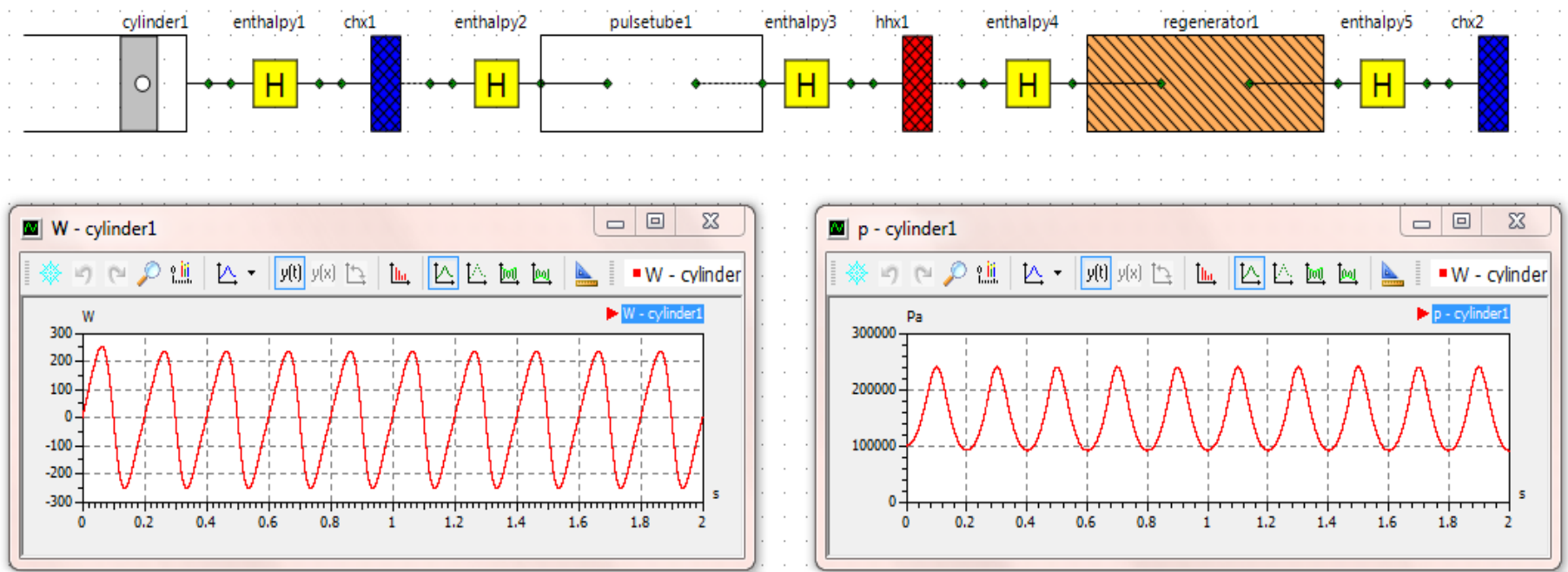
$$\frac{dp}{dt} = (\dot{m}_{in} - \dot{m}_{out}) \frac{R T}{V} - \frac{p}{V} \frac{dV}{dt} + \frac{p}{T} \frac{dT}{dt}$$

$$c_v \frac{p V}{R T} \frac{dT}{dt} = -c_v T (\dot{m}_{in} - \dot{m}_{out}) + \sum_i (\dot{Q}_i + \dot{W}_i + \dot{H}_i)$$

$$\frac{\partial \dot{m}}{\partial t} = -\frac{R T}{p A_g} \frac{\partial \dot{m}^2}{\partial x} - A_g \frac{\partial p}{\partial x} - \frac{2 f_R |\dot{m}| \dot{m}}{\rho A_g^2 d_h}$$

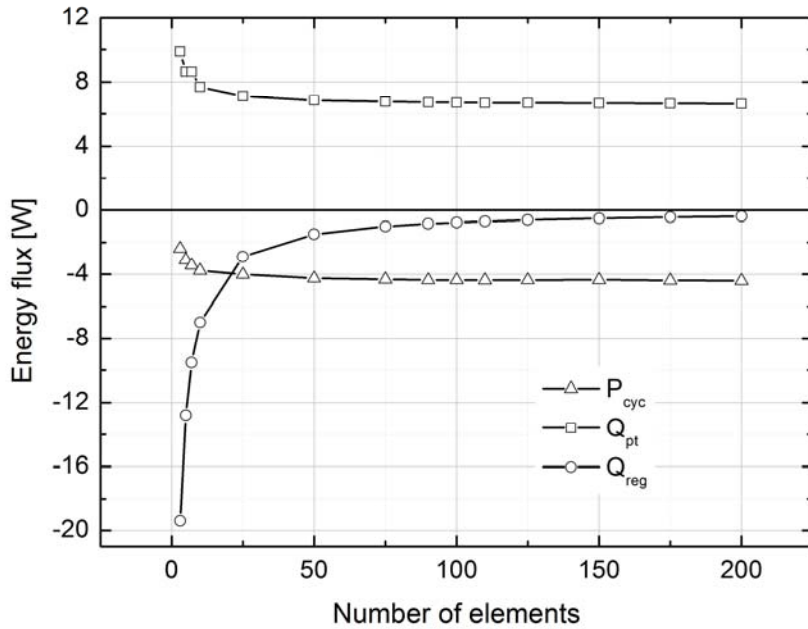
Step 4: Solving the system of differential equations

- numerical integration via implementation in Modelica
- environment: SimulationX 3.3 (ITI GmbH)

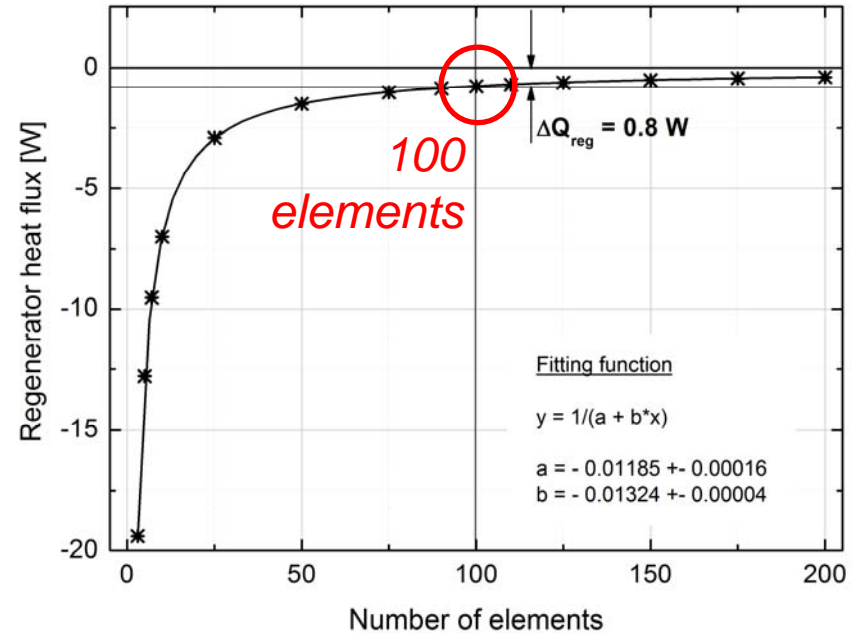


SimulationX representation of the Pulse Tube Engine

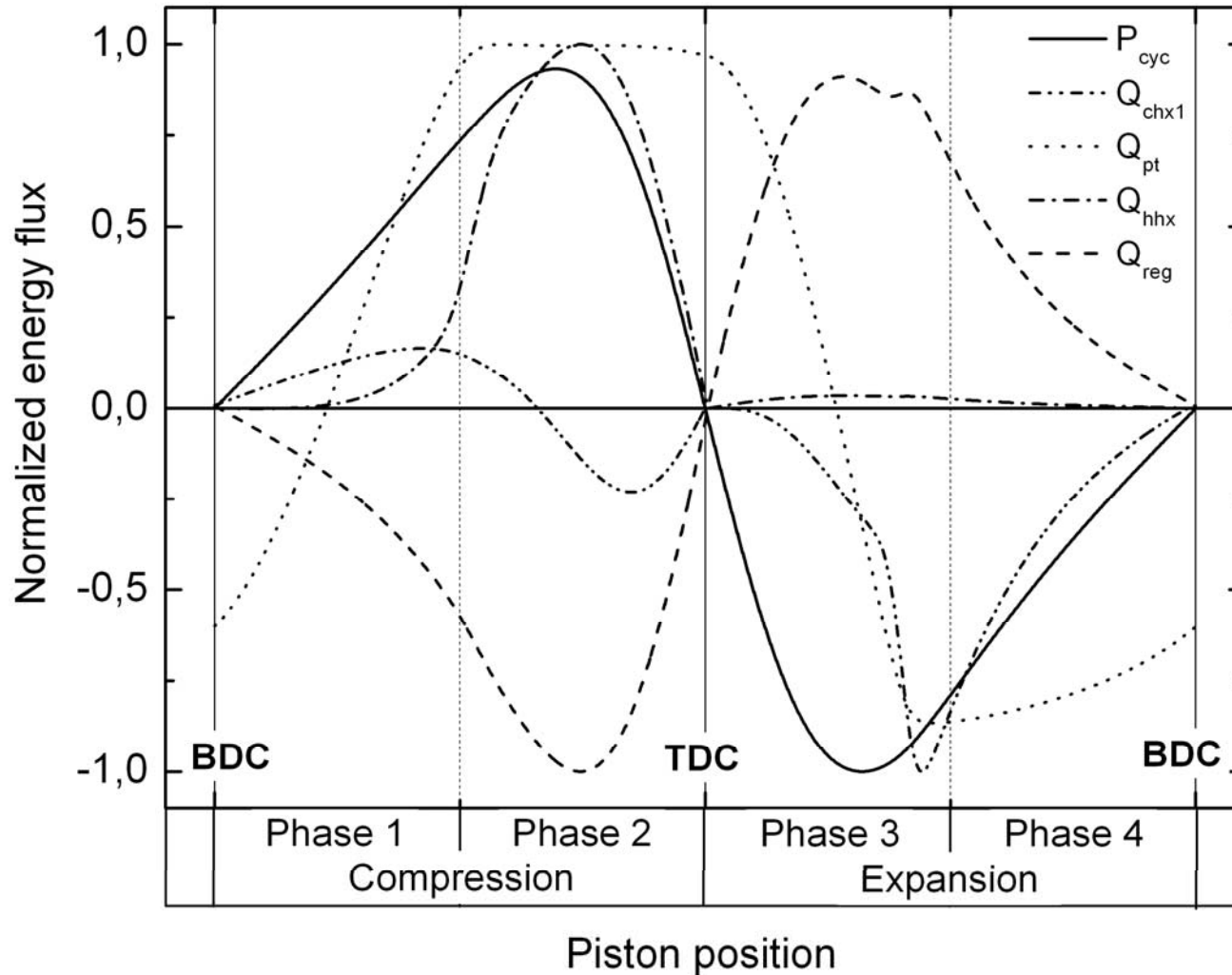
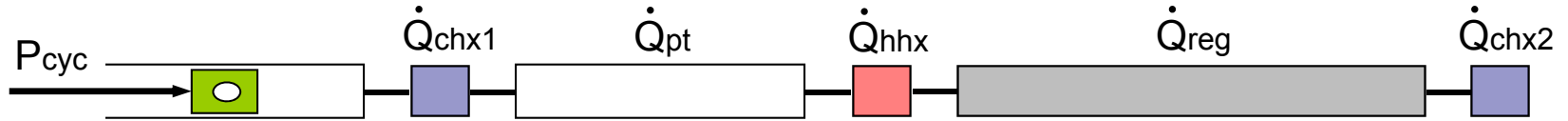
Step 5: Defining the number of pulse tube / regenerator elements



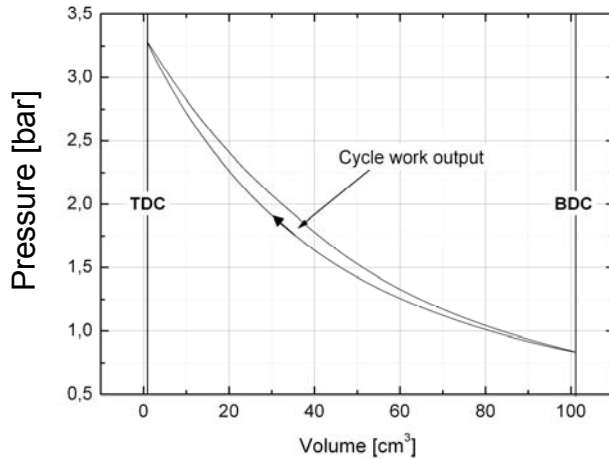
Model of an ideal regenerator



Results – Energy fluxes

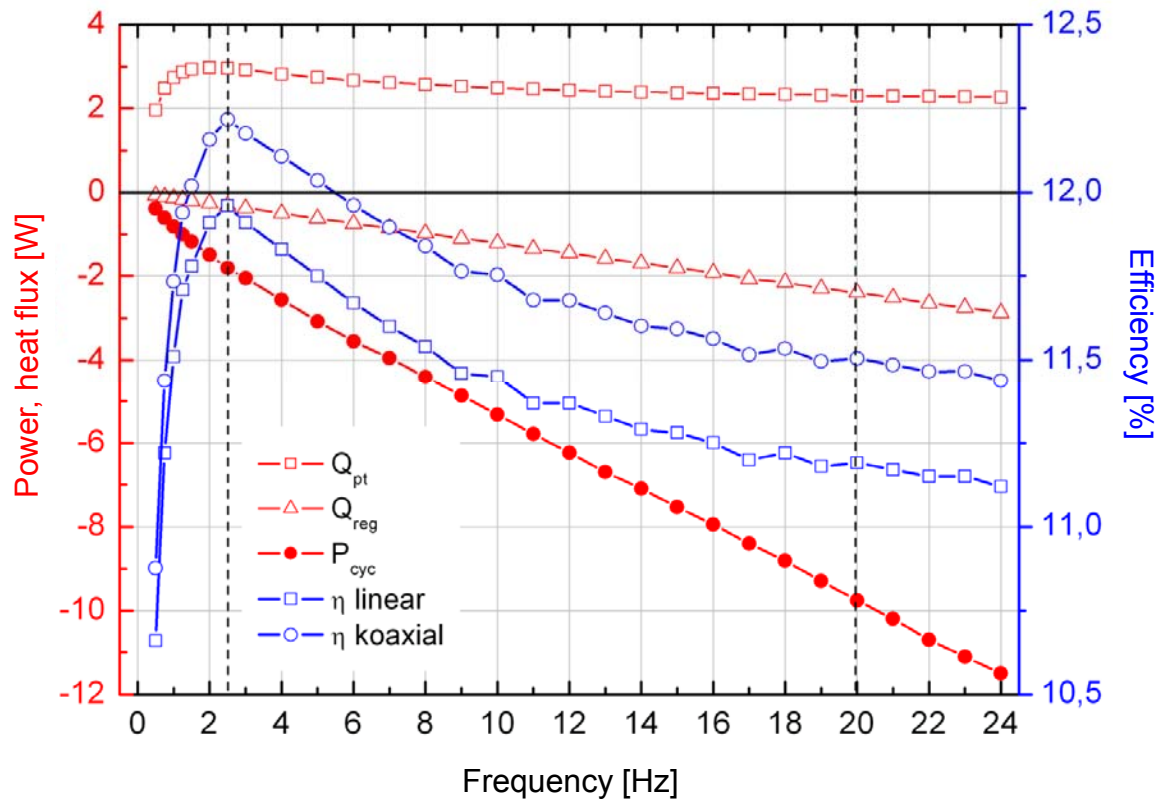


Performance of the Pulse Tube Engine



$V_s = 100 \text{ cm}^3$
 $p_{\text{fill}} = 1 \text{ bar}$
 $T_h = 600 \text{ K}$ (waste heat)
 $T_c = 300 \text{ K}$ (ambient)

$P_{\text{out}} = 3 \text{ W}$
 $\eta = 12\%$ @ $f = 5 \text{ Hz}$



Summary

- Pulse Tube Engine = simple prime mover
- only one moving component in the cold region
- SimulationX model allows to study physical properties
- model based optimization is possible

Possibility of a market for small pressurized engines!

